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NUMBER

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**MATHEMATICS**

**0580/22**

Paper 2 (Extended)

**May/June 2014**

**1 hour 30 minutes**

Candidates answer on the Question Paper.

Additional Materials:    Electronic calculator  
   Tracing paper (optional)

Geometrical instruments

**READ THESE INSTRUCTIONS FIRST**

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

**DO NOT WRITE IN ANY BARCODES.**

Answer **all** questions.

If working is needed for any question it must be shown below that question.

Electronic calculators should be used.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For  $\pi$ , use either your calculator value or 3.142.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [ ] at the end of each question or part question.

The total of the marks for this paper is 70.

The syllabus is approved for use in England, Wales and Northern Ireland as a Cambridge International Level 1/Level 2 Certificate.

This document consists of **12** printed pages.

1 Calculate  $\frac{\sqrt[3]{16}}{1.3^2}$ .

$$1.491030828$$

Answer .....  $1.49$  [1]

2 (a) Write 569 000 correct to 2 significant figures.

Answer(a) .....  $570\,000$  [1]

(b) Write  $569\,000$  in standard form.

Answer(b) .....  $5.69 \times 10^5$  [1]

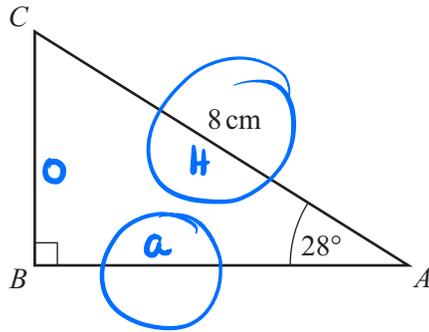
3 Solve the simultaneous equations.

$$\begin{array}{r}
 + \quad 2x - y = 7 \\
 \quad 3x + y = 3 \\
 \hline
 5x = 10 \\
 x = \frac{10}{5} = 2
 \end{array}$$

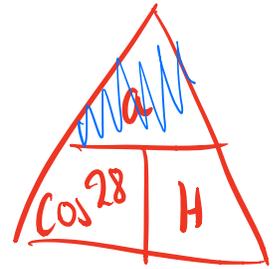
$$\begin{array}{r}
 2(2) - y = 7 \\
 4 - 7 = y
 \end{array}$$

Answer x = .....  $2$   
 y = .....  $-3$  [2]

4



NOT TO SCALE

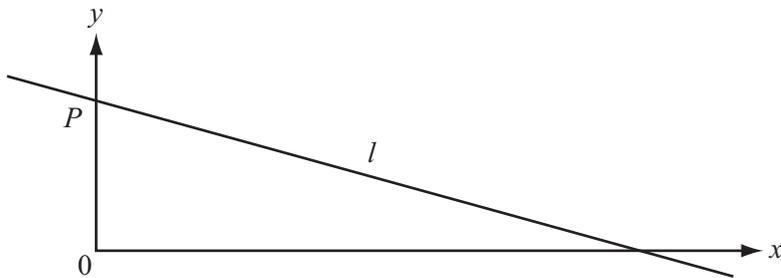


Calculate the length of  $AB$ .

$$\cos(28) \times 8 = 7.063580743$$

Answer  $AB = 7.06$  cm [2]

5



NOT TO SCALE

The equation of the line  $l$  in the diagram is  $y = 5 - x$ .

$$\rightarrow y = -x + 5$$

$$y = mx + c$$

(a) The line cuts the  $y$ -axis at  $P$ .

Write down the co-ordinates of  $P$ .

Answer(a) (0, 5) [1]

(b) Write down the gradient of the line  $l$ .

Answer(b) -1 [1]

- 6 The mass of  $1 \text{ cm}^3$  of copper is 8.5 grams, correct to 1 decimal place.  $\rightarrow \frac{0.1}{2} = 0.05$

Complete the statement about the total mass,  $T$  grams, of  $12 \text{ cm}^3$  of copper.

$$8.5 + 0.05 = 8.55$$

$$8.5 - 0.05 = 8.45$$

$$12 \times 8.55$$

$$12 \times 8.45$$

$$\text{Answer } \dots 101.4 \dots \leq T < \dots 102.6 \dots [2]$$

- 7 Write the following in order, smallest first.

$$\sqrt{0.1}$$

$$\frac{43}{201}$$

$$2\frac{1}{2}\%$$

$$0.2$$

$$\text{Answer } \dots 2\frac{1}{2}\% < 0.2 < \frac{43}{201} < \sqrt{0.1} \dots [2]$$

- 8 Without using your calculator, work out  $\frac{5}{6} - \left(\frac{1}{2} \times 1\frac{1}{2}\right)$ .

Write down all the steps of your working.

$$\frac{5}{6} - \left(\frac{1}{2} \times \frac{3}{2}\right)$$

$$\frac{5^{x2}}{6^{x2}} - \frac{3^{x3}}{4^{x3}} = \frac{10}{12} - \frac{9}{12}$$

$$\text{Answer } \dots \frac{1}{12} \dots [3]$$

- 9 At the beginning of July, Kim had a mass of 63 kg.  
At the end of July, his mass was 61 kg.

Calculate the percentage loss in Kim's mass.

$$\text{Percentage change} = \left( \frac{\text{New amount} - \text{Old amount}}{\text{Old amount}} \right) \times 100$$

$$= \left( \frac{61 - 63}{63} \right) \times 100 = -3.174603$$

3.17

Answer ..... % [3]

10  $V = \frac{1}{3}Ah$

- (a) Find  $V$  when  $A = 15$  and  $h = 7$ .

$$V = \frac{1}{3}(15)(7)$$

Answer(a)  $V = 35$  ..... [1]

- (b) Make  $h$  the subject of the formula.

$$3V = Ah$$

$$\frac{3V}{A} = h$$

Answer(b)  $h = \frac{3V}{A}$  ..... [2]

- 11 Anita buys a computer for \$391 in a sale.  
The sale price is 15% less than the original price.

Calculate the original price of the computer.

$$\text{So } 100\% - 15\% = 85\%.$$

$$85\% = 391$$

$$\frac{391}{85} \times 100$$

Answer \$ 460 ..... [3]

- 12 Solve the equation.

$$\frac{3}{2x} + \frac{1}{x+1} = 0$$

$$\frac{3(x+1) + 1(2x)}{2x(x+1)} = \frac{3x+3+2x}{2x(x+1)} = 0$$

$$5x + 3 = 0$$

$$5x = -3$$

$$x = \frac{-3}{5}$$

Answer  $x = \frac{-3}{5}$  ..... [3]

- 13  $w$  varies inversely as the square root of  $x$ .  
When  $x = 4$ ,  $w = 4$ .

Find  $w$  when  $x = 25$ .

$$w = \frac{K}{\sqrt{x}}$$

So  $x=4$   $w=4$

$$4 = \frac{K}{\sqrt{4}}$$

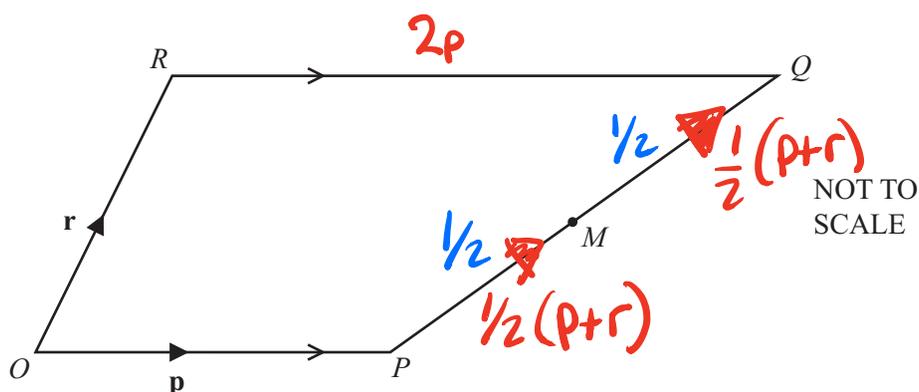
$$2 \times 4 = K = 8$$

hence

$$w = \frac{8}{\sqrt{25}} = \frac{8}{5}$$

Answer  $w = \frac{8}{5} = 1.6$  [3]

14



$OPQR$  is a trapezium with  $RQ$  parallel to  $OP$  and  $RQ = 2OP$ .

$O$  is the origin,  $\vec{OP} = \mathbf{p}$  and  $\vec{OR} = \mathbf{r}$ .

$M$  is the midpoint of  $PQ$ .

Find, in terms of  $\mathbf{p}$  and  $\mathbf{r}$ , in its simplest form

- (a)  $\vec{PQ}$ ,

$$-\mathbf{p} + \mathbf{r} + 2\mathbf{p}$$

Answer(a)  $\vec{PQ} = \mathbf{p} + \mathbf{r}$  [1]

- (b)  $\vec{OM}$ , the position vector of  $M$ .

$$\mathbf{p} + \frac{1}{2}(\mathbf{p} + \mathbf{r}) = \frac{3}{2}\mathbf{p} + \frac{1}{2}\mathbf{r} = \frac{1}{2}(3\mathbf{p} + \mathbf{r})$$

Answer(b)  $\vec{OM} = \frac{1}{2}(3\mathbf{p} + \mathbf{r})$  [2]

15  $M = \begin{pmatrix} 4 & 2 \\ 3 & 5 \end{pmatrix}$

Find

(a)  $M^2$ ,

$$\begin{pmatrix} 4 & 2 \\ 3 & 5 \end{pmatrix} \begin{pmatrix} 4 & 2 \\ 3 & 5 \end{pmatrix} = \begin{pmatrix} (4 \times 4) + (2 \times 3) & (4 \times 2) + (2 \times 5) \\ (3 \times 4) + (5 \times 3) & (3 \times 2) + (5 \times 5) \end{pmatrix}$$

Answer(a)  $\begin{pmatrix} 22 & 18 \\ 27 & 31 \end{pmatrix}$  [2]

(b) the determinant of  $M$ .

$$\det(M) = 4 \times 5 - 3 \times 2$$

Answer(b) ..... 14 ..... [1]

16 Factorise completely.

(a)  $4p^2q - 6pq^2$

$$2pq(2p - 3q)$$

Answer(a) .....  $2pq(2p - 3q)$  ..... [2]

(b)  $u + 4t + ux + 4tx$

$$1(u + 4t) + x(u + 4t)$$

Answer(b) .....  $(u + 4t)(1 + x)$  ..... [2]

17 (a) Simplify  $(3125t^{125})^{\frac{1}{5}}$ .

$$(3125)^{\frac{1}{5}} (t^{125})^{\frac{1}{5}}$$

$$\text{Answer(a)} \dots\dots\dots 5t^{25} \dots\dots\dots [2]$$

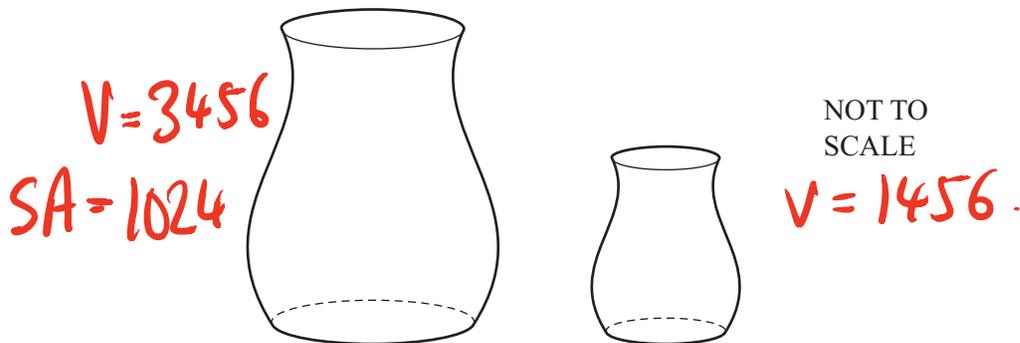
(b) Find the value of  $p$  when  $3^p = \frac{1}{9}$ .

$$\text{Answer(b)} p = \dots\dots\dots -2 \dots\dots\dots [1]$$

(c) Find the value of  $w$  when  $x^{72} \div x^w = x^8$ .

$$\text{Answer(c)} w = \dots\dots\dots 64 \dots\dots\dots [1]$$

18



The two containers are mathematically similar in shape.  
 The larger container has a volume of  $3456 \text{ cm}^3$  and a surface area of  $1024 \text{ cm}^2$ .  
 The smaller container has a volume of  $1458 \text{ cm}^3$ .

Calculate the surface area of the smaller container.

$$\text{Volume Scale Factor} = \frac{3456}{1456} = \frac{216}{92}$$

$$\text{Scale Factor} = \sqrt[3]{\text{Volume Scale factor}} = \sqrt[3]{\frac{216}{92}}$$

$$\text{Area SF} = (\text{SF})^2 = 1.333943555$$

So

$$\frac{1024}{(1.333943555)^2} \dots\dots\dots \text{Answer} \dots\dots\dots 576 \dots\dots\dots \text{cm}^2 [4]$$

19 Simplify.

$$\frac{x^2 + 6x - 7}{3x + 21}$$

$$x^2 + 6x - 7 \quad \left\{ \begin{array}{l} \text{Product} = -7 \\ \text{Sum} = 6 \end{array} \right\} \quad 7 \text{ and } -1$$

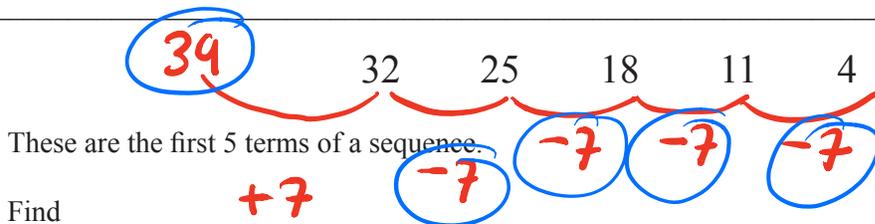
$$\frac{(\cancel{x+7})(x-1)}{3(\cancel{x+7})}$$

$$3(x-1)$$

$$\frac{x-1}{3}$$

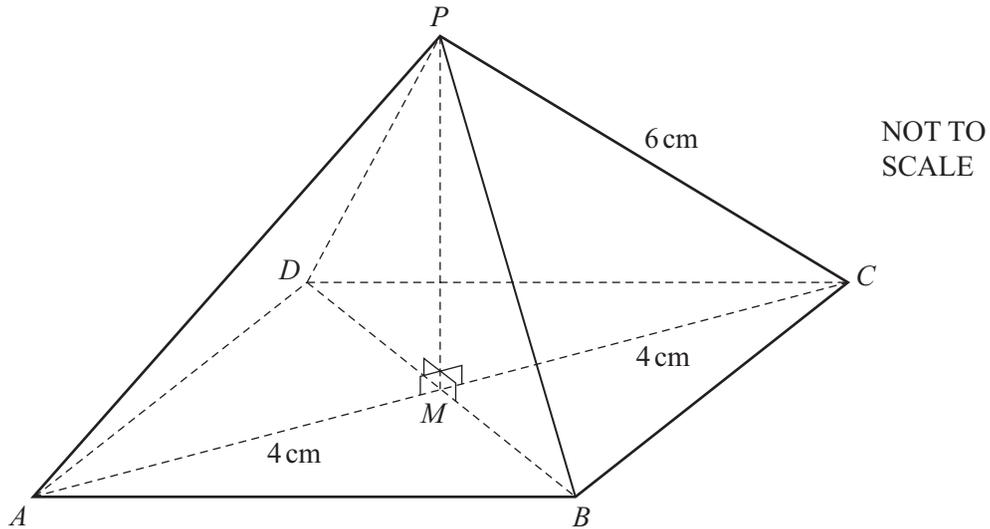
Answer ..... [4]

20

Answer(a) .....  $-3$  [1]Answer(b) .....  $39 - 7n$  [2]Answer(c) .....  $53$  [2]

$$39 + 332 = 7n$$

$$\frac{371}{7} = n = 53$$



The diagram shows a pyramid on a square base  $ABCD$  with diagonals,  $AC$  and  $BD$ , of length 8 cm.  $AC$  and  $BD$  meet at  $M$  and the vertex,  $P$ , of the pyramid is vertically above  $M$ . The sloping edges of the pyramid are of length 6 cm.

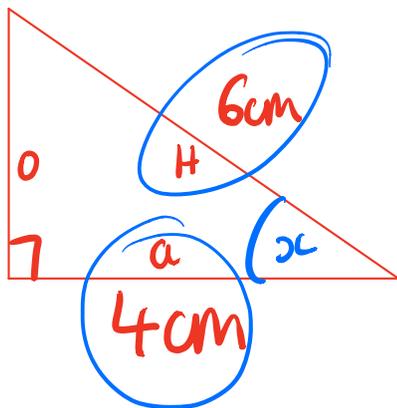
Calculate

- (a) the perpendicular height,  $PM$ , of the pyramid,

$$\sqrt{6^2 - 4^2} = 2\sqrt{5}$$

Answer(a)  $PM = 4.47$  ..... cm [3]

- (b) the angle between a sloping edge and the base of the pyramid.

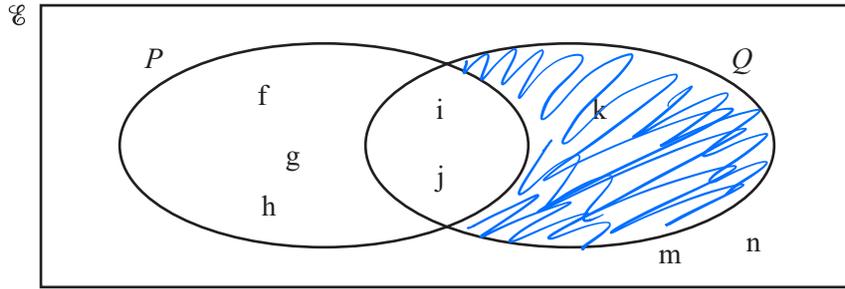


$$\cos \alpha = \frac{4}{6}$$

$$\alpha = \cos^{-1}\left(\frac{4}{6}\right)$$

Answer(b)  $48.2$  ..... [3]

Question 22 is printed on the next page.



(a) Use the information in the Venn diagram to complete the following.

(i)  $P \cap Q = \{ \dots i, j \dots \}$  [1]

(ii)  $P \cup Q = \{ \dots k, m, n, i, j \dots \}$  [1]

(iii)  $n(P \cup Q)' = \dots 2 \dots$  [1]

(b) A letter is chosen at random from the set Q.

Find the probability that it is also in the set P.

Answer(b)  $\dots \frac{2}{3} \dots$  [1]

(c) On the Venn diagram shade the region  $P' \cap Q$ . [1]

(d) Use a set notation symbol to complete the statement.

$\{f, g, h\} \subseteq P$  [1]

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