



# sequences

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1	<b>11 (a)</b> Reasonable diagram, 25, 13, 62 <b>(b)</b> 64, 19, 146 <b>(c)</b> $n^2$ oe $2n + 3$ oe <b>(d)(i)</b> 2 <b>(ii)</b> 20202 ft	4 3 2 1 1ft	<b>B1 B1 B1 B1</b> diagram may be freehand <b>B1 B1 B1</b> <b>B1</b> <b>B1</b> ft 10101 $\times$ their $k$
2	<b>10 (a)</b> Pentagon Octagon                      20  <b>(b)(i)</b> 35 <b>(ii)</b> 54  <b>(c)(i)</b> $p = 2, q = 3$  <b>(ii)</b> 4850 ft <b>(iii)</b> 20 cao  <b>(d)</b> 31 cao	1 1, 1  1 1  3  1ft 2  1	   <b>M1</b> for substituting a value of $n$ e.g. $\frac{1}{p} 4(4 - q) = 2 \quad n \geq 3$ <b>or M1</b> for number of diagonals from one vertex is $n - 3$ (allow in words) <b>and B1</b> for one correct value. If 0, SC1 for $\frac{n}{2}(n - 3)$ seen. ft their <b>(c)(i)</b> allow only if ft calculates to a positive integer. SC1 for answer of 17 <b>or M1</b> for their formula = 170
3	<b>10 (a)</b> Dots all correctly placed in Diagram 4  <b>(b)</b> Column 4 16, 25, 16, 41 Column 5 25, 41, 20, 61 Column $n$ : $n^2, 4n, n^2 + (n + 1)^2$ oe  <b>(c)(i)</b> 79 601 cao <b>(ii)</b> 800 ft  <b>(d)</b> 12 cao	1 7  1 1ft 1	  <b>B2 or B1</b> for three correct <b>B2 or B1</b> for three correct <b>B1 B1 B1</b> oe likely to be $(n - 1)^2 + n^2 + 4n$ or $2n^2 + 2n + 1$ After any correct answer for column $n$ , apply isw  ft their $4n$ linear expression only

4	9	<p>(a) (i) 21  (ii) <math>P_6 = \frac{1}{2} \times 6 \times 7</math> or better (= 21)  (iii) 1275  (iv) 3825  (v) 11325  (vi) 7500</p> <p>(b) (i) 56  (ii) <math>S_6 = \frac{1}{6} \times 6 \times 7 \times 8</math> or better (= 56)  (iii) 1540</p> <p>(c) <math>56 - 35 = 21</math></p> <p>(d) Correct algebraic proof with no errors</p>	<p>1  1  1  1ft  1  1ft  2  1  1  1  3</p>	<p>Allow <math>3(6 + 1)</math></p> <p>ft for <math>3 \times</math> their (iii)</p> <p>ft their (v) – their (iv) provided <math>&gt; 0</math></p> <p><b>M1</b> for <math>1 \times 6 + 2 \times 5 + 3 \times 4 + 4 \times 3 + 5 \times 2 + 6 \times 1</math></p> <p><b>M1</b> for <math>\frac{1}{6}n(n+1)(n+2) - \frac{1}{6}(n-1)(n)(n+1)</math> oe  and <b>M1</b> for <math>\frac{1}{6}n(n+1)(3)</math> oe</p>
5	10	<p>(a) 21 and 34</p> <p>(b) -5 8</p> <p>(c) (i) 4, 6</p> <p>(ii) <math>x = 28</math>  <math>y = -5</math>  <math>z = 23</math></p>	<p>1  1 + 1  3  5</p>	<p><b>M1</b> for <math>2 + d = e</math> oe or <math>d + e = 10</math> oe seen  and either <b>M1</b> for a correct eqn in <math>d</math> or <math>e</math> seen  e.g. <math>2e = 12</math> oe or <math>2d = 8</math> oe  or <b>B1</b> for either correct  <b>B4</b> for any two correct  or <b>M3</b> for <b>any</b> of <math>18 = 3x - 66</math> oe  or <math>3y + 33 = 18</math> oe or <math>33 - 3z = -36</math> oe  or <b>M1</b> for 2 of <math>y = x - 33</math> oe or <math>y + z = 18</math> oe  or <math>x + y = z</math> oe  and <b>M1</b> for combining two of the previous  equations correctly isw (does not have to be  simplified)</p> <p>after 0 scored  <b>SC1</b> for <math>-33 +</math> their <math>x =</math> their <math>y</math>  or their <math>x +</math> their <math>y =</math> their <math>z</math>  or their <math>y +</math> their <math>z = 18</math></p>

6	<p><b>11 (a)</b> 30 42 42 56 71 97</p> <p><b>(b) (i)</b> 2550 <b>(ii)</b> 30</p> <p><b>(c)</b> <math>(n + 1)(n + 2)</math> oe final ans</p> <p><b>(d) (i)</b> <math>2n^2 + pn + 1 = t</math> Uses a value of <math>n</math> up to 6 and a matching <math>t</math> from the table e.g. puts <math>n = 3</math> and <math>t = 31</math> <math>2 \times 3^2 + 3p + 1 = 31</math> <b>M1</b></p> <p><b>OR</b> Use <math>p = 4</math> to get <math>2n^2 + 4n + 1 = 31</math> and simplifies to 3 term eqn <b>M1</b></p> <p><b>OR both</b> <math>2 \times 9 + 4 \times 3 + 1 (= 31)</math> <b>M1</b> with one part evaluated</p> <p><b>OR</b> <math>n(n + 1) + (n + 1)(n + 2) - 1</math> or better <b>M1</b></p> <p><b>(ii)</b> 241 <b>(iii)</b> 12</p> <p><b>(e)</b> <math>L = A + D - 1</math> oe</p>	<p>4</p> <p>1 1</p> <p>1</p> <p>2</p> <p>1 3</p> <p>1</p>	<p><b>B3</b> for 2 correct rows or <b>B2</b> for 1 correct row or <b>B1</b> for any term in column 5 correct</p> <p>Correct solution shown with 1 intermediate step to <math>p = 4</math> <b>E1</b></p> <p>Solve correctly to get <math>n = 3</math> <b>E1</b></p> <p>Conclusion e.g. <math>31 = 31</math> <b>E1</b></p> <p>Correct simplification to <math>2n^2 + 4n + 1</math> <b>E1</b></p> <p><b>M1</b> for <math>2n^2 + 4n + 1 = 337</math> and <b>M1</b> for <math>(n - 12)(n + 14)</math> or correct expression for <math>n</math> using formula</p>
7	<p><b>10(a)</b> (A 1) 8 27 64 125 (B 4) 8 12 16 20 (C 4) 9 16 25 36</p> <p><b>(b)</b> 512 169</p> <p><b>(c)</b> 25 99</p> <p><b>(d)</b> 145 <math>n^3 + 4n</math> oe 16 <math>(n + 1)^2 - 4n</math> oe but isw</p>	<p>2 1 2</p> <p>1 1</p> <p>1 1</p> <p>1, 1 1, 1</p>	<p>B1 for 3 correct</p> <p>B1 for 3 correct</p> <p>Likely oe is <math>(n - 1)^2</math></p>

8	<p><b>9 (a)</b></p> <p>(i) 3, 8, 15 in correct positions (ii) 12</p> <p><b>(b)</b></p> <p>(i) <math>2 + 3n</math> oe (ii) <math>2^{n-1}</math> oe</p> <p><b>(c)</b> <math>a = \frac{1}{2}, b = 1\frac{1}{2}</math> cao</p>	<p>2 3</p> <p>2 2</p> <p>6</p>	<p>B1 for 2 correct values in correct positions M2 for <math>12 \times (12 + 2)</math> (= 168) or 12, (12 + 2) or M1 for <math>n^2 + 2n = 168</math> then M1 for <math>(n + a)(n + b)</math> where <math>a</math> and <math>b</math> are integers and <math>ab = -168</math> or <math>a + b = 2</math> oe</p> <p>Allow unsimplified e.g. <math>5 + 3(n - 1)</math> B1 for <math>3n</math> oe seen B1 for <math>2^k</math> seen</p> <p>B1 for 12 or 30 seen but if 30 clearly only from Diagram 4 then B0. M1 for any 1 of <math>a + b + 1 = 3</math> oe <math>8a + 4b + 2 = 12</math> oe <math>27a + 9b + 3 = 30</math> oe M1 for a 2<sup>nd</sup> of the above equations M1 (indep) for correctly eliminating <math>a</math> or <math>b</math> from pair of linear equations B1 for one correct value</p>
9	<p><b>11 (a)</b></p> <p>(i) 10 (ii) <math>\frac{3 \times 4}{2}</math> or <math>\frac{3 \times (3 + 1)}{2}</math> (= 6) (iii) 7260 (iv) 12 840 (v) 160 400</p> <p><b>(b)</b></p> <p>(i) 36, 100 (ii) 11025 (iii) <math>\left[ \frac{n(n+1)}{2} \right]^2</math> oe (iv) 3 348 900 (v) 32</p>	<p>1 1 1 2 2</p> <p>1, 1 1 1 1 2</p>	<p>M1 for <math>S_{200} - S_{120}</math> (20100 - 7260) or <math>\frac{80}{2}(121 + 200)</math> o.e. M1 for <math>2(1 + 2 + 3 + \dots + 400)</math> o.e.</p> <p>Ignore right-hand column isw M1 for square root then <math>\times 2</math> (1056) or SC1 for answer 33</p>
10	<p><b>12</b></p> <p><b>(a)</b></p> <p>(i) 12, ..., 30 (ii) <math>(n + 1)(n + 2)</math> oe (iii) <math>p = 2</math> <math>q = 2</math> (iv) 69(th), 70(th)</p> <p><b>(b)</b></p> <p>(i) <math>2 \times 3 + 7</math> (ii) 27 (iii) 1707, ..., 13 653</p>	<p>2 1 1 1 2</p> <p>1 1 1,1</p>	<p><b>B1</b> each isw if expand incorrectly</p> <p><b>M1</b> for their <math>2n + 2 = 140</math> soi Accept <math>2 \times 3 + 2 \times 2 + 3</math></p>

11	<p><b>6 (a)</b> <math>(x =) 64</math> www 3</p> <p><b>(b) (i)</b> <math>-1</math> <math>n^2</math> oe <math>5n</math> oe <math>n^2 + 5n</math> oe</p> <p><b>(ii)</b> 20</p> <p><b>(c)</b> <b>Final answer</b> <math>\frac{x-4}{2x-1}</math> cao www 4</p>	<p>3</p> <p>1 1 1 1</p> <p>2</p> <p>4</p>	<p><b>B2</b> for <math>x + 2x + x = 360 - 114 + 10</math> or better or <b>M1</b> for <math>x + 2x + 114 + x - 10 = 360</math></p> <p><b>M1</b> for their <math>n^2 + 5n = 500</math> or 20 <b>and</b> 25 seen</p> <p><b>B1</b> for <math>(x - 4)(x + 4)</math> <b>B2</b> for <math>(2x - 1)(x + 4)</math> or <b>SC1</b> for <math>(2x + a)(x + b)</math> where either <math>a + 2b = 7</math> or <math>ab = -4</math></p>
12	<p><b>11 (a)</b> 33, 41 <math>16\pi, 25\pi</math> <math>20\pi, 30\pi</math></p> <p><b>(b) (i)</b> <math>8n + 1</math> oe final answer</p> <p><b>(ii)</b> 137 www2</p> <p><b>(c) (i)</b> <math>n^2\pi</math> oe final answer</p> <p><b>(ii)</b> <math>9n^2\pi</math> oe final answer</p> <p><b>(d)</b> <math>n(n+1)\pi</math> oe final answer</p>	<p>1 1 2</p> <p>2</p> <p>2</p> <p>1</p> <p>1</p> <p>2</p>	<p><b>B1</b> each</p> <p>e.g. <math>9 + 8(n - 1)</math>, condone <math>n = 8n + 1</math> <b>SC1</b> for <math>8n + k</math></p> <p><b>M1</b> for their (b)(i) = 1097</p> <p>Allow <math>(3n)^2\pi</math></p> <p><b>SC1</b> for a quadratic expression e.g. <math>n(n + 1)</math>, <math>n^2 + 5</math>, <math>n^2 + n\pi</math></p>
13	<p><b>10</b></p> <p><b>(a)</b> <math>A</math> 1, <math>13 - 2n</math> oe <math>B</math> 36, <math>n^2</math> oe <math>C</math> 42, <math>n(n + 1)</math> oe <math>D</math> 729, <math>3^n</math> oe <math>E</math> 687, <math>3^n - n(n + 1)</math> oe</p> <p><b>(b) (i)</b> <math>-187</math></p> <p><b>(ii)</b> 10 100</p> <p><b>(c)</b> 8</p> <p><b>(d)</b> 58 939</p>	<p>3 2 3 2 2ft</p> <p>1ft</p> <p>1ft</p> <p>1</p> <p>1</p>	<p><b>B1, B2</b> (<b>M1</b> for <math>k - 2n</math>) oe</p> <p><b>B1, B1</b></p> <p><b>B1, B2</b> (<b>B1</b> for a quadratic in <math>n</math>)</p> <p><b>B1, B1</b></p> <p><b>B1ft</b> their <math>D -</math> their <math>C</math>, <b>B1ft</b> their <math>D -</math> their <math>C</math> only if both in terms of <math>n</math></p> <p>ft if <math>A</math> is linear</p> <p>ft if <math>C</math> is quadratic</p>

14	<p><b>10 (a)</b> 50, 70</p> <p>10<i>n</i> oe</p> <p>51, 71</p> <p>10<i>n</i> + 1 oe</p> <p><b>(b) (i)</b> 212</p> <p><b>(ii)</b> 20<i>n</i> + 12</p> <p><b>(iii)</b> 20<i>n</i> + 152</p> <p><b>(c) (i)</b> <math>5 \times 3^2 + 6 \times 3 = 63</math></p> <p>and <math>11 + 21 + 31 = 63</math></p> <p>or <math>32 + 31 = 63</math> or <math>11 + 52 = 63</math></p> <p><b>(ii)</b> 560</p> <p><b>(d)</b> Complete solution with no errors seen and a conclusion</p> <p>e.g.</p> $5n^2 + 6n + 10(n + 1) + 1$ $= 5n^2 + 6n + 10n + 10 + 1$ $= 5n^2 + 10n + 5 + 6n + 6$ $= 5n^2 + 10n + 5 + 6n + 6$ $= 5(n + 1)^2 + 6(n + 1)$	<p><b>1</b></p> <p><b>1</b></p> <p><b>1</b></p> <p><b>1</b></p> <p><b>1</b></p> <p><b>1</b></p> <p><b>1</b></p> <p><b>1</b></p> <p><b>1</b></p> <p><b>1</b></p> <p><b>1</b></p> <p><b>1</b></p> <p><b>1</b></p> <p><b>4</b></p>	<p><b>B1</b> for <math>5n^2 + 6n + 10n + 10 + 1</math> or better</p> <p><b>B1</b> for use of <math>5(n + 1)^2 = 5n^2 + 10n + 5</math> oe at any stage</p> <p><b>B1</b> for use of <math>6n + 6 = 6(n + 1)</math> oe at any stage</p>
15	<p><b>10 (a) (i)</b> 4.5 or <math>4\frac{1}{2}</math></p> <p><b>(ii)</b> <math>(x - 6)(x - 1)</math></p> <p>1, 6</p> <p><b>(iii)</b> 6</p> <p><b>(b)</b> <math>a = 1/3</math> oe, <math>b = 1/2</math> oe</p>	<p><b>3</b></p> <p><b>M2</b></p> <p><b>A1FT</b></p> <p><b>4</b></p> <p><b>6</b></p>	<p><b>M2</b> for a complete correct method <b>or M1</b> for one correct step at any stage.</p> <p><b>M1</b> for <math>(x + a)(x + b)</math> where <math>ab = 6</math> <b>or</b> <math>a + b = -7</math></p> <p><b>FT</b> their brackets <b>dep</b> on <b>M1</b> earned After <b>M0</b> scored <b>SC1</b> for 1, 6 as answer</p> <p><b>B1</b> for <math>2(3x - 2) + x + 2 = 4 \times 10</math> oe <b>and B1</b> for correct multiplication of a bracket <b>and M1</b> for correct rearrangement of their linear equation without brackets to <math>ax = b + c + d</math> or better</p> <p><b>B1</b> for any one of  <math>1 = a + b + 1/6</math> oe  <math>5 = 8a + 4b + 2/6</math> oe  <math>14 = 27a + 9b + 3/6</math> oe  <math>30 = 64a + 16b + 4/6</math> oe  Or any other correct equation  <b>and B1</b> for another of the above equations  <b>and M1</b> for equating one coefficient  or correct rearrangement to give <math>a</math> or <math>b</math> as subject  <b>and M1</b> for subtracting to eliminate <math>a</math> or <math>b</math>  or correct substitution for <i>their</i> <math>a</math> or their <math>b</math>  <b>A1</b> for <math>a = 1/3</math> oe or <math>b = 1/2</math> oe</p>

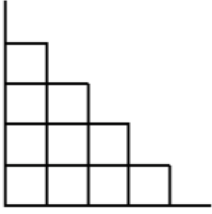
16	10	(a)	(i) $1 + 2 + 3 + 4 + 5 = 15$	1	
			(ii) Correct substitution equating to sum e.g. $\frac{2(2+1)}{k} = 3$ and $k = 2$ stated with no errors seen	2	<b>M1</b> for using a value of $n$ in $\frac{n(n+1)}{k}$ e.g. $\frac{2(2+1)}{k} = 3$ or for a verification using $k = 2$ e.g. $\frac{2(2+1)}{2} = 3$
			(iii) 1830	1	
			(iv) 30	2	<b>M1</b> for $\frac{n(n+1)}{2} = 465$ or better
			(v) $n - 8$	1	
	(b)	(i) 225, 15	2	<b>B1</b> either	
		(ii) $\frac{n^2(n+1)^2}{4}$ oe	1		
		(iii) 36100	2	<b>M1</b> for $\frac{19^2(19+1)^2}{4}$ oe or $190^2$	
17	10	(a)	48 and 57, $9n + 3$ oe	1 2	<b>B1</b> for $9n + k$ oe
		(b)	56 and 50, $86 - 6n$ oe	1 2	<b>B1</b> for $k - 6n$ oe
		(c)	125 and 216, $n^3$ oe	1 1	
		(d)	130 and 222 $n^3 + n$ oe	1 1FT	FT <i>their</i> (c) + $n$ dep on expression in $n$ in (c)
18	9	(a)	15 18 $3n + 3$ or $3(n + 1)$ 6 10 25 36 $(n + 1)^2$	9	<b>B2</b> for 15, 6, 25 or <b>B1</b> for two correct values  <b>B3</b> for 18, 10, 36 or <b>B1</b> for each correct value  <b>B2</b> for $3n + 3$ oe or <b>M1</b> for $3n + k$ , for any $k$  <b>B2</b> for $(n + 1)^2$ oe or <b>M1</b> for a quadratic expression
		(b)	14	2	<b>M1</b> for $(n + 1)(n + 2) = 240$ or better or $15 \times 16 = 240$
		(c)	(i) $\frac{1}{2} + p + q = 9$  (ii) $[p = ] 3$ $[q = ] \frac{11}{2}$	1  5	<b>B2</b> for $4p + 2q = 23$ or <b>B1</b> for $\frac{1}{2} \times 23 + p \times 22 + q \times 2$ oe <b>M1</b> for correct multiplication and subtraction of <i>their</i> equations  <b>A1</b> for $[p = ] 3$ or $[q = ] \frac{11}{2}$  If 0 scored then <b>SC1</b> for either correct



19	<b>11 (a)</b> $\frac{1}{8} \frac{1}{16} \frac{1}{32}$ $\frac{1}{2^{n-1}}$ oe $2^{-3} 2^{-4} 2^{-5}$ $2^{1-n}$ or $2^{-(n-1)}$	<b>2</b>  <b>2</b>  <b>1</b>  <b>1</b>	<b>B1</b> for 2 correct  <b>SC1</b> for $\frac{1}{2^n}$ oe
	<b>(b) (i)</b> 64 256 1024 $2^6 2^8 2^{10}$	<b>1</b> <b>1</b>	
	<b>(ii)</b> $2^{2(n-1)}$ or $2^{2n-2}$	<b>1</b>	
	<b>(c)</b> 16384	<b>2</b>	<b>B1</b> for $n = 8$
20	<b>9 (a)</b> 36, 9, 45 $8n + 4$ oe $(n-1)^2$ oe	<b>2</b> <b>2</b> <b>2</b>	<b>B1</b> for two correct values  <b>M1</b> for $8n + k$ , for any $k$  <b>M1</b> for a quadratic expression of form $n^2 [+ an + b]$ oe
	<b>(b)</b> 19	<b>2</b>	<b>M1</b> for $(n+1)(n+5) = 480$ or better or $20 \times 24$ seen
	<b>(c) (i)</b> $\frac{1}{3} + p + q = 12$ and no errors seen	<b>1</b>	Accept $p + q = 12 - \frac{1}{3}$ after $\frac{1}{3}[l^3] + p[l^2] + q[l]$ shown
	<b>(ii)</b> $\frac{1}{3} \times 8 + 4p + 2q = 12 + 21$	<b>2</b>	<b>M1</b> for $12 + 21$ seen or 33 seen
	<b>(iii)</b> $[p =] \frac{7}{2}$ oe $[q =] \frac{49}{6}$ oe	<b>3</b>	<b>M1</b> for correct multiplication and subtraction or substitution using the correct given equations <b>B1</b> for $[p =] \frac{7}{2}$ or $[q =] \frac{49}{6}$  After 0 scored, <b>SC1</b> for 2 values satisfying one of the original correct given equations
21	<b>9 (a)</b> 28 45 17 21 45 66	<b>1, 1</b> <b>1</b> <b>1</b>	
	<b>(b) (i)</b> $4n - 3$ oe	<b>2</b>	<b>M1</b> for $4n + k$
	<b>(ii)</b> 237	<b>1</b>	
	<b>(iii)</b> 50	<b>2FT</b>	<b>FT</b> <i>their (b)(i) = 200</i> solved and then answer truncated <b>dep</b> on linear expression of form $an + k$ <b>M1</b> for <i>their</i> $4n - 3 = 200$ or <i>their</i> $4n - 3 \leq 200$

		(c) $p = 2$ and $q = -5$ with some correct supporting working leading to the solutions	5	<p><b>M2</b> for any 2 of <math>p + q + 3 = 0</math> oe, <math>2^2 p + 2q + 3 = 1</math> oe, <math>3^2 p + 3q + 3 = 6</math> oe, <math>4^2 p + 4q + 3 = 15</math> oe, <math>5^2 p + 5q + 3 = \text{their } 28</math> oe, etc.  or <b>M1</b> for any one of these  <b>M1</b> indep for correctly eliminating <math>p</math> or <math>q</math> from pair of linear equations  <b>A1</b> for one correct value  If 0 scored <b>SC1</b> for 2 values that satisfy one of their original equations  After <b>M0</b>, 2 correct answers <b>SC1</b></p>
		(d) $2n^2 - n$ or $n(2n - 1)$	2	<p><b>B1</b> for answer <math>2n^2 + k[n]</math>  or <b>M1</b> for <i>their quadratic</i> from (c) + <i>their linear</i> from (b)(i)</p>
22	11	<p>(a) 5 <math>\frac{n}{n+2}</math> oe  7 <math>n+2</math> oe  7 <math>n-2</math> oe  3 <math>n^2 - 4</math> oe  21</p> <p>(b) 72</p> <p>(c) 27</p>	8	<p><b>B1</b> each</p> <p><b>M1</b> for <math>\frac{72}{74}</math> or <i>their</i> <math>\frac{n}{n+2} = \frac{36}{37}</math></p> <p><b>M1</b> for <i>their</i> <math>(n^2 - 4) = 725</math> or <math>25 \times 29 [= 725]</math></p>

23	9	<p>(a) (i) 16 (ii) <math>n^2</math></p> <p>(b) (i) 43 (ii) 7</p> <p>(c) <math>a = \frac{5}{2}</math> oe, <math>b = \frac{5}{6}</math> oe with supporting working</p>	<p>1 1 1 1 6</p>	<p><b>M1</b> for any correct substitution eg <math>\frac{2}{3}(2)^3 + 2^2a + 2b</math></p> <p><b>A1</b> for <b>one</b> of eg <math>\frac{2}{3} + a + b = 4</math> or better eg <math>\frac{16}{3} + 4a + 2b = 17</math> or better eg <math>\frac{54}{3} + 9a + 3b = 43</math> or better</p> <p><b>A1</b> for <b>another</b> of eg <math>\frac{2}{3} + a + b = 4</math> or better eg <math>\frac{16}{3} + 4a + 2b = 17</math> or better eg <math>\frac{54}{3} + 9a + 3b = 43</math> or better</p> <p><b>M1</b> for correctly eliminating one variable from two of <i>their</i> equations in <math>a</math> and <math>b</math></p> <p><b>A1</b> for <math>a = \frac{5}{2}</math> oe <b>A1</b> for <math>b = \frac{5}{6}</math> oe</p> <p>After zero scored, <b>SC2</b> for 2 correct answers without supporting working or <b>SC1</b> for 2 of 17, 43, 86, 150, 239 seen</p>
24	10	<p><b>A</b> -13, -20 <math>-7n + 22</math> oe</p> <p><b>B</b> <math>\frac{9}{22}, \frac{10}{23}</math> <math>n + 4</math> <math>n + 17</math> oe</p> <p><b>C</b> 26, 37 <math>n^2 + 1</math> oe</p> <p><b>D</b> 162, 486 <math>2 \times 3^{n-1}</math> oe</p>	<p>1 2 1 2 1 1 1 2</p>	<p><b>SC1</b> for <math>-7n + k</math> or <math>kn + 22</math> oe</p> <p><b>B1</b> for <math>n + 4</math> oe or <math>n + 17</math> oe seen, but not in wrong position</p> <p><b>SC1</b> for <math>k \times 3^{n+p}</math> [<math>k, p</math> integers] Accept <math>2 \times \frac{3^n}{3}</math></p>

25	11 (a)		1	
	(b)	30 10	1 1	
	(c)	$n(n+1)$ oe	2	<b>B1</b> for $an^2 + bn + c$ $a, b, c$ numeric $a \neq 0$
	(d)	$\frac{1}{2}n(n-1)$ oe	2	<b>B1</b> for using $\frac{1}{2}$ oe in expression of form
				$\frac{1}{2}(an^2 + bn + c)$ $a \neq 0$ or $kn(n-1)$ $k \neq 0$
26	10 (a)	10 15 15 21 35 48	6	<b>B1</b> for each correct entry
	(b) (i)	3	2	<b>M1</b> for any correct substitution in $n^2 + 4n + p$ = number of tiles eg $2^2 + 4(2) + p = 15$
	(ii)	143	1FT	<b>FT</b> 140 + <i>their</i> (b)(i)
	(c)	$a = \frac{1}{2}$ oe $b = \frac{3}{2}$ oe nfw	5	<b>B1</b> for a correct simplified equation e.g. $a + b + 1 = 3$ , $4a + 2b + 1 = 6$ , $9a + 3b + 1 = 10$ etc <b>B1</b> for a 2 <sup>nd</sup> correct simplified equation <b>M1</b> for correctly eliminating one variable for <i>their</i> equations in $a$ and $b$
				<b>A1</b> for $a = \frac{1}{2}$ nfw
				<b>A1</b> for $b = \frac{3}{2}$ nfw
27	9(a)(i) 9(a)(ii)	5 and 13 $8n - 3 = 203$  25.75 or $25\frac{3}{4}$	1 <b>M1</b>  <b>A1</b>	Evaluation of 25th or 26th term with supporting evidence or explanation  Second evaluation of 25th or 26th terms with supporting evidence or explanation  If zero scored, <b>SC1</b> for 25.75 or 197 and 205 with partial evidence or explanation
	9(b)(i)	$6n + 7$ oe final answer	2	<b>B1</b> for $6n + c$ or $kn + 7$ $k \neq 0$
	9(b)(ii)	$n^2 + n + 2$ oe final answer	2	<b>B1</b> for a quadratic expression or second difference = 2
	9(c)	[ $y =$ ] 10	2	<b>M1</b> for $5(20 - y) = 50$
		[First term =] 14	2	<b>M1</b> for $5(x - \text{their } y) = 20$ or for $20 \div 5 + \text{their } y$

28	6(a)   6(b)  6(c)  6(d)	$18 \quad 22 \quad 4n + 2$ oe $17 \quad 26 \quad n^2 + 1$ oe  242  15  3	6   1  1  2	<b>B2</b> for 18, 22, 17, 26 or <b>B1</b> for two or three correct values AND <b>B2</b> for $4n + 2$ oe or <b>B1</b> for $4n + k$ oe or $pn + 2$ ( $p \neq 0$ ) AND <b>B2</b> for $n^2 + 1$ oe or <b>B1</b> for $n^2 + k$ oe  <b>FT</b> <i>their</i> $4n + 2$ provided a linear expression  <b>M1</b> for $2 \times 1^2 + 2 \times 1 + q = 7$ oe
29	12(a)    12(b)  12(c)  12(d)	18 28  $3n + 3$ oe  45  $[a = ] \frac{3}{2}$ oe $[b = ] \frac{13}{3}$ oe	2   2  2  6	<b>B1</b> for each  <b>B1</b> for $3n + k$ oe or $cn + 3$ oe $c \neq 0$  <b>M1</b> for identifying 7th pattern or <b>M1</b> for <i>their</i> $(3n + 3) = 24$  <b>M1</b> for any correct substitution e.g. $\frac{1}{6}(2)^3 + 2^2a + 2b$  <b>A1</b> for one of e.g. $\frac{1}{6} + a + b = 6$ oe $\frac{8}{6} + 4a + 2b = 16$ oe $\frac{27}{6} + 9a + 3b = 31$ oe $\frac{64}{6} + 16a + 4b = 52$ oe  <b>A1</b> for another of the above <b>M1</b> for correctly eliminating one variable from <i>their</i> equations  <b>A1</b> for $a = \frac{3}{2}$  <b>A1</b> for $b = \frac{13}{3}$ oe

30	11(a)	40 54 26 34	4	<b>B1</b> for each
	11(b)	$n^2 + 3n$ or $n(n + 3)$ oe	2	<b>B1</b> for a quadratic expression or for 2nd common difference 2 (at least 2 shown) or for 2 correct equations seen  or for subtracting $n^2$
	11(c)	100	2	<b>M1</b> for <i>their</i> <b>(b)</b> = 10300 seen
	11(d)	$[a = ] \frac{1}{2}$ oe and $[b = ] \frac{5}{2}$ oe	2	<b>B1</b> for each or <b>M1</b> for one correct equation or for 2nd difference = 1 soi (at least 2 shown)
31	7(a)	25 36 10 15 35 51	2	<b>B1</b> for 3, 4 or 5 correct
	7(b)	$n^2$	1	
	7(c)(i)	92	1	
	7(c)(ii)	$\frac{1}{2}(n^2 - n)$ oe	2	<b>M1</b> for $\frac{1}{2}(3n^2 - n) - n^2$ oe or for final quadratic answer with $\frac{1}{2}n^2$ oe or $-\frac{1}{2}n^2$ oe but not both
	7(d)	$a = \frac{1}{2}, b = \frac{1}{2}$	5	<b>B2</b> for 2 correct equations eg $a + b = 1, 8a + 4b = 6$ or <b>B1</b> for 1 correct equation  <b>B2</b> for one correct value or <b>M1</b> (dep on at least B1) for correctly eliminating one variable from two linear equations in a and b  OR  <b>B2</b> for $a = \frac{1}{2}$ or <b>B1</b> for $6a = 3$ or for 3 <sup>rd</sup> difference = 3  <b>B2</b> for $b = \frac{1}{2}$ or <b>M1</b> for substituting <i>their</i> a into a correct equation of first differences

32	<p>11(a) A: <math>-3</math>      <math>17 - 4n</math> oe</p> <p>B: <math>124</math>      <math>n^3 - 1</math> oe</p> <p>C: <math>\frac{11}{128}</math>      <math>\frac{n+6}{2^{n+2}}</math> oe</p>		<p>3</p> <p>3</p> <p>4</p>	<p><b>B1</b> for <math>-3</math>  <b>B2</b> for <math>17 - 4n</math> oe  or <b>B1</b> for <math>k - 4n</math> oe or <math>17 - pn</math> oe, <math>p \neq 0</math></p> <p><b>B1</b> for <math>124</math>  <b>B2</b> for <math>n^3 - 1</math> oe  or <b>B1</b> for any cubic</p> <p><b>B1</b> for <math>\frac{11}{128}</math>  <b>B3</b> for <math>\frac{n+6}{2^{n+2}}</math> oe  or <b>B2</b> for <math>2^{n+2}</math> oe seen  or <b>B1</b> for <math>2^k</math> oe or <math>n + 6</math> seen</p>
33	<p>11(b) <math>\frac{p+1}{2q}</math> oe</p>	<p>11A <math>24</math></p> <p><math>5n - 1</math> oe</p> <p>11B <math>127</math></p> <p><math>n^3 + 2</math> oe</p> <p>11C <math>256</math></p> <p><math>4^{(n-1)}</math> oe</p>	<p>2</p> <p><b>B1</b></p> <p><b>B2</b></p> <p><b>B1</b></p> <p><b>B2</b></p> <p><b>B1</b></p> <p><b>B2</b></p>	<p><b>B1</b> for <math>p + 1</math> or <math>2q</math> oe</p> <p><b>B1</b> for <math>5n - k</math> or <math>jn - 1</math> oe <math>j \neq 0</math></p> <p><b>B1</b> for <math>n^3</math> oe</p> <p><b>B1</b> for <math>4^k</math> oe</p>