



MATHEMATICS

0580/41

Paper 4 (Extended)

May/June 2017

MARK SCHEME

Maximum Mark: 130

Published

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Abbreviations

cao	correct answer only
dep	dependent
FT	follow through after error
isw	ignore subsequent working
oe	or equivalent
SC	Special Case
nfww	not from wrong working
soi	seen or implied

Question	Answer	Marks	Part marks
1(a)(i)	275.31	2	M1 for $90 \times 23.15 + 1885 \times 13.5$ oe
1(a)(ii)	3202	3	M2 for $\frac{198.16 - 90 \times 0.245}{0.055}$ oe M1 for 90×0.245 or 90×24.5 oe
1(b)	17.[0] or 17.00 to 17.01	2	M1 for $13.5 \times \left(1 + \frac{8}{100}\right)^3$
1(c)(i)	40	3	M2 for $\frac{7.7 - 5.5}{5.5} [\times 100]$ oe or $\frac{7.7}{5.5} \times 100$ or M1 for $\frac{7.7}{5.5}$ oe
1(c)(ii)	11.9 or 11.86 to 11.87	3	M2 for $\sqrt[3]{\frac{7.7}{5.5}}$ oe or M1 for $5.5 \times x^3 = 7.7$ oe
1(d)	150 [million] oe	2	M1 for 390 [million] $\div (5 + 2 + 6)$
1(e)	250 nfww	3	M2 for $258.25 \div ((100 + 3.3) \div 100)$ or M1 for 258.25 associated with 103.3[%]
2(a)	$71 < t \leq 72$	1	
2(b)	72.3 or 72.27 to 72.28 nfww	4	M1 for midpoints soi (condone 1 error or omission) M1 for use of $\sum fx$ with x in correct interval including both boundaries M1 (dep on 2nd M1) for $\sum fx \div 90$
2(c)(i)	41, 62, 80, 90	2	B1 for 2 correct values

Question	Answer	Marks	Part marks
2(c)(ii)	Correct curve	3	B1FT <i>their</i> (c)(i) for 5 correct heights B1 for 5 points plotted at upper ends of intervals B1FT (dep on at least B1) for increasing curve or increasing polygon through 5 points If zero scored, SC1FT for 4 correct points plotted
2(c)(iii)	72.1 to 72.4	1	
2(c)(iv)	1.9 to 2.2	2	M1 for UQ = 73.2 to 73.4 or LQ = 71.2 to 71.3
2(d)	180 cao nfw	4	B3 for 50 [m/s] nfw OR M3 for $\frac{3725 \div 1000}{74.5 \div 3600}$ OR M2 for $3725 \div 74.5$ or M1 for 3725 or 74.5 seen or for $(3715 \text{ to } 3725) \div (74.5 \text{ to } 75.5)$ M1 indep for multiply by 3.6 oe
3(a)(i)	Image at (5, 1), (7, 1), (7, 4)	2	B1 reflection in $y = 4$ or $x = k$
3(a)(ii)	Image at (-1, 1), (-4, 1), (-1, 3)	2	B1 correct size and correct orientation wrong position or for rotation 90° clockwise around (0, 0)
3(a)(iii)	Image at (2, -4), (4, -4), (2, -1)	2	B1 for translation by $\begin{pmatrix} 1 \\ k \end{pmatrix}$ or $\begin{pmatrix} k \\ -5 \end{pmatrix}$
3(b)	Enlargement	1	
	[sf] – 0.5 oe	1	
	(5, 5)	1	
3(c)	$\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$	2	B1 for one correct column or row
3(d)(i)	(4, 2)	2	M1 for $\begin{pmatrix} 1 & 0 \\ 0 & 2 \end{pmatrix} \begin{pmatrix} 4 \\ 1 \end{pmatrix}$ oe

Question	Answer	Marks	Part marks
3(d)(ii)	$(-4, 2)$	3	M2 for $\begin{pmatrix} -1 & 0 \\ 0 & 2 \end{pmatrix}$ or $\begin{pmatrix} 1 & 0 \\ 0 & 2 \end{pmatrix} \begin{pmatrix} -4 \\ 1 \end{pmatrix}$ or M1 for $\begin{pmatrix} 1 & 0 \\ 0 & 2 \end{pmatrix} \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix} \begin{bmatrix} 4 \\ 1 \end{bmatrix}$ or $\begin{pmatrix} -4 \\ 1 \end{pmatrix}$
3(d)(iii)	$\frac{1}{2} \begin{pmatrix} 2 & 0 \\ 0 & 1 \end{pmatrix}$ oe isw	3	M2 for $\det = 2$ soi or $k \begin{pmatrix} 2 & 0 \\ 0 & 1 \end{pmatrix}$ soi or M1 for recognition that Q is inverse matrix of G or GQ = I or QG = I
4(a)	-1.6 to -1.4	1	
4(b)	-0.5	1	
4(c)	$k > -4$	2	B1 for identifying the -4 or for horizontal line drawn $y = -4$
4(d)	$y = x - 5$ ruled and -2.3 to -2.1 -1.2 to -1.1 1.3 to 1.4	3	B2 for correct line and 2 correct values or no line and 3 correct values or B1 for no line and 2 correct values or B1 for correct line
4(e)	Tangent ruled at $x = 1$	B1	No daylight at point of contact. Consider point of contact as midpoint between two vertices of daylight, the midpoint must be between $x = 0.8$ and 1.2
	-6 to -4	2	Dep on B1 or close attempt at tangent at $x = 1$ M1 for rise/run for <i>their</i> tangent at $x = 1$
5(a)(i)	50890 or 50893 to 50900.4	2	M1 for $\pi \times 18^2 \times 50$

Question	Answer	Marks	Part marks
5(a)(ii)	20.5 or 20.52 to 20.534	3	<p>B2 for answer 29.5 or 29.46 to 29.48 OR M2 for $(50900 - 30000) \div (\pi \times 18^2)$ oe</p> <p>or M1 for $(\text{figs } 50.9 - \text{figs } 30) \div (\pi \times \text{figs } 18^2)$ or M1 for $(50900 - 30000) = (\pi \times 18^2)h$ oe</p> <p>OR <u>alternative method</u> M2 for $50 - \frac{30000}{\pi \times 18^2}$ oe</p> <p>M1 for $\text{figs } 30 = \pi \times \text{figs } 18^2 \times (50 - h)$ oe or for $\frac{\text{figs } 30}{\pi \times \text{figs } 18^2}$ oe</p> <p>OR <u>alternative method</u> M2 for $\frac{(50.9 - 30)}{50.9} \times 50$ oe or M1 for $\frac{(50.9 - 30)}{50.9}$ or $\frac{30}{50.9} \times 50$ oe or M1 for $\frac{(\text{figs } 50.9 - \text{figs } 30)}{\text{figs } 50.9} \times 50$ oe</p>
5(a)(iii)	334 nfw	4	<p>M2 for $\text{figs } 30 \div \frac{2}{3}\pi \times 3.5^3$ oe or M1 for $\frac{1}{2} \times \frac{4}{3}\pi \times 3.5^3$ oe</p> <p>and B1 for 30 000</p>
5(b)(i)	3.28[6..] or 3.29	3	<p>M2 for $[r^2 =] \frac{95 \times 3}{8.4\pi}$ oe or M1 for $\frac{1}{3}\pi \times r^2 \times 8.4 [= 95]$</p>
5(b)(ii)	93.1 to 93.6	4	<p>M3 for $\pi \times 3.3 \times \sqrt{3.3^2 + 8.4^2}$ or M2 for $\sqrt{3.3^2 + 8.4^2}$ or M1 for $3.3^2 + 8.4^2$</p>
6(a)(i)	$-7x + 55$ final answer	2	<p>M1 for $8x + 20$ or $-15x + 35$ or answer $-7x + k$ or $kx + 55$</p>
6(a)(ii)	$x^2 - 14x + 49$ final answer	2	<p>M1 for 3 of $x^2 - 7x - 7x + 49$</p>

Question	Answer	Marks	Part marks
6(b)(i)	-18	3	M1 for a correct first step ie correctly multiplying by 3 or correctly dividing by 2 or for correctly subtracting 5 M1 for correctly reaching $ax = b$ from <i>their</i> first step
6(b)(ii)	15	3	M2 for $6x - 4x = 21 + 9$ oe or M1 for $6x - 21$ or correct division by 3 or for correctly reaching $ax = b$ from <i>their</i> first step
6(b)(iii)	5 and -5	3	B2 for 5 or -5 or M1 for $[x^2 =] (74 + 1) \div 3$ or better
7(a)	(-0.5, 3)	2	B1 for one correct value
7(b)	$[y =] -2x + 2$ final answer	3	M1 for $\frac{-2-8}{2-3}$ or better M1 for substitution of (-3, 8) or (2, -2) or <i>their</i> midpoint into $y = mx + c$ with <i>their</i> m
7(c)	$y = -2x + 7$ oe	2FT	FT <i>their</i> (b) M1 for $y = (\text{their}-2)x + k$ ($k \neq 2$) or $y = kx + 7$ ($k \neq 0$) If zero scored, SC1 for $(\text{their} - 2)x + 7$
7(d)	$x - 2y + 9 = 0$ or $2y - x - 9 = 0$ oe	4	B3 for any correct equivalent in wrong form Or M2 for $y = \frac{1}{2}x + k$ oe (FT negative reciprocal of <i>their</i> gradient in (b)) or M1 for $\text{grad} = \frac{1}{2}$ (FT negative reciprocal of <i>their</i> gradient in (b)) M1 for substitution of (1, 5) into $y = mx + c$ oe with <i>their</i> m
8(a)(i)	290	2	M1 for $180 + 110$ oe
8(a)(ii)	156.8 or 156.7[9..]	5	B1FT for $CBA = 10^\circ$ (<i>their</i> (a) - 280) and B3 for [angle $ACB =]13.2^\circ$ or M2 for $[\sin C] = \frac{50 \sin(\text{their}10)}{38}$ or M1 for $\frac{50}{\sin C} = \frac{38}{\sin(\text{their}10)}$ oe

Question	Answer	Marks	Part marks
8(a)(iii)	8.68 or 8.677 to 8.684	3	M2 for $[x =]50\sin(\text{their}10)$ oe or M1 for $\sin(\text{their}10) = \frac{x}{50}$ oe or M1 for a correct right-angled triangle drawn with 50 as hypotenuse
8(b)(i)	$x(x - 25) = 2200$	1	and no errors seen
8(b)(ii)	$\frac{-(-25) \pm \sqrt{(-25)^2 - 4(1)(-2200)}}{2(1)}$ or better	B2	B1 for $\sqrt{(-25)^2 - 4(1)(-2200)}$ or better or for $\left(x - \frac{25}{2}\right)^2$ oe or B1 for $\frac{-(-25) + \sqrt{q}}{2(1)}$ or $\frac{-(-25) - \sqrt{q}}{2(1)}$ or both or for $\frac{25}{2} + \text{or} - \sqrt{\left(\frac{25}{2}\right)^2 + 2200}$
	-36.04 and 61.04 final answer	B1,B1	If B0B0, SC1 for values in ranges -36.042 to -36.041 and 61.041 to 61.042 seen or for answers -36[.0] or -36.042 to -36.041 and 61[.0] or 61.041 to 61.042 or -36.04 and 61.04 seen in working or for -61.04 and 36.04 as final ans
9(a)(i)	5 and 13	1	
9(a)(ii)	$8n - 3 = 203$	M1	Evaluation of 25th or 26th term with supporting evidence or explanation
	25.75 or $25\frac{3}{4}$	A1	Second evaluation of 25th or 26th terms with supporting evidence or explanation If zero scored, SC1 for 25.75 or 197 and 205 with partial evidence or explanation
9(b)(i)	$6n + 7$ oe final answer	2	B1 for $6n + c$ or $kn + 7$ $k \neq 0$
9(b)(ii)	$n^2 + n + 2$ oe final answer	2	B1 for a quadratic expression or second difference = 2
9(c)	$[y =] 10$	2	M1 for $5(20 - y) = 50$
	[First term =] 14	2	M1 for $5(x - \text{their } y) = 20$ or for $20 \div 5 + \text{their } y$