

UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS International General Certificate of Secondary Education

CANDIDATE NAME				
CENTRE NUMBER		CANDIDATE NUMBER		
MATHEMATICS		0580/42		
Paper 4 (Extende	ed)	May/June 2010		
		2 hours 30 minutes		
Candidates answ	ver on the Question Paper.			
Additional Materials: Electronic calculator Mathematical tables (optional)		Geometrical instruments Tracing paper (optional)		

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.Write in dark blue or black pen.You may use a pencil for any diagrams or graphs.Do not use staples, paper clips, highlighters, glue or correction fluid.DO **NOT** WRITE IN ANY BARCODES.

Answer all questions.

If working is needed for any question it must be clearly shown below that question.

Electronic calculators should be used.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place. For π use either your calculator value or 3.142.

At the end of the examination, fasten all your work securely together. The number of marks is given in brackets [] at the end of each question or part question.

The total of the marks for this paper is 130.

This document consists of 19 printed pages and 1 blank page.



1	Alb	perto and Maria share \$240 in the ratio 3 : 5.	For Examiner's Use
	(a)	Show that Alberto receives \$90 and Maria receives \$150.	Ose
		Answer(a)	
	(b)	 (i) Alberto invests his \$90 for 2 years at r % per year simple interest. At the end of 2 years the amount of money he has is \$99. Calculate the value of r. 	
		<i>Answer(b)</i> (i) <i>r</i> = [2] (ii) The \$99 is 60% of the cost of a holiday. Calculate the cost of the holiday.	
	(c)	<i>Answer(b)</i> (ii) \$ [2] Maria invests her \$150 for 2 years at 4% per year compound interest. Calculate the exact amount Maria has at the end of 2 years.	
	(d)	 Answer(c) \$ [2] Maria continues to invest her money at 4% per year compound interest. After 20 years she has \$328.67. (i) Calculate exactly how much more this is than \$150 invested for 20 years at 4% per year simple interest. 	
		<i>Answer(d)</i> (i) \$ [3] (ii) Calculate \$328.67 as a percentage of \$150.	
		<i>Answer(d)</i> (ii) % [2]	

2 (a)
$$\mathbf{p} = \begin{pmatrix} 3 \\ 2 \end{pmatrix}$$
 and $\mathbf{q} = \begin{pmatrix} 6 \\ 3 \end{pmatrix}$.
(i) Find, as a single column vector, $\mathbf{p} + 2\mathbf{q}$.
(ii) Calculate the value of $|\mathbf{p} + 2\mathbf{q}|$.
(iii) Calculate the value of $|\mathbf{p} + 2\mathbf{q}|$.
(b)

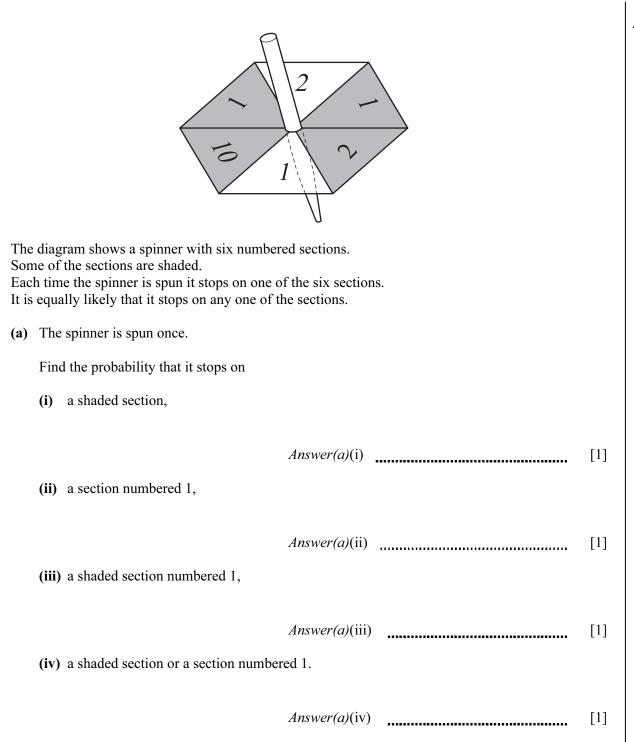
$$Mnswer(a)(ii) \dots (2)$$
(c)

$$Mnswer(a)(ii) \dots (2)$$
In the diagram, $CM = MV$ and $OL = 2LV$.
 O is the origin. $\overline{CC} = \mathbf{c}$ and $\overline{OV} = \mathbf{v}$.
Find, in terms of \mathbf{c} and \mathbf{v} , in their simplest forms
(i) \overline{CM} ,

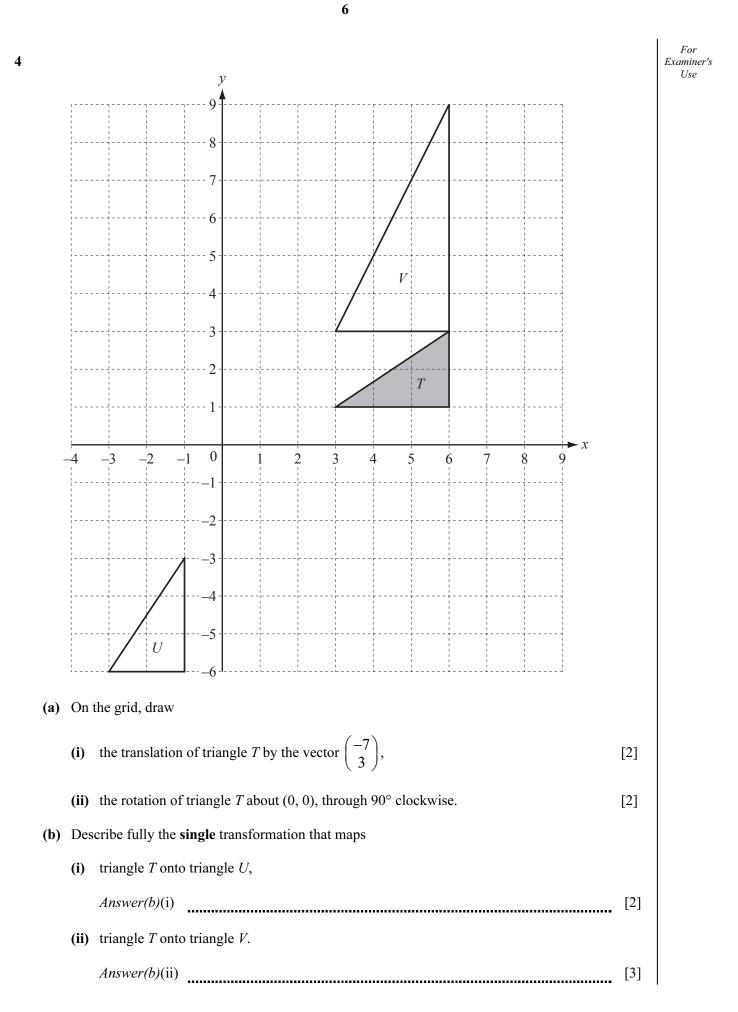
$$Mnswer(b)(i) \dots (2)$$
(ii) the position vector of M .

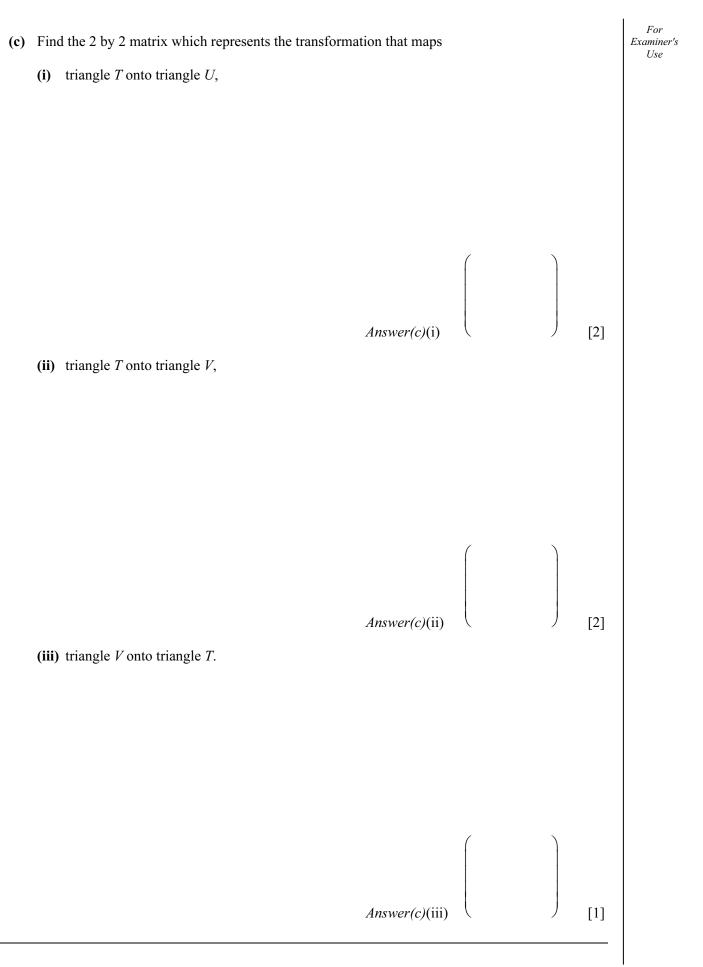
$$Mnswer(b)(ii) \dots (2)$$
(iii) \overline{ML} .

$$Mnswer(b)(iii) \dots (2)$$



(b)	The	spinner is now spun twice.	For Examiner's Use
	Finc	I the probability that the total of the two numbers is	
	(i)	20,	
	(ii)	<i>Answer(b)</i> (i) [2] 11.	
(c)	(i)	Answer(b)(ii) [2] The spinner stops on a shaded section.	
		Find the probability that this section is numbered 2.	
	(ii)	<i>Answer(c)</i> (i) [1] The spinner stops on a section numbered 2. Find the probability that this section is shaded.	
(d)	The	$Answer(c)(ii) \qquad [1]$ spinner is now spun until it stops on a section numbered 2. probability that this happens on the <i>n</i> th spin is $\frac{16}{243}$. If the value of <i>n</i> .	
		Answer(d) n = [2]	





North A A BO km 115 km H 90 km H 30° 70° R

8

The diagram shows some straight line distances between Auckland (A), Hamilton (H), Tauranga (T) and Rotorua (R).

AT = 180 km, AH = 115 km and HT = 90 km.

(a) Calculate angle *HAT*. Show that this rounds to 25.0° , correct to 3 significant figures.

Answer(a)

- 6 A spherical ball has a radius of 2.4 cm.
 - (a) Show that the volume of the ball is 57.9 cm³, correct to 3 significant figures.

[The volume V of a sphere of radius r is $V = \frac{4}{3}\pi r^3$.]

Answer(a)

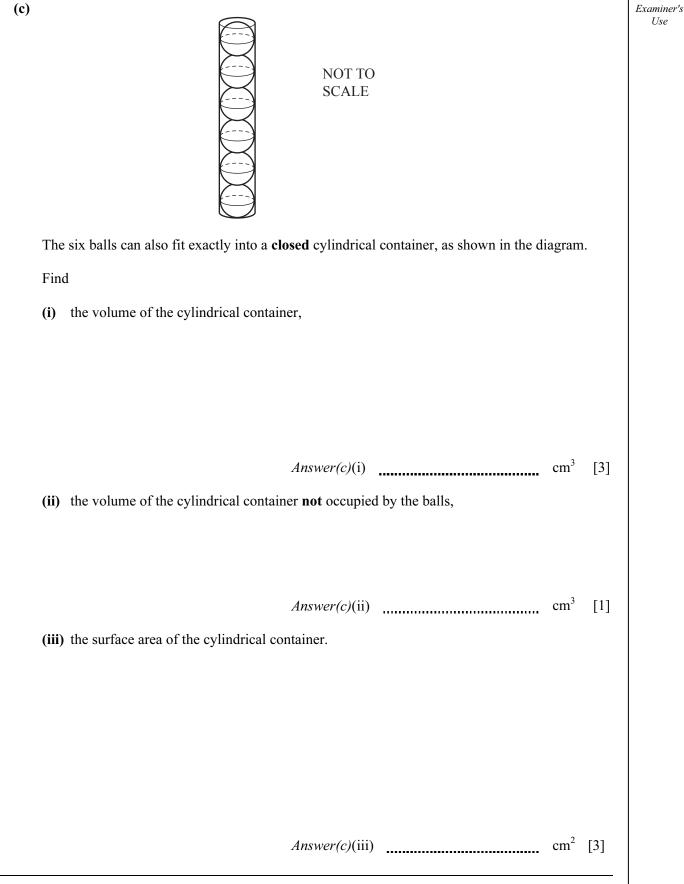
(b)

[2] NOT TO SCALE Six spherical balls of radius 2.4 cm fit exactly into a closed box. The box is a cuboid. Find (i) the length, width and height of the box, Answer(b)(i) cm, cm, cm [3] (ii) the volume of the box, Answer(b)(ii) cm^3 [1] (iii) the volume of the box not occupied by the balls, Answer(b)(iii) cm³ [1] (iv) the surface area of the box. Answer(b)(iv) cm²

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[2]



For

7 200 students were asked how many hours they exercise each week.

The table shows the results.

Time (<i>t</i> hours)	0< <i>t</i> ≤5	5< <i>t</i> ≤10	10< <i>t</i> ≤15	15< <i>t</i> ≤20	20< <i>t</i> ≤25	25< <i>t</i> ≤30	30< <i>t</i> ≤35	35< <i>t</i> ≤40
Number of students	12	15	23	30	40	35	25	20

12

(a) Calculate an estimate of the mean.

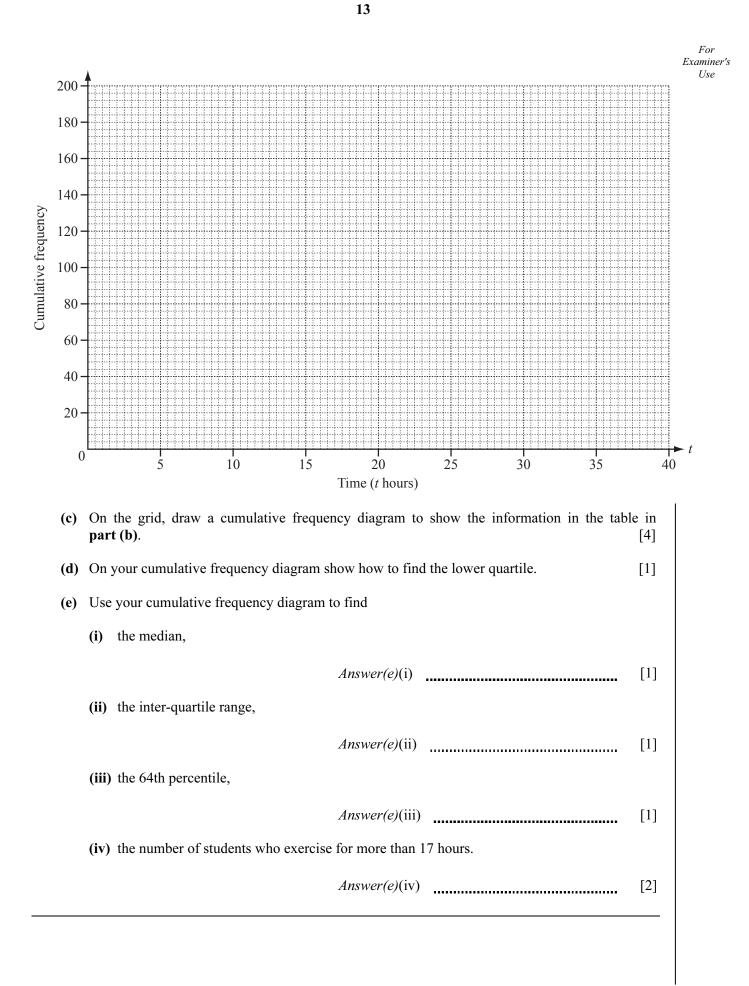
Answer(a) h [4]

[1]

(b) Use the information in the table above to complete the cumulative frequency table.

Time (<i>t</i> hours)	<i>t</i> ≤ 5	<i>t</i> ≤ 10	<i>t</i> ≤ 15	<i>t</i> ≤ 20	<i>t</i> ≤ 25	<i>t</i> ≤ 30	<i>t</i> ≤ 35	<i>t</i> ≤ 40
Cumulative frequency	12	27	50	80	120			200

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8 (a) y is 5 less than the square of the sum of p and q.Write down a formula for y in terms of p and q.

Answer(a) y =[2]

(b) The cost of a magazine is \$x and the cost of a newspaper is \$(x - 3). The total cost of 6 magazines and 9 newspapers is \$51.Write down and solve an equation in x to find the cost of a magazine.

Answer(b) \$ [4]

(c) Bus tickets cost \$3 for an adult and \$2 for a child.
There are *a* adults and *c* children on a bus.
The total number of people on the bus is 52.
The total cost of the 52 tickets is \$139.

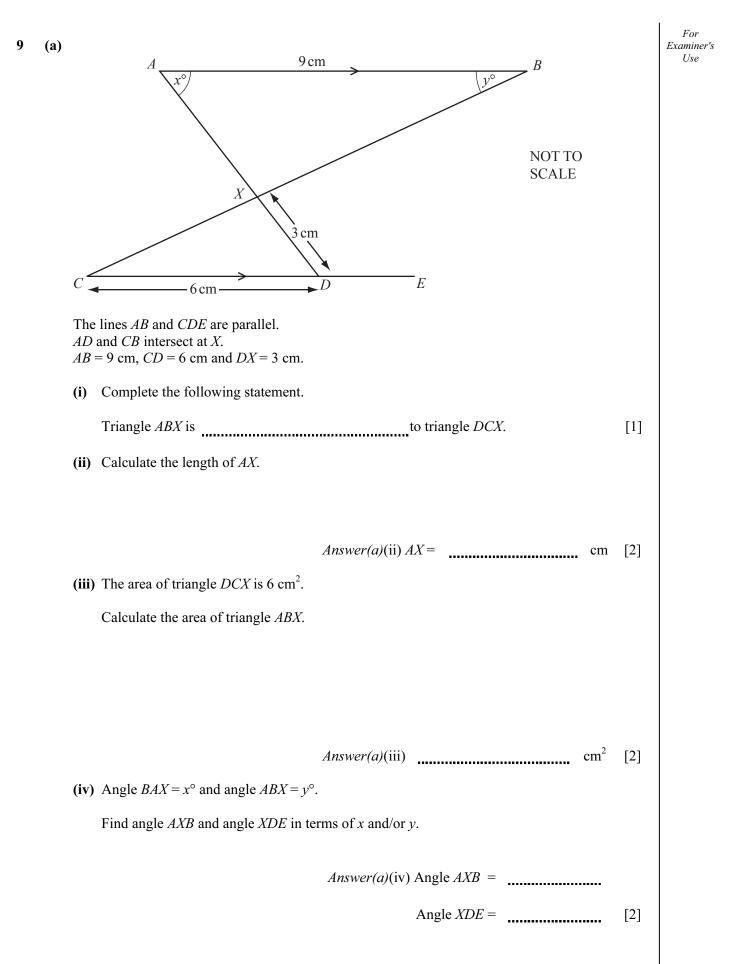
Find the number of adults and the number of children on the bus.

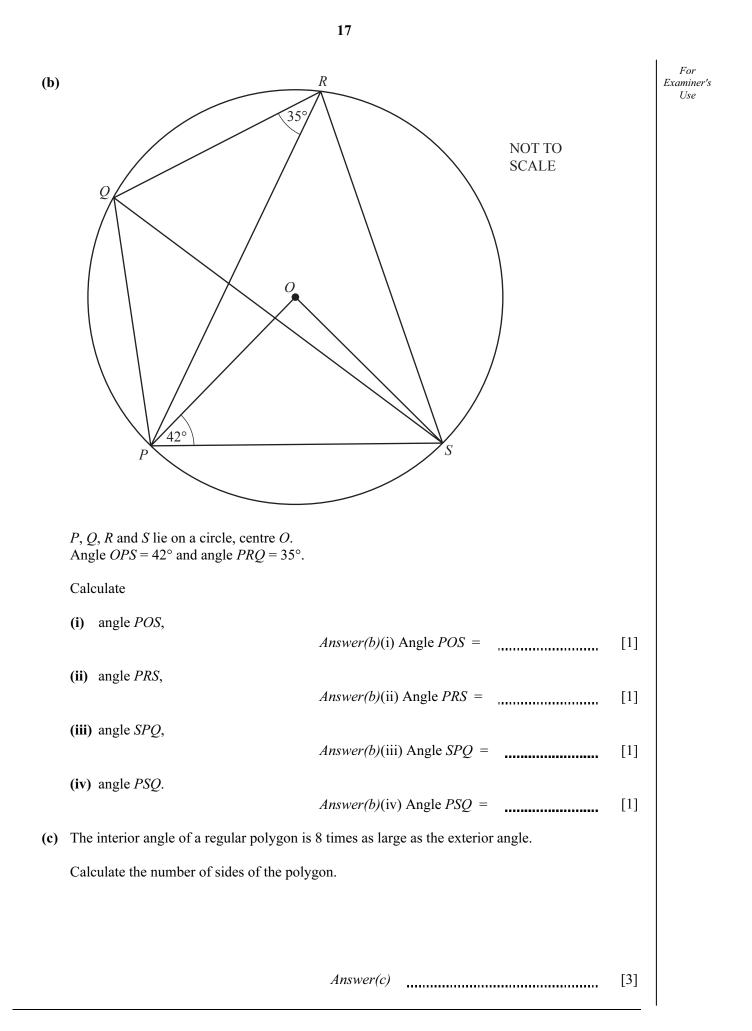
Answer(c) Number of adults =

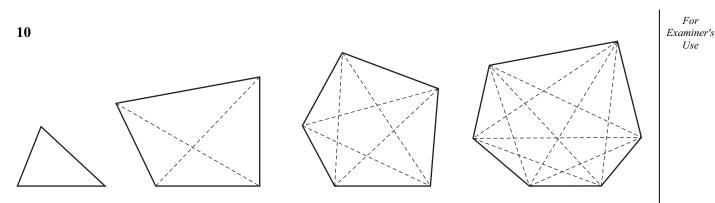
Number of children = [5]

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The diagrams show some polygons and their diagonals.

(a) Complete the table.

Number of sides	Name of polygon	Total number of diagonals		
3	triangle	0		
4	quadrilateral	2		
5		5		
6	6 hexagon			
7 heptagon		14		
8				

[3]

- (b) Write down the total number of diagonals in
 - (i) a decagon (a 10-sided polygon),

Answer(b)(i) [1]

(ii) a 12-sided polygon.

Answer(b)(ii) [1]

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(c) A polygon with *n* sides has a total of $\frac{1}{p}n(n-q)$ diagonals, where *p* and *q* are integers. (i) Find the values of p and q. Answer(c)(i) p =*q* = [3] (ii) Find the total number of diagonals in a polygon with 100 sides. Answer(c)(ii) [1] (iii) Find the number of sides of a polygon which has a total of 170 diagonals. Answer(c)(iii) [2] (d) A polygon with n + 1 sides has 30 more diagonals than a polygon with n sides. Find *n*. Answer(d) n =[1]

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