



# Solving Equations and Inequalities

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1	14	6	3	<b>M1</b> for one correct first step which leads towards simplifying $3y - 12 + \frac{y}{2} = 9$ or $6(y - 4) + y = 18$ or $y - 4 + \frac{y}{6} = 3$
2	10	3.4 or $3\frac{2}{5}$	3	<b>M1</b> $22 - 6x$ <b>M1</b> $4x + 6x = 22 + 12$
3	12	14.5 oe	3	<b>M2</b> for complete correct method or <b>M1</b> for one correct step
4	5	4.8 oe	2	<b>M1</b> for $5 + 19 = 3x + 2x$ oe or better or <b>B1</b> for $24 - 2x = 3x$ oe or $5 = 5x - 19$ oe
5	3	-8	2	<b>M1</b> for $2x = -16$ or $\frac{1}{2} + x = -7.5$ oe or better
6	3	30	2	<b>M1</b> for $n - 8 = 22$ or $\frac{n}{7} = 15$
7	10	3.75 oe	3	<b>M2</b> for $3 \times 5 = 7x - 3x$ oe or <b>M1</b> for $3(x + 5) = 7x$ or $x + 5 = \frac{7}{3}x$ or $1 + \frac{5}{x} = \frac{7}{3}$ or better
8	6	9.5 or $\frac{19}{2}$	3	<b>M2</b> for $2x = (8 \times 3) - 5$ or better oe or <b>M1</b> for $2x + 5 = 8 \times 3$ or better
9	6	$8 \times 10^3$ or 8000 nfw	2	<b>M1</b> for $w + 4 \times 10^3 = 1.2 \times 10^4$ oe or $5w + 20 \times 10^3 = 6 \times 10^4$ oe
10	9	2.8 oe	3	<b>M2</b> for $12 + 2 = 8x - 3x$ or better or <b>M1</b> for $3x + 12$ or $8x - 2$
11	1	7, -4	1	
12	4	0.5 or $\frac{1}{2}$	2	<b>M1</b> for correct first step e.g. $6y + 6 = 9$ or $y + 1 = \frac{9}{6}$
13	3	21	2	<b>M1</b> for $k - 8 = 13$ or $6k - 48 = 78$ or better

14	13	(a) 11 (b) 8	1 2FT	FT 30 – 2 × <i>their</i> (a)  or M1 for $4 \times 7 = 2(x - 1) + FG$ oe or $4(x - 4) = 2(x - 1) + FG$ oe or $2 \times 7 + 2(x - 4) = 2(x - 1) + FG$ oe Allow $x$ to be <i>their</i> (a) in each
15	10	120	3	M1 $7t + 11(t + 5) = 2215$ A1 $18t + 55 = 2215$
16	10	(a) $x + x + 4 + x + 4 = 26$ oe (b) 6[.00] cao	1 2	M1 for their linear eqn simplified to $ax = b$
17	7	5	3	M2 for $(x - 5)(x - 1)$ or M1 for evidence of a factorisation which gives the correct coefficient of $x$ or positive prime constant term e.g. $(x - 7)(x + 1)$ , $(x - 4)(x - 2)$ , $(x - 3)(x - 1)$
18	12	(a) $(3x - 4)(x + 2)$  (b) $1\frac{1}{3}, -2$	2  1FT	M1 for $(3x + a)(x + b)$ where $a + 3b = 2$ or $ab = -8$ if M0 then SC1 for $3\left(x - \frac{4}{3}\right)(x + 2)$  dep on M1
19	14	-2.64, 1.14 cao with working	4	B1 for $\sqrt{3^2 - 4(2)(-6)}$ or better seen anywhere B1 for $p = -3$ and $r = 2 \times 2$ or better as long as in the form $\frac{p + \sqrt{q}}{r}$ or $\frac{p - \sqrt{q}}{r}$ After B0B0, SC1 for -2.6 or -2.637(45...) and 1.1 or 1.137(45...)
20	20	$x = 0.84$ or $7.16$	4	B1 $\frac{8 \pm k}{2}$ B1 $\sqrt{8^2 - 4 \times 1 \times 6}$ or better A1 A1
21	15	-3.44, 0.44  correct working must be shown	4	B1 for $\sqrt{(6)^2 - 4(2)(-3)}$ or better seen B1 if in form $\frac{p + (or-)q}{r}$ , for $p = -6$ and $r = 2 \times 2$ oe B1, B1 (SC1 -3.4 or -3.436... and 0.4 or 0.436...)

22	15	$\frac{-7 \pm \sqrt{7^2 - 4(2)(-3)}}{2 \times 2}$ <p>0.39, -3.89    cao</p>	<p><b>B2</b></p> <p><b>B1,B1</b></p>	<p><b>B1</b> for <math>\sqrt{7^2 - 4(2)(-3)}</math> or better seen</p> <p><b>B1</b> for <math>p = -7</math> and <math>r = 2 \times 2</math> or better as long as in the form <math>\frac{p + \sqrt{q}}{r}</math> or <math>\frac{p - \sqrt{q}}{r}</math></p> <p>After <b>B0B0</b> for the two answers, <b>SC1</b> for 0.4 or 0.386[0009...] and -3.9 or -3.886[0009...] or <b>SC1</b> for -0.39 and 3.89</p>
23	14	$\sqrt{1^2 - 4(2)(-2)}$ <p>If in form <math>\frac{p + \sqrt{q}}{r}</math> or <math>\frac{p - \sqrt{q}}{r}</math>  <math>p = -1, r = 2(2)</math> or 4</p> <p>- 1.28 0.78</p>	<p><b>B1</b></p> <p><b>B1</b></p> <p><b>B1</b></p> <p><b>B1</b></p> <p><b>B1</b></p>	<p>If completing the square <b>B1</b> for <math>\left(x + \frac{1}{4}\right)^2</math> oe</p> <p><b>B1</b> for <math>x = -\frac{1}{4} + \sqrt{1 + \left(\frac{1}{4}\right)^2}</math>  or <math>x = -\frac{1}{4} - \sqrt{1 + \left(\frac{1}{4}\right)^2}</math></p> <p>If <b>0</b> scored for the last two <b>B</b> marks then <b>SC1</b> for - 1.3 and 0.8  or - 1.281 to - 1.280 and 0.781 or 0.7807 to 0.7808  or 1.28 and - 0.78  or - 1.28 and 0.78 seen in the working</p>
24	19	$\sqrt{(-6)^2 - 4(5)(-3)}$ <p>if <math>\frac{p + \sqrt{q}}{r}</math> or <math>\frac{p - \sqrt{q}}{r}</math> seen then  <math>p = -(-6)</math> and <math>r = 2 \times 5</math></p> <p>-0.38 1.58 cao final answers</p>	<p><b>B1</b></p> <p><b>B1</b></p> <p><b>B1</b></p> <p><b>B1</b></p>	<p>If completing the square  <b>B1</b> for <math>\left(x - \frac{3}{5}\right)^2</math> oe</p> <p><b>B1</b> for <math>\frac{3}{5} + \sqrt{\frac{3}{5} + \left(\frac{3}{5}\right)^2}</math> or <math>\frac{3}{5} - \sqrt{\frac{3}{5} + \left(\frac{3}{5}\right)^2}</math> oe</p> <p>If <b>B0</b>, <b>SC1</b> for  - 0.4 and 1.6  or - 0.379[795..] and 1.579[795..]  or - 1.58 and 0.38  as final answers  or - 0.38 and 1.58 seen in working</p>

25	21	$\sqrt{(4)^2 - 4(3)(-5)}$ or better seen if $\frac{p + \sqrt{q}}{r}$ or $\frac{p - \sqrt{q}}{r}$ seen then  $p = -4$ and $r = 2(3)$  $-2.12$ $0.79$ final answers	<b>B1</b> If completing the square  <b>B1</b> for $\left(x + \frac{2}{3}\right)^2$ oe  <b>B1</b> for $-\frac{2}{3} + \sqrt{\frac{5}{3} + \frac{2^2}{3^2}}$ or $-\frac{2}{3} - \sqrt{\frac{5}{3} + \frac{2^2}{3^2}}$  <b>B1</b> <b>B1</b> If <b>B0</b> , <b>SC1</b> for $0.786[299]$ <b>and</b> $-2.119[632]$ $-2.1$ <b>and</b> $0.8$ or $-2.120$ or $-2.119$ <b>and</b> $0.786$ or $2.12$ and $-0.79$ final answers $-2.12$ <b>and</b> $0.79$ seen not as final answers
26	17	$\frac{-(-11) \pm \sqrt{(-11)^2 - 4(3)(4)}}{2 \times 3}$  $0.41$ and $3.26$ final ans cao	<b>2</b> <b>B1</b> for $\sqrt{(-11)^2 - 4(3)(4)}$ or better  and, if in form $\frac{p + \sqrt{q}}{r}$ or $\frac{p - \sqrt{q}}{r}$ , <b>B1</b> for $p = -(-11)$ and $r = 2(3)$  <b>B1B1</b> <b>SC1</b> for $0.4$ and $3.3$ or $0.409\dots$ and $3.257\dots$ or $-0.41$ and $-3.26$  or $0.41$ and $3.26$ seen in working
27	23	$\sqrt{(3)^2 - 4(2)(-3)}$ oe or better  $\frac{-3 + \sqrt{k}}{2(2)}$ or $\frac{-3 - \sqrt{k}}{2(2)}$ oe  $-2.19, 0.69$	<b>B1</b> If completing the square, <b>B1</b> for $\left(x + \frac{3}{4}\right)^2$ oe  <b>B1</b> <b>B1</b> for $-\frac{3}{4} + \sqrt{\frac{3}{2} + \left(\frac{3}{4}\right)^2}$ or $-\frac{3}{4} - \sqrt{\frac{3}{2} + \left(\frac{3}{4}\right)^2}$ oe  <b>B1B1</b> <b>SC1</b> for $-2.2$ or $-2.186\dots$ <b>and</b> $0.7$ or $0.686\dots$ or $-2.19$ <b>and</b> $0.69$ seen but not final answer or $2.19$ <b>and</b> $-0.69$ <b>Maximum score without working is 2</b>
28	13	$x < -3$	<b>3</b> <b>M1</b> correct move <b>M1</b> correct move <b>M1</b> correct move
29	6	1, 2, 3, 4	<b>3</b> <b>M1</b> $10x < 45$ <b>A1</b> $x < 4.5$
30	4	$y \neq -1.25$	<b>2</b> <b>M1</b> inequality with $y$ 's and constants correctly collected

31	9	$x \leq 39$ www	3	M1 correct first move M1 correct 2nd move M1 correct move to answer line
32	16	$x < 6.8$	4	B3 for 6.8 with wrong inequality or equal as answer. Or M1 for first move completed correctly and M1 for second move completed correctly and M1 for third move completed correctly
33	8	$x \geq -\frac{3}{8}$ oe	2	M1 for $-3 \leq 8x$ oe If 0 then SC1 for $-\frac{3}{8}$ with incorrect inequality.
34	18	-1 -2 -3 -4	4	B3 for $x < -\frac{3}{5}$ and $x > -4.5$ oe or B2 for $x < -\frac{3}{5}$ or $x > -4.5$ oe or B1 for $5x < -3$ or $-9 < 2x$ oe Or mark on answer line -1 oe
35	14 (a)	$n < 9$	2	M1 for $2n < 18$ or $2n - 18 < 0$ oe If 0 scored SC1 for 9 with incorrect inequality.
	(b)	$(b + d)(a + c)$	2	B1 for $b(a + c) + d(a + c)$ or $a(b + d) + c(b + d)$
36	15	[0], 1, 2, 3	4	M1 for moving the 5 correctly M1 for collecting <i>their</i> terms
37	9	$t < -\frac{6}{7}$	2	M1 for $5t + 2t < 17 - 23$ If zero scored SC1 for $-\frac{6}{7}$ with incorrect inequality sign or equals sign
38	4	$n < 1.5$ oe final answer	2	B1 for 1.5 oe in answer or M1 for $3 > 8n - 6n$ oe
39	8	$x > -9$	2	M1 for $\frac{x}{3} > 2 - 5$ oe or $\left(\frac{x}{3} + 5\right) \times 3 > 2 \times 3$ oe
40	7	1, 2, 3	3	B2 for $t < 4$ or M1 for $2 + 6 > 3t - t$ oe or better If zero scored, SC1 for answer 0, 1, 2, 3 or 1, 2, 3, 4
41	12	$n < -4.4$ or $n < -4\frac{2}{5}$ final answer	2	M1 for $8n - 3n < -5 - 17$ or better or $3n - 8n > 17 + 5$ or better