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0580/21

October/November 2014

**1 hour 30 minutes**

Candidates answer on the Question Paper.

Additional Materials:      Electronic calculator  
Tracing paper (optional)

## Geometrical instruments

**READ THESE INSTRUCTIONS FIRST**

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use an HB pencil for any diagrams or graphs.

Do not use staples, paper clips, glue or correction fluid.

DO **NOT** WRITE IN ANY BARCODES.

Answer **all** questions.

If working is needed for any question it must be shown below that question.

Electronic calculators should be used.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For  $\pi$ , use either your calculator value or 3.142.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [ ] at the end of each question or part question.

The total of the marks for this paper is 70.

The syllabus is approved for use in England, Wales and Northern Ireland as a Cambridge International Level 1/Level 2 Certificate.

This document consists of **12** printed pages.

- 1 Use your calculator to find the value of  $1.35^7$ .

Give your answer correct to 5 significant figures.

$$(1.35)^7 = 8.17215094$$

Answer 8.1722 [2]

- 2 Write the following in order of size, smallest first.

$\pi$       3.14       $\frac{22}{7}$       3.142      3

Answer 3 < 3.14 <  $\pi$  < 3.142 <  $\frac{22}{7}$  [2]  
smallest

3

ZEBRA

Write down the letters in the word above that have

- (a) exactly one line of symmetry,

Answer(a) E B A [1]

- (b) rotational symmetry of order 2.

Answer(b) Z [1]

- 4 Cheryl recorded the midday temperatures in Seoul for one week in January.

| Day              | Mon | Tue | Wed | Thu | Fri | Sat | Sun |
|------------------|-----|-----|-----|-----|-----|-----|-----|
| Temperature (°C) | -4  | -5  | -3  | -11 | -8  | -3  | -1  |

- (a) Write down the mode.

Answer(a)  $-3$  °C [1]

- (b) On how many days was the temperature lower than the mode?

Answer(b)  $4 \text{ days}$  [1]

- 5 Without using a calculator, work out  $\frac{1}{4} + \frac{1}{6}$ .

Write down all the steps in your working and give your answer as a fraction in its simplest form.

$$\frac{3}{12} + \frac{2}{12} = \frac{5}{12}$$

Answer  $\frac{5}{12}$  [2]

- 6 Write 15.0782 correct to

- (a) one decimal place,

Answer(a)  $15.1$  [1]

- (b) the nearest 10.

Answer(b)  $20$  [1]

- 7 The population of Dubai at the end of 2012 was 2.1 million.  
This was predicted to increase at a rate of 6% each year.

Calculate the predicted population of Dubai at the end of 2015.

$$100\% + 6\% = 106$$

$$2.1 \times (1.06)^3 = 2.5011336$$

Answer ..... 2.50 million [3]

- 8 On a ship, the price of a gift is 24 euros (€) or \$30.

What is the difference in the price on a day when the exchange rate is €1 = \$1.2378?  
Give your answer in dollars, correct to the nearest cent.

$$24 \times 1.2378 = 29.7072$$

$$30 - 29.7072 = 0.2928$$

Answer \$ ..... 0.29 [3]

- 9 (a) Write  $2.8 \times 10^2$  as an ordinary number.

2.800

Answer(a) ..... 280 [1]

- (b) Work out  $2.5 \times 10^8 \times 2 \times 10^{-2}$ .  
Give your answer in standard form.

$$2.5 \times 2 = 5$$

$$10^8 \times 10^{-2} = \frac{10^8}{10^2} = 10^6$$

Answer(b) .....  $5 \times 10^6$  [2]

- 10 Solve the equation.

$$\frac{x+5}{x} = \frac{7}{3}$$

$$3(x+5) = 7x$$

$$3x + 15 = 7x$$

$$15 = 7x - 3x$$

$$15 = 4x$$

$$\frac{15}{4} = x$$

Answer x = .....  $\frac{15}{4} = 3.75$  [3]

11 (a) Simplify  $x^8 \div x^2$ .

Answer(a) .....  $x^6$  [1]

(b) Simplify  $\left(\frac{x^6}{27}\right)^{\frac{1}{3}}$ .

Answer(b) .....  $\frac{x^2}{3}$  [2]

12 Solve the simultaneous equations.

$$\begin{aligned} (0.4x - 5y = 27) \times 5 \\ 2x + 0.2y = 9 \end{aligned}$$

$$\begin{array}{r} 2x - 25y = 135 \\ -2x + 0.2y = 9 \\ \hline -25.2y = 126 \\ y = \frac{126}{-25.2} = -5 \end{array}$$

$$\begin{aligned} 2x + 0.2(-5) &= 9 \\ 2x - 1 &= 9 \\ 2x &= 10 \\ x &= 5 \end{aligned}$$

Answer x = ..... 5  
y = ..... -5 [3]

13  $y$  varies directly with  $\sqrt{x+5}$ .  
 $y = 4$  when  $x = -1$ .

Find  $y$  when  $x = 11$ .

$$\begin{aligned} y &= k\sqrt{x+5} \\ \text{Let } x = -1 \text{ and } y &= 4 \\ 4 &= k\sqrt{-1+5} \\ 4 &= k\sqrt{4} \\ \frac{4}{\sqrt{4}} &= k = \frac{4}{\pm 2} = \pm 2 \end{aligned}$$

$$\begin{aligned} y &= \pm 2\sqrt{x+5} \\ \text{Let } x &= 11 \\ y &= \pm 2\sqrt{11+5} \rightarrow \pm 2\sqrt{16} \\ y &= \pm 2 \times \pm 4 = \pm 8 \end{aligned}$$

Answer y = .....  $\pm 8$  [3]

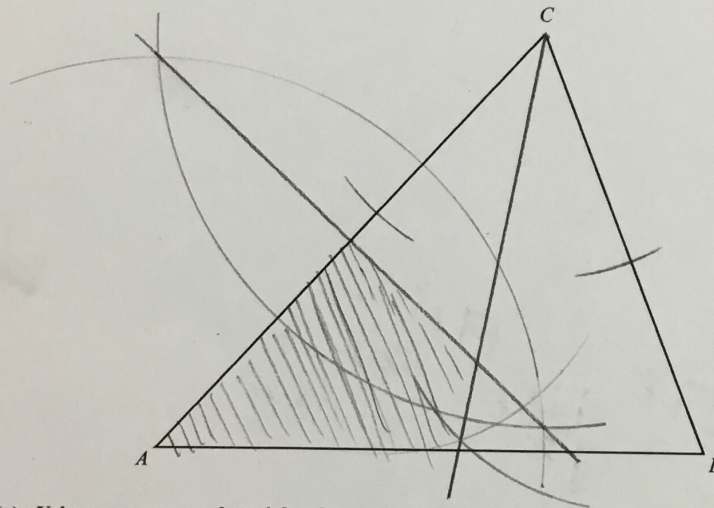
14  $A = \begin{pmatrix} 2 & 8 \\ 1 & 4 \end{pmatrix}$

Work out  $A^2 - 4A$ .

$$A^2 - 4A = \begin{pmatrix} 12 & 48 \\ 6 & 24 \end{pmatrix} - 4 \begin{pmatrix} 2 & 8 \\ 1 & 4 \end{pmatrix} = \begin{pmatrix} 12 & 48 \\ 6 & 24 \end{pmatrix} - \begin{pmatrix} 8 & 32 \\ 4 & 16 \end{pmatrix}$$

Answer  $\begin{pmatrix} 4 & 16 \\ 2 & 8 \end{pmatrix}$  [3]

15



(a) Using compasses and straight edge only, construct

(i) the perpendicular bisector of  $AC$ ,

[2]

(ii) the bisector of angle  $ACB$ .

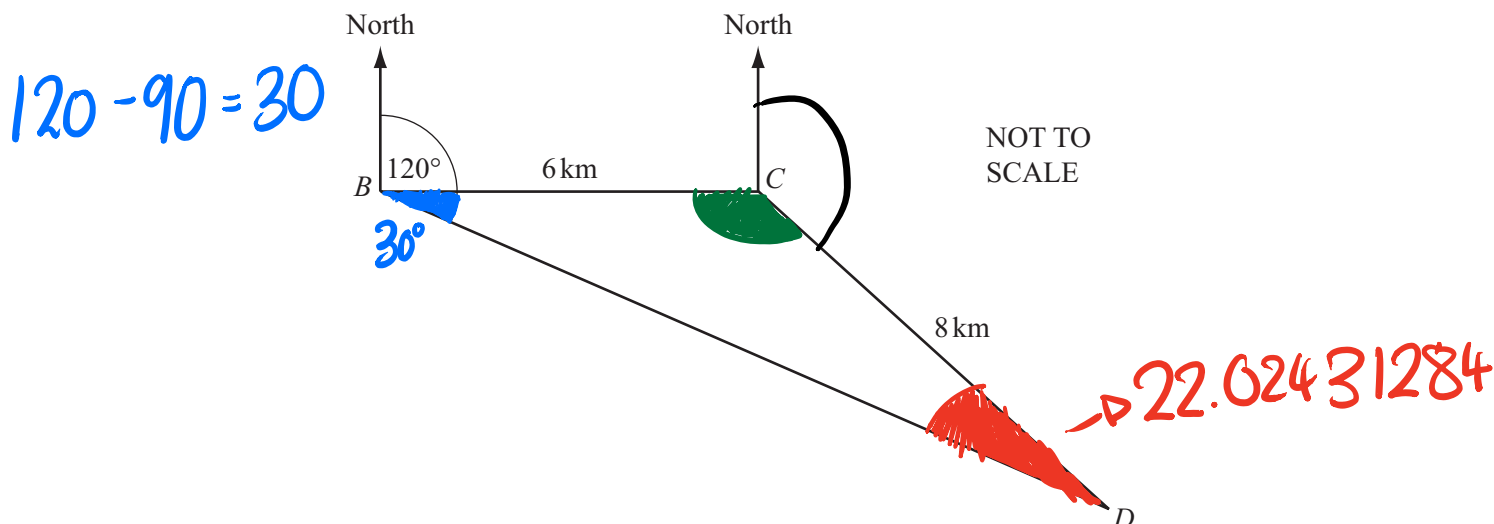
[2]

(b) Shade the region inside the triangle which is

- nearer to  $A$  than to  $C$
- and
- nearer to  $AC$  than to  $BC$ .

[1]

- 16 A helicopter flies from its base  $B$  to deliver supplies to two oil rigs at  $C$  and  $D$ .  
 $C$  is 6 km due east of  $B$  and the distance from  $C$  to  $D$  is 8 km.  
 $D$  is on a bearing of  $120^\circ$  from  $B$ .



Find the bearing of  $D$  from  $C$ .

$$\frac{\sin 30}{8} = \frac{\sin x}{6}$$

$$\frac{6 \sin(30)}{8} = \sin x$$

$$x = 22.02431284$$

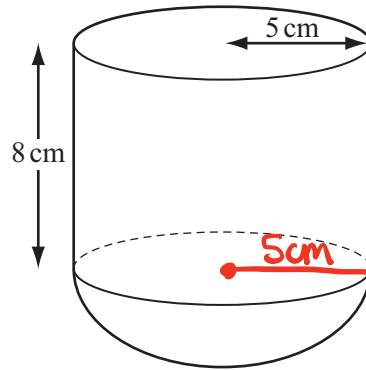
$$180 - 30 - 22.02431284 = 127.9756872$$

$$360 - 127.9756872 - 90 = 142.0243128$$

Answer  $142^\circ$  [5]



17 The diagram shows a child's toy.



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The shape of the toy is a cylinder of radius 5 cm and height 8 cm on top of a hemisphere of radius 5 cm.

Calculate the volume of the toy.

[The volume,  $V$ , of a sphere with radius  $r$  is  $V = \frac{4}{3}\pi r^3$ .]

$$\text{Volume of cylinder} \\ \pi(5)^2 \times 8 = 200\pi$$

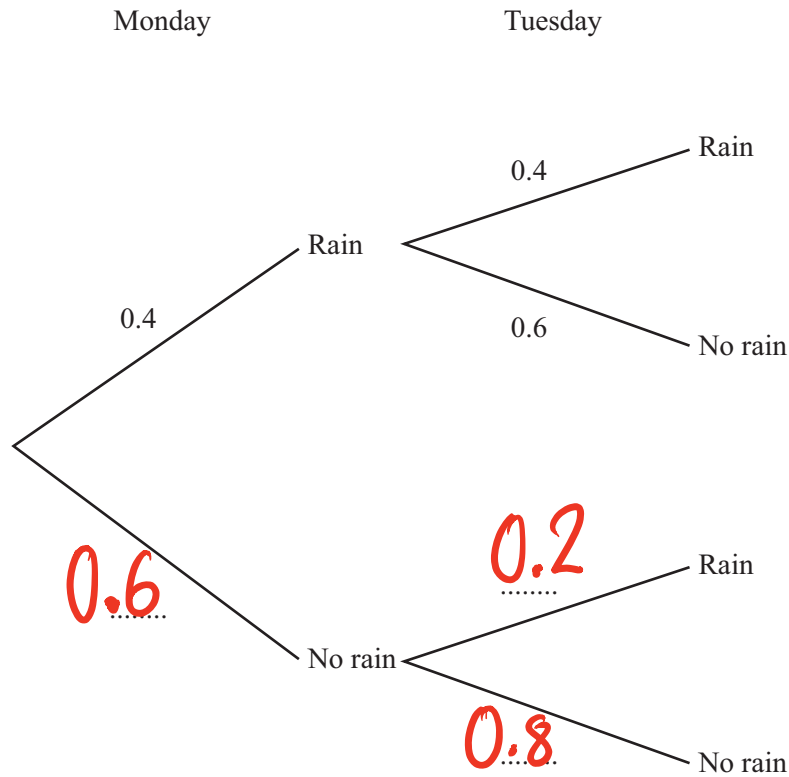
$$\text{Volume of hemisphere} \\ \frac{1}{2} \times \frac{4}{3} \times \pi \times (5)^3 \\ = \frac{250\pi}{3}$$

$$200\pi + \frac{250\pi}{3} = 890.1179185$$

Answer ..... **890** .....  $\text{cm}^3$  [5]

- 18 If it rains today the probability that it will rain tomorrow is 0.4 .  
 If it does not rain today the probability that it will rain tomorrow is 0.2 .  
 On Sunday it rained.

(a) Complete the tree diagram for Monday and Tuesday.



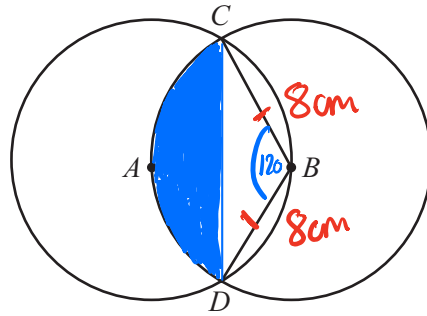
[2]

(b) Find the probability that it rains on at least one of the two days shown in the tree diagram.

$$\begin{aligned}
 (R, R) &= 0.4 \times 0.4 = 0.16 \\
 (NR, R) &= 0.6 \times 0.2 = 0.12 \\
 (R, NR) &= 0.4 \times 0.6 = 0.24
 \end{aligned}
 \left. \vphantom{\begin{aligned} (R, R) \\ (NR, R) \\ (R, NR) \end{aligned}} \right\} \text{Sum to} = 0.52$$

Answer(b) 0.52 [3]

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Two circles, centres  $A$  and  $B$ , are each of radius 8 cm and intersect at  $C$  and  $D$ . Each circle passes through the centre of the other circle.

- (a) Explain why angle  $CBD$  is  $120^\circ$ .

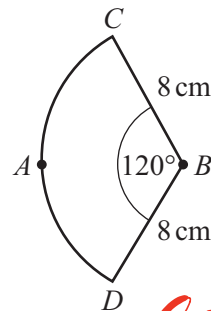
Answer(a)

Triangles  $CBA$  and  $BDA$  are equilateral triangles

[1]

- (b) For the circle, centre  $B$ , find the area of the sector  $BCD$ .

$$\frac{120}{360} \times \pi \times (8)^2 = \frac{64\pi}{3}$$

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Answer(b) ..... 67 .....  $\text{cm}^2$  [2]

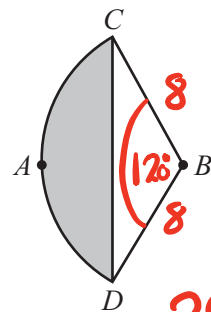
- (c) (i) Find the area of the shaded segment  $CAD$ .

$$\begin{aligned} \text{Area of triangle} &= \frac{1}{2} \times a \times b \times \sin C \\ 27.71281292 &= \frac{1}{2} \times 8 \times 8 \times \sin(120) \end{aligned}$$

$$\text{Area of Sector} - \text{Area of Triangle} = 67 - 27.71281292$$

- (ii) Find the area of overlap of the two circles.

$$2 \times 39.3$$

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Answer(c)(i) ..... 39.3 .....  $\text{cm}^2$  [3]

Answer(c)(ii) ..... 78.6 .....  $\text{cm}^2$  [1]

Question 20 is printed on the next page.

20

$$f(x) = 3x - 2$$

$$g(x) = \frac{2}{x+1}, \quad x \neq -1$$

(a) Find  $gf(2)$ .

$$f(2) = 3(2) - 2 = 6 - 2 = 4$$

$$g(4) = \frac{2}{4+1} = \frac{2}{5}$$

Answer(a) .....  $\frac{2}{5}$  ..... [2](b) Solve  $g(x) = 10$ .

$$\frac{2}{x+1} = 10$$

$$2 = 10(x+1)$$

$$2 = 10x + 10$$

$$2 - 10 = 10x$$

$$-8 = 10x$$

$$\frac{-8}{10} = x = -\frac{4}{5}$$

Answer(b)  $x =$  .....  $-\frac{4}{5}$  ..... [2]

(c) Simplify.

$$f(2x) - f(x+2)$$

$$f(2x) - f(x+2) = 3(2x) - 2 - (3(x+2) - 2)$$

$$6x - 2 - (3x + 6 - 2)$$

$$6x - 2 - 3x - 4$$

$$3x - 6 = 3(x-2)$$

Answer(c) .....  $3(x-2)$  ..... [3]

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