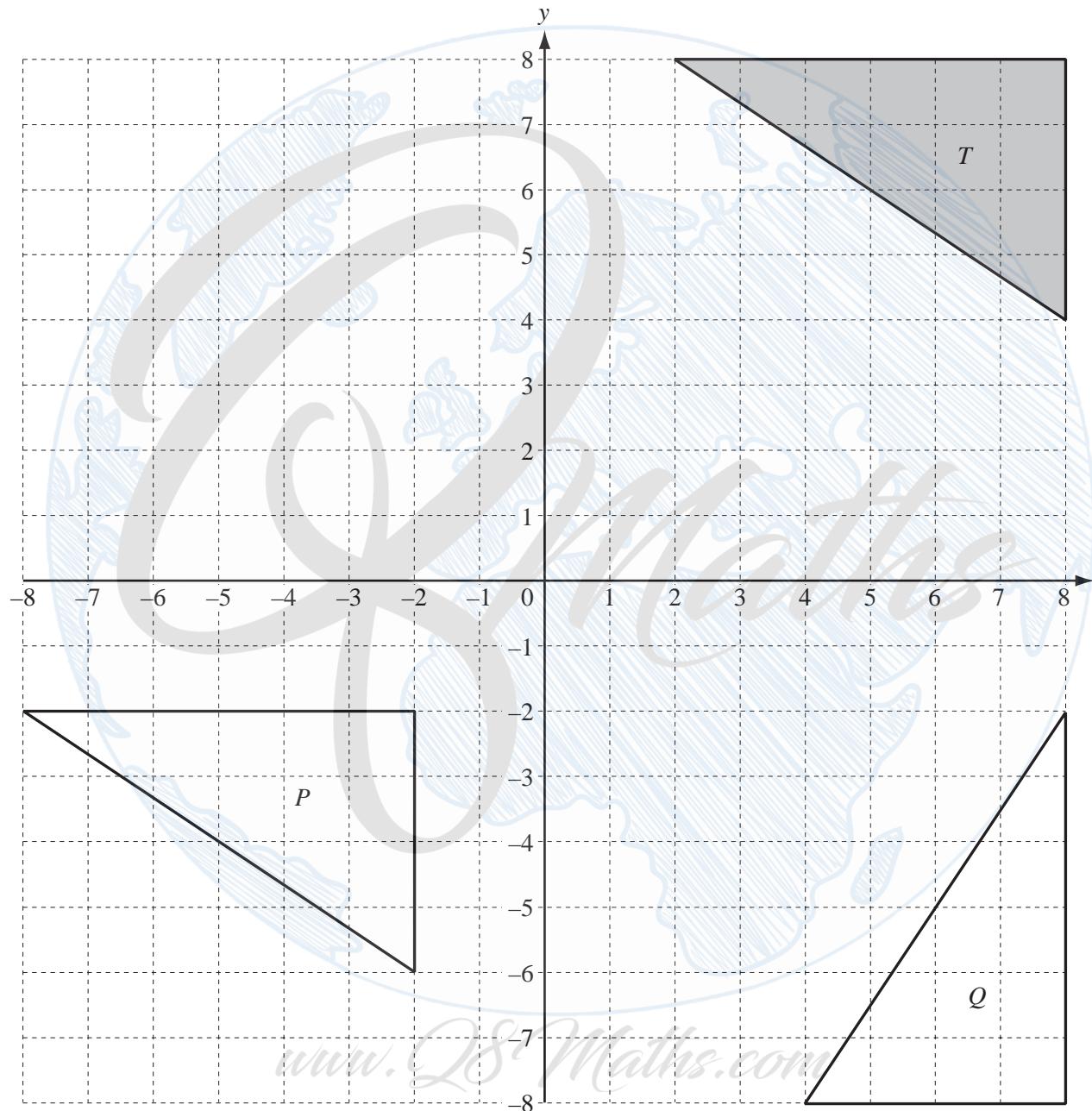


# Transformations

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3



- (a) On the grid, draw the enlargement of the triangle  $T$ , centre  $(0, 0)$ , scale factor  $\frac{1}{2}$ . [2]

**(b)** The matrix  $\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$  represents a transformation.

**(i)** Calculate the matrix product  $\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} 8 & 8 & 2 \\ 4 & 8 & 8 \end{pmatrix}$ .

*Answer(b)(i)*

[2]

**(ii)** On the grid, draw the image of the triangle  $T$  under this transformation. [2]

**(iii)** Describe fully this **single** transformation.

*Answer(b)(iii)* ..... [2]

**(c)** Describe fully the **single** transformation which maps

**(i)** triangle  $T$  onto triangle  $P$ ,

*Answer(c)(i)* ..... [2]

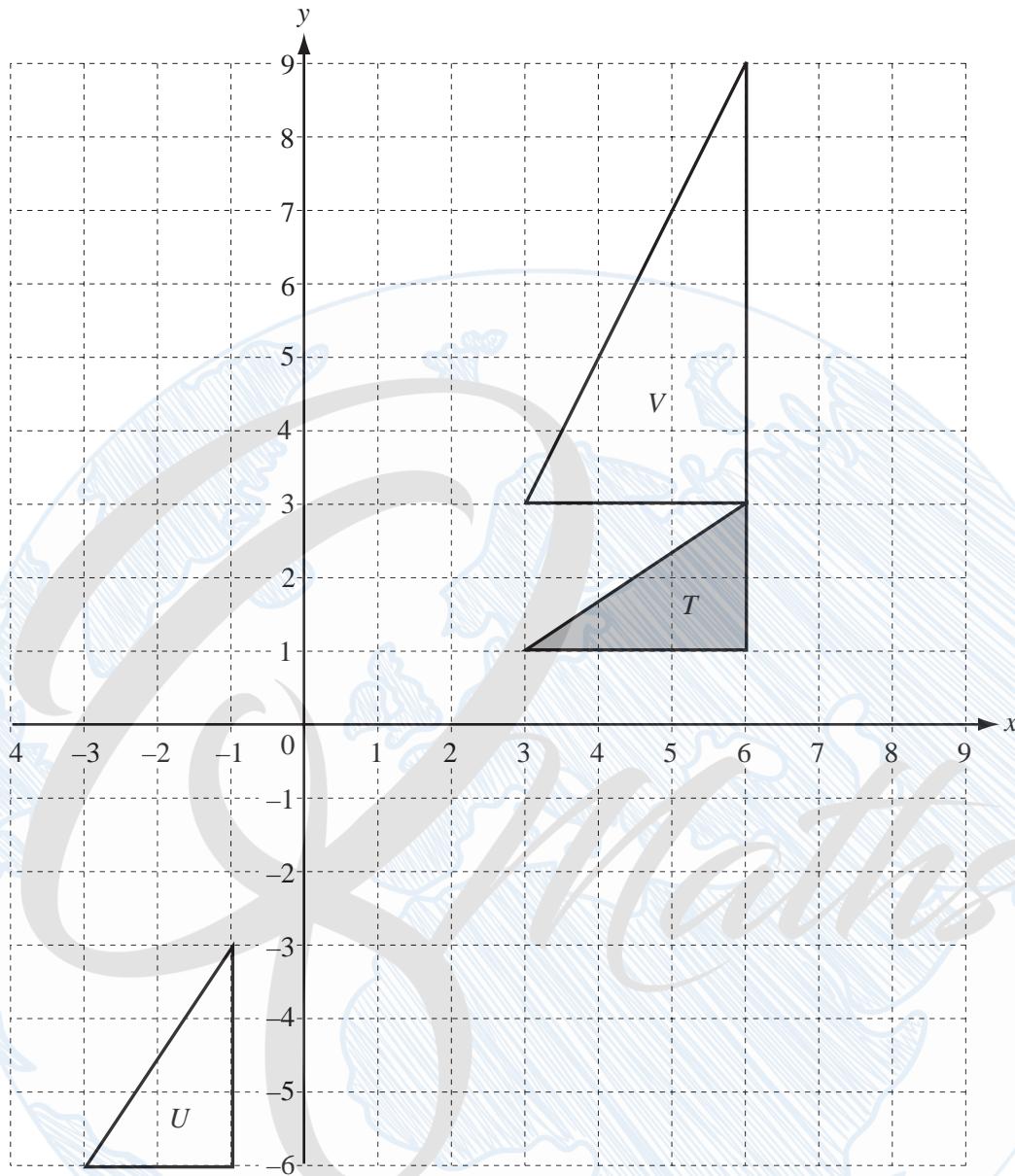
**(ii)** triangle  $T$  onto triangle  $Q$ .

*Answer(c)(ii)* ..... [3]

**(d)** Find the 2 by 2 matrix which represents the transformation in **part (c)(ii)**.

*Answer(d)*  $\begin{pmatrix} & \\ & \end{pmatrix}$  [2]

4



(a) On the grid, draw

(i) the translation of triangle  $T$  by the vector  $\begin{pmatrix} 7 \\ 3 \end{pmatrix}$ , [2]

(ii) the rotation of triangle  $T$  about  $(0, 0)$ , through  $90^\circ$  clockwise. [2]

(b) Describe fully the **single** transformation that maps

(i) triangle  $T$  onto triangle  $U$ ,

*Answer(b)(i)* ..... [2]

(ii) triangle  $T$  onto triangle  $V$

*Answer(b)(ii)* ..... [3]

(c) Find the 2 by 2 matrix which represents the transformation that maps

(i) triangle  $T$  onto triangle  $U$ ,

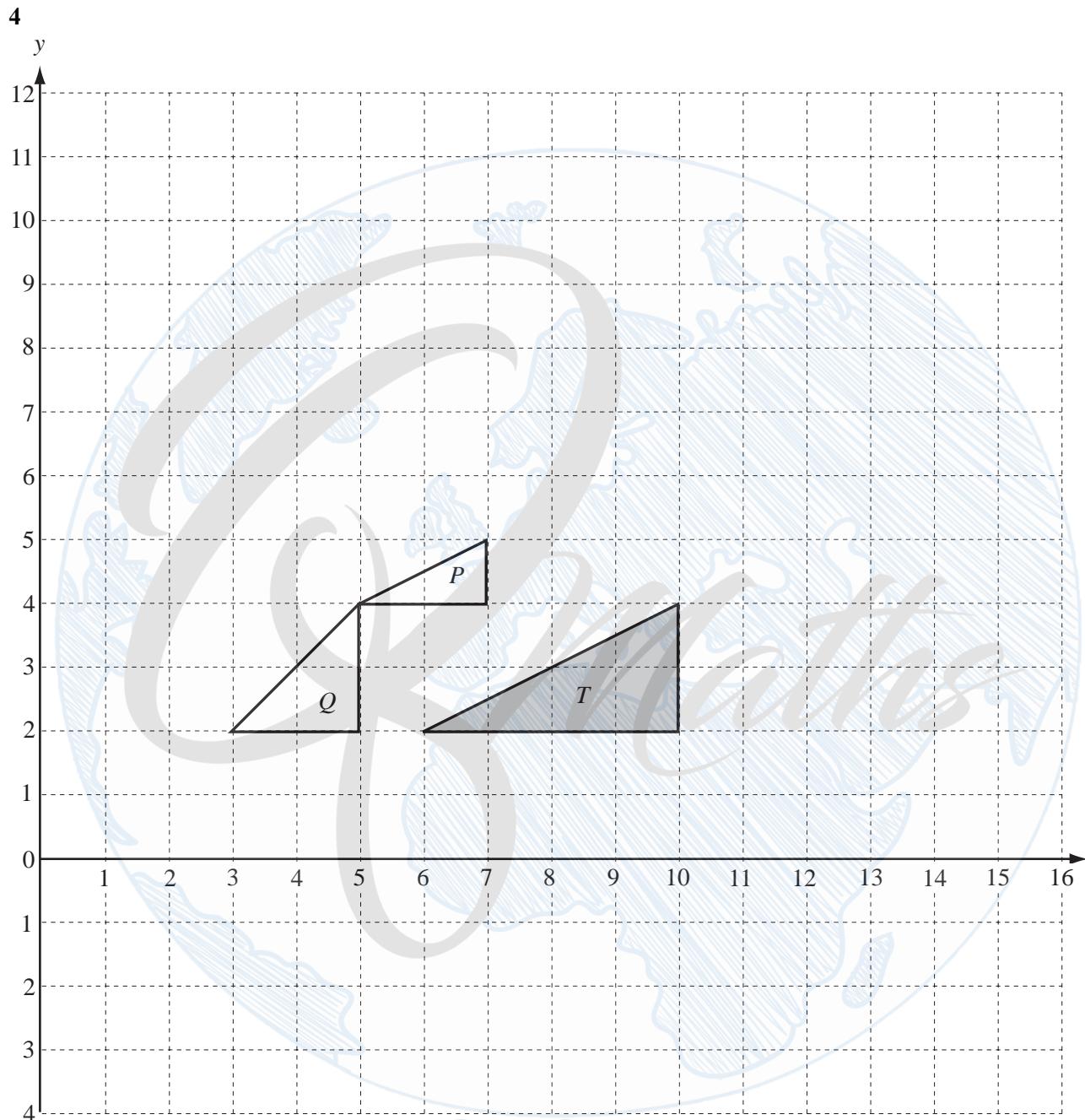
*Answer(c)(i)*  $\left( \begin{array}{c} \\ \\ \end{array} \right)$  [2]

(ii) triangle  $T$  onto triangle  $V$ ,

*Answer(c)(ii)*  $\left( \begin{array}{c} \\ \\ \end{array} \right)$  [2]

(iii) triangle  $V$  onto triangle  $T$ .

*Answer(c)(iii)*  $\left( \begin{array}{c} \\ \\ \end{array} \right)$  [1]



- (a) Draw the reflection of triangle  $T$  in the line  $y = 6$ .

Label the image  $A$ .

[2]

- (b) Draw the translation of triangle  $T$  by the vector  $\begin{pmatrix} 4 \\ 6 \end{pmatrix}$ .

Label the image  $B$ .

[2]

- (c) Describe fully the **single** transformation which maps triangle  $B$  onto triangle  $T$ .

*Answer(c)* ..... [2]

- (d) (i) Describe fully the **single** transformation which maps triangle  $T$  onto triangle  $P$ .

*Answer(d)(i)* ..... [3]

- (ii) Complete the following statement.

Area of triangle  $P$  = .....  $\times$  Area of triangle  $T$  [1]

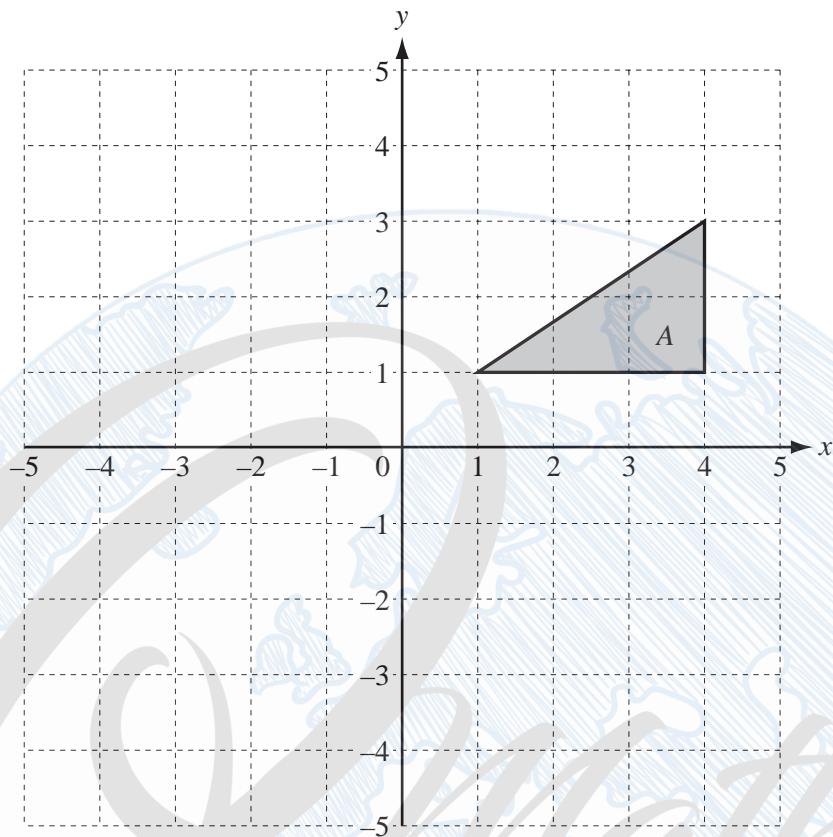
- (e) (i) Describe fully the **single** transformation which maps triangle  $T$  onto triangle  $Q$ .

*Answer(e)(i)* ..... [3]

- (ii) Find the 2 by 2 matrix which represents the transformation mapping triangle  $T$  onto triangle  $Q$ .

*Answer(e)(ii)*  $\begin{pmatrix} & \\ & \end{pmatrix}$  [2]

2 (a)



- (i) Draw the image when triangle  $A$  is reflected in the line  $y = 0$ .  
Label the image  $B$ . [2]
- (ii) Draw the image when triangle  $A$  is rotated through  $90^\circ$  anticlockwise about the origin.  
Label the image  $C$ . [2]
- (iii) Describe fully the **single** transformation which maps triangle  $B$  onto triangle  $C$ .

*Answer(a)(iii)* ..... [2]

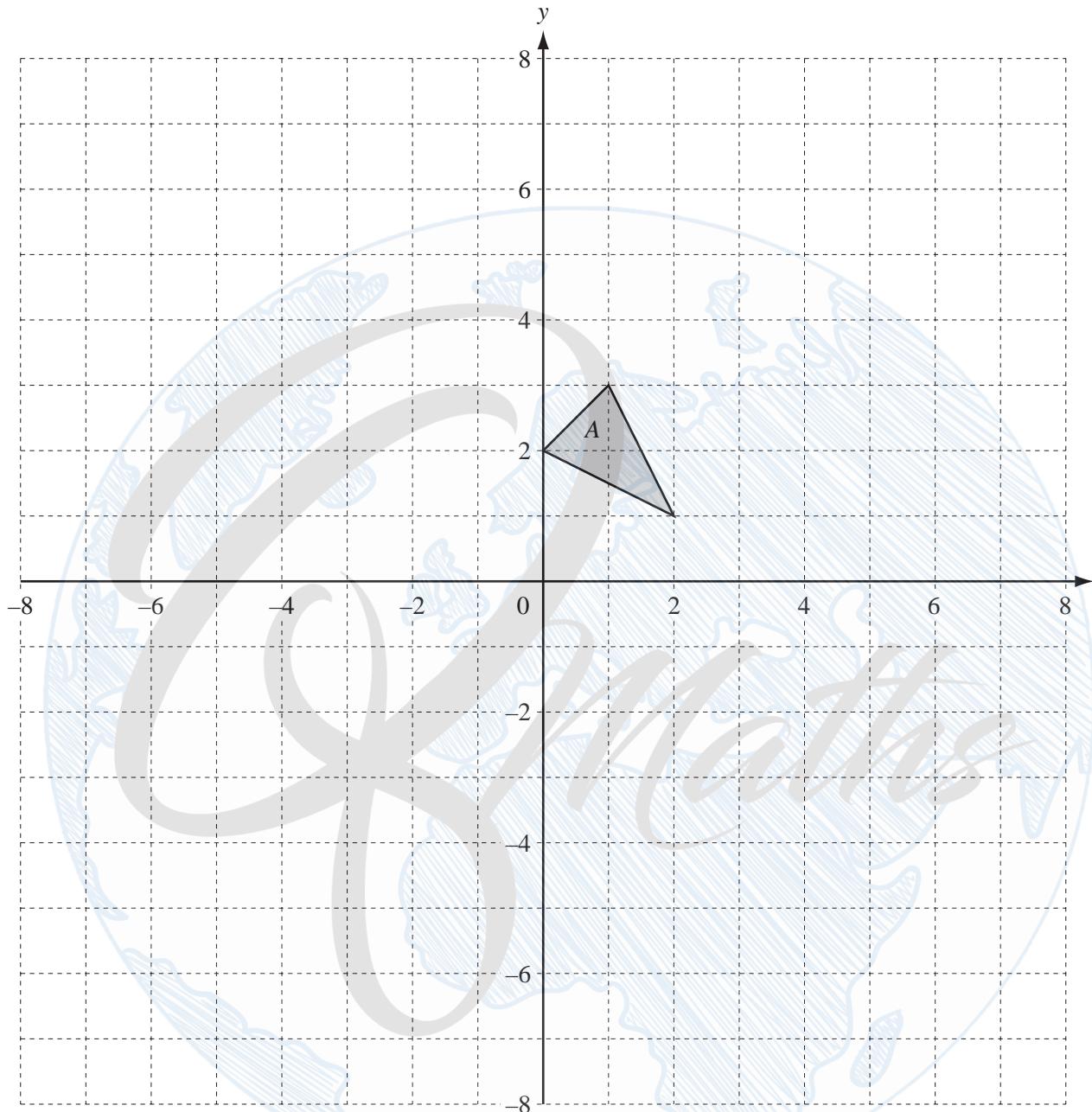
- (b) Rotation through  $90^\circ$  anticlockwise about the origin is represented by the matrix  $\mathbf{M} = \begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$ .
- (i) Find  $\mathbf{M}^{-1}$ , the inverse of matrix  $\mathbf{M}$ .

*Answer(b)(i)  $\mathbf{M}^{-1} = \begin{pmatrix} & \\ & \end{pmatrix}$*  [2]

- (ii) Describe fully the **single** transformation represented by the matrix  $\mathbf{M}^{-1}$ .

*Answer(b)(ii)* ..... [2]

8 (a)



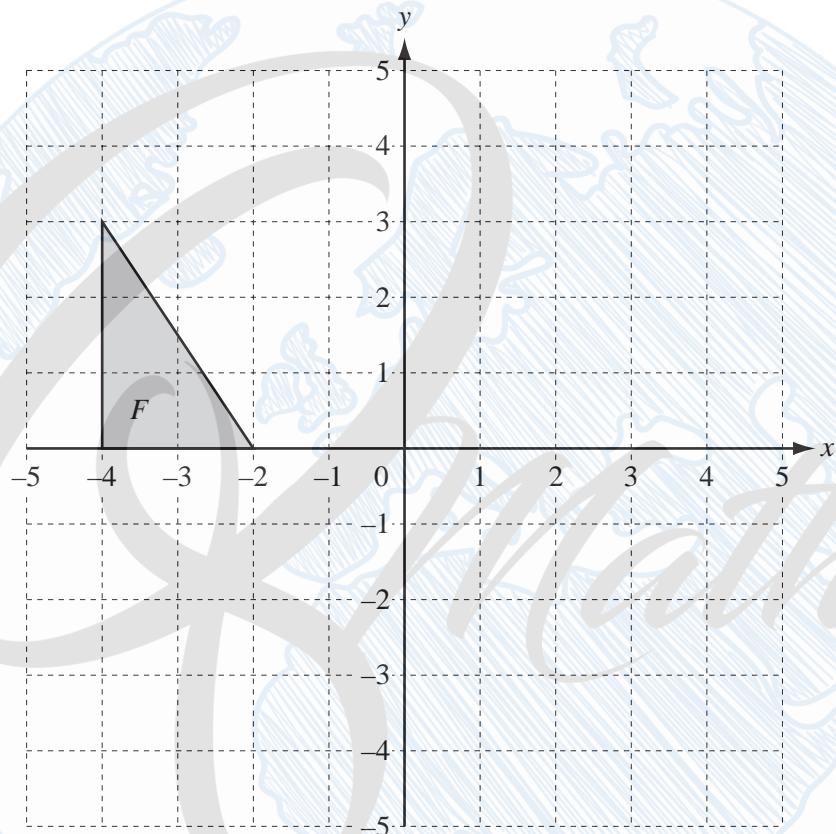
Draw the images of the following transformations on the grid above.

- (i) Translation of triangle  $A$  by the vector  $\begin{pmatrix} 3 \\ -7 \end{pmatrix}$ . Label the image  $B$ . [2]
- (ii) Reflection of triangle  $A$  in the line  $x = 3$ . Label the image  $C$ . [2]
- (iii) Rotation of triangle  $A$  through  $90^\circ$  anticlockwise around the point  $(0, 0)$ . Label the image  $D$ . [2]
- (iv) Enlargement of triangle  $A$  by scale factor  $-4$ , with centre  $(0, 1)$ . Label the image  $E$ . [2]

- (b) The area of triangle  $E$  is  $k \times$  area of triangle  $A$ .  
Write down the value of  $k$ .

*Answer(b)*  $k = \dots$  [1]

(c)



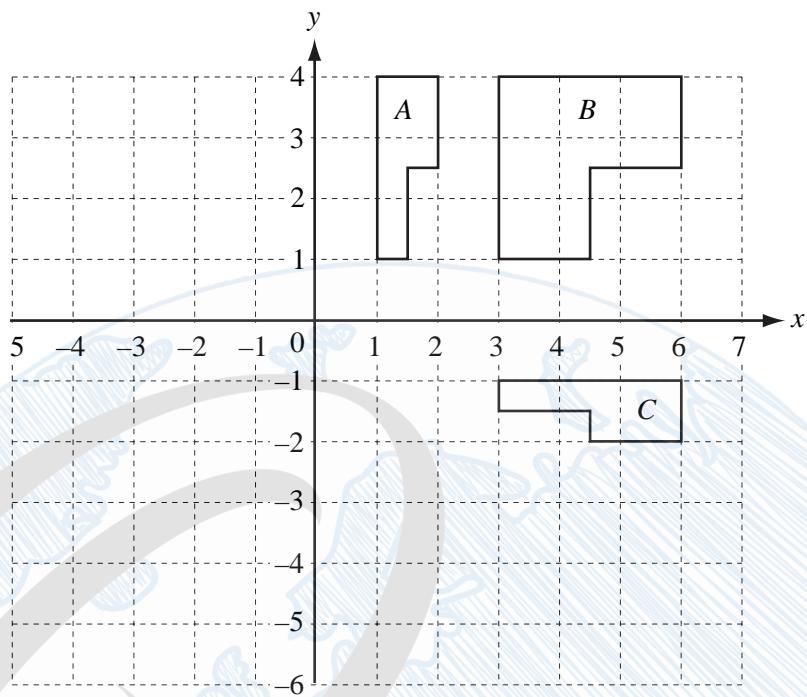
- (i) Draw the image of triangle  $F$  under the transformation represented by the matrix  $\mathbf{M} = \begin{pmatrix} 1 & 3 \\ 0 & 1 \end{pmatrix}$ . [3]
- (ii) Describe fully this single transformation.

*Answer(c)(ii)*  $\dots$  [3]

- (iii) Find  $\mathbf{M}^{-1}$ , the inverse of the matrix  $\mathbf{M}$ .

*Answer(c)(iii)*  $\left( \begin{array}{c} \quad \\ \quad \end{array} \right)$  [2]

5



(a) On the grid above, draw the image of

(i) shape  $A$  after translation by the vector  $\begin{pmatrix} 3 \\ 2 \end{pmatrix}$ ,

[2]

(ii) shape  $A$  after reflection in the line  $x = -1$ .

[2]

(b) Describe fully the **single** transformation which maps(i) shape  $A$  onto shape  $B$ ,

Answer(b)(i) ..... [3]

(ii) shape  $A$  onto shape  $C$ .

Answer(b)(ii) ..... [3]

(c) Find the matrix representing the transformation which maps shape  $A$  onto shape  $B$ .

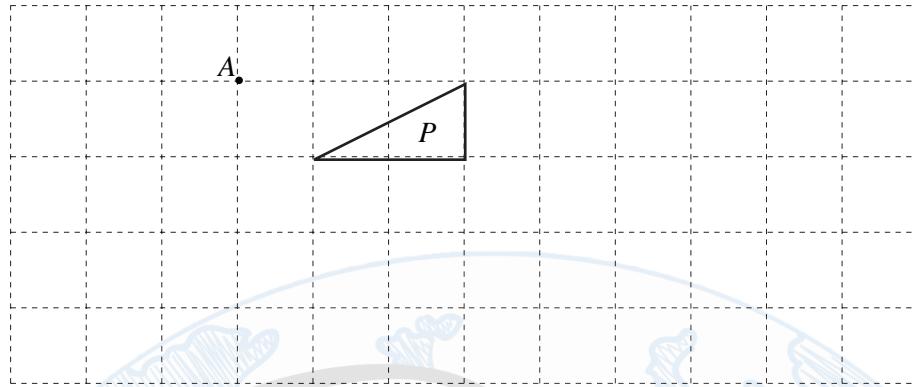
$$\text{Answer(c)} \begin{pmatrix} & \\ & \end{pmatrix}$$

[2]

(d) Describe fully the **single** transformation represented by the matrix  $\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$ 

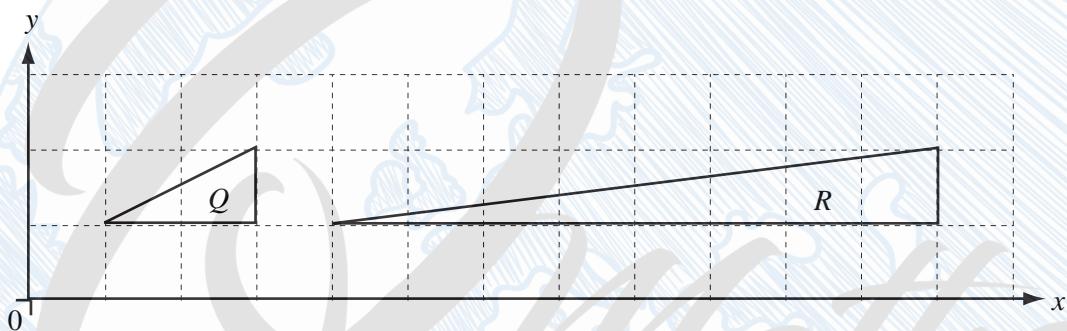
Answer(d) ..... [3]

8 (a)

Draw the enlargement of triangle  $P$  with centre  $A$  and scale factor 2.

[2]

(b)



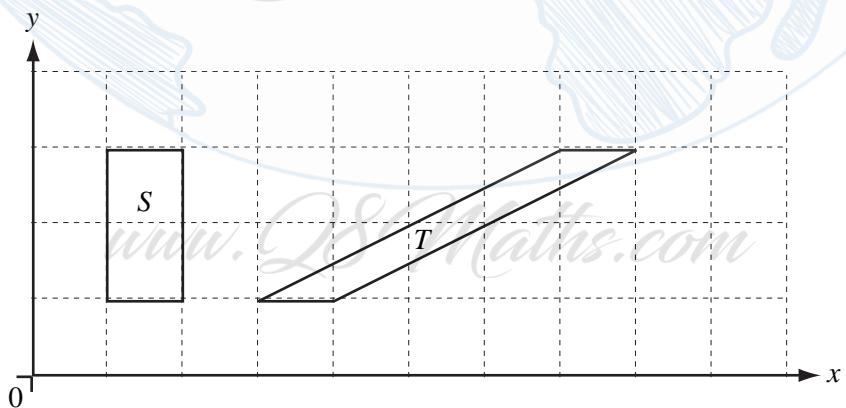
- (i) Describe fully the **single** transformation which maps shape  $Q$  onto shape  $R$ .

*Answer(b)(i)* ..... [3]

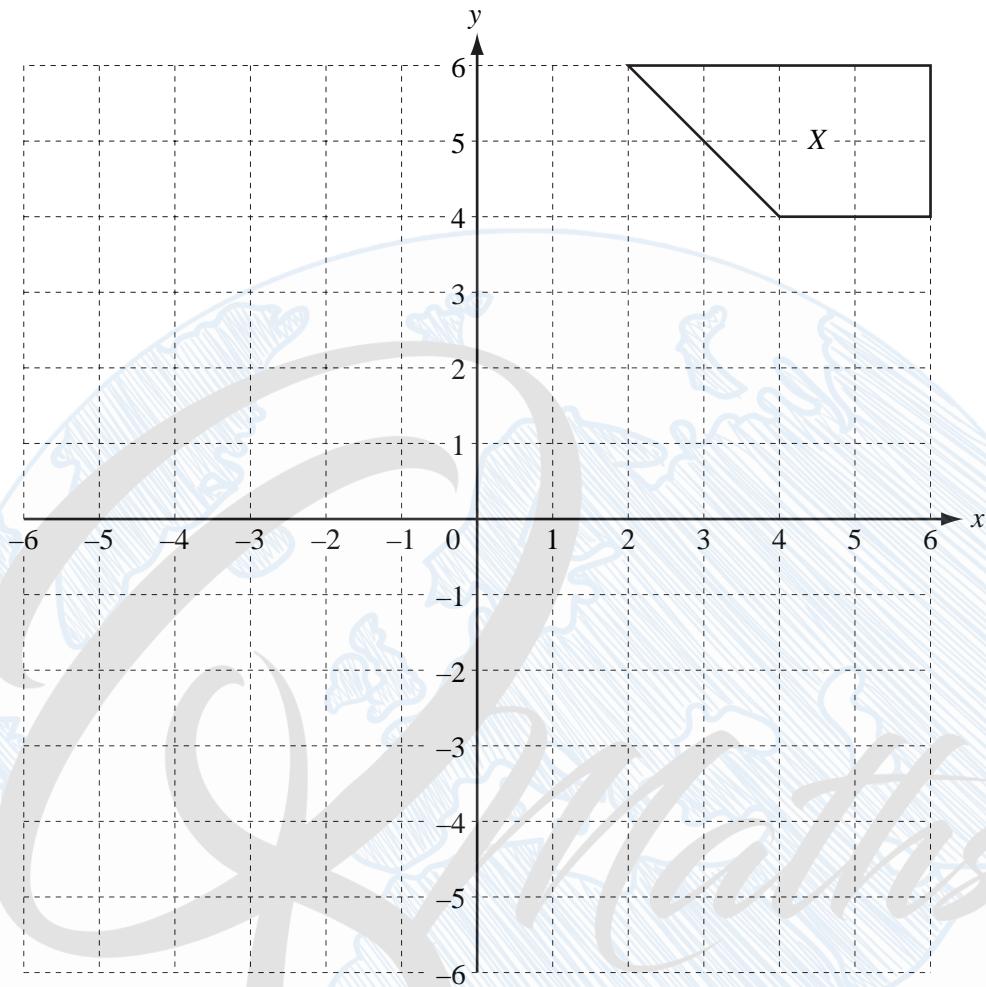
- (ii) Find the matrix which represents this transformation.

*Answer(b)(ii)*  $\left( \begin{array}{c} \\ \end{array} \right)$  [2]

(c)

Describe fully the **single** transformation which maps shape  $S$  onto shape  $T$ .

*Answer(c)* ..... [3]



- (a) (i) Draw the reflection of shape  $X$  in the  $x$ -axis. Label the image  $Y$ . [2]
- (ii) Draw the rotation of shape  $Y$ ,  $90^\circ$  clockwise about  $(0, 0)$ . Label the image  $Z$ . [2]
- (iii) Describe fully the **single** transformation that maps shape  $Z$  onto shape  $X$ .

*Answer(a)(iii)* ..... [2]

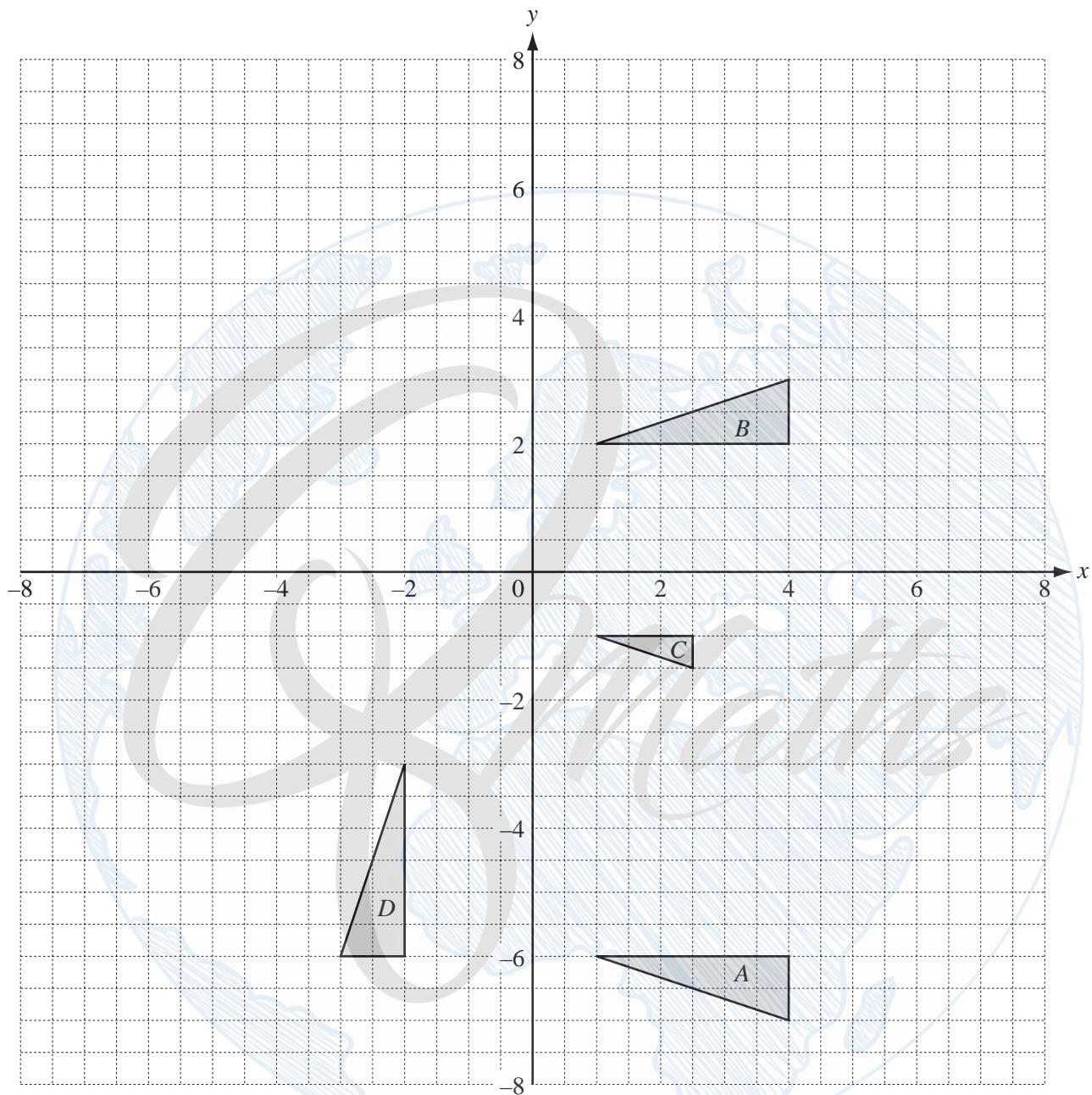
- (b) (i) Draw the enlargement of shape  $X$ , centre  $(0, 0)$ , scale factor  $\frac{1}{2}$ . [2]
- (ii) Find the matrix which represents an enlargement, centre  $(0, 0)$ , scale factor  $\frac{1}{2}$ .

*Answer(b)(ii)*  $\begin{pmatrix} & \\ & \end{pmatrix}$  [2]

- (c) (i) Draw the shear of shape  $X$  with the  $x$ -axis invariant and shear factor  $-1$ . [2]
- (ii) Find the matrix which represents a shear with the  $x$ -axis invariant and shear factor  $-1$ .

*Answer(c)(ii)*  $\begin{pmatrix} & \\ & \end{pmatrix}$  [2]

7



- (a) Describe fully the **single** transformation which maps

- (i) triangle A onto triangle B,

*Answer(a)(i)* ..... [2]

- (ii) triangle A onto triangle C,

*Answer(a)(ii)* ..... [3]

- (iii) triangle A onto triangle D.

*Answer(a)(iii)* ..... [3]

**(b)** Draw the image of

(i) triangle  $B$  after a translation of  $\begin{pmatrix} -5 \\ 2 \end{pmatrix}$ , [2]

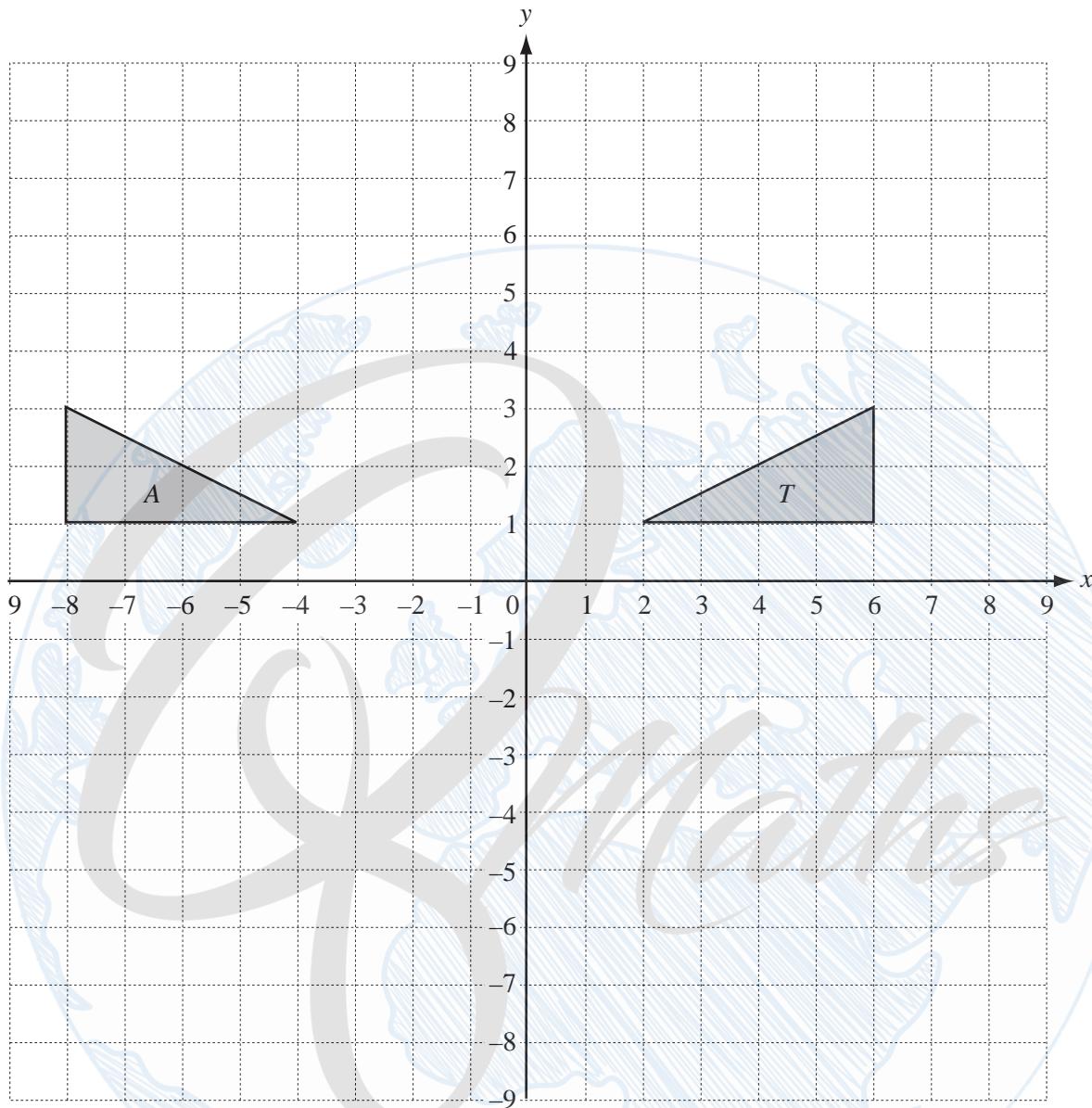
(ii) triangle  $B$  after a transformation by the matrix  $\begin{pmatrix} 1 & 0 \\ 0 & 2 \end{pmatrix}$ . [3]

**(c)** Describe fully the **single** transformation represented by the matrix  $\begin{pmatrix} 1 & 0 \\ 0 & 2 \end{pmatrix}$ .

Answer(c)

.....  
..... [3]

3



Triangles  $T$  and  $A$  are drawn on the grid above.

- (a) Describe fully the **single** transformation that maps triangle  $T$  onto triangle  $A$ .

*Answer(a)* ..... [2]

- (b) (i) Draw the image of triangle  $T$  after a rotation of  $90^\circ$  anticlockwise about the point  $(0,0)$ .

Label the image  $B$ . [2]

- (ii) Draw the image of triangle  $T$  after a reflection in the line  $x + y = 0$ .

Label the image  $C$ . [2]

- (iii) Draw the image of triangle  $T$  after an enlargement with centre  $(4, 5)$  and scale factor 1.5.

Label the image  $D$ . [2]

- (c) (i) Triangle  $T$  has its vertices at co-ordinates  $(2, 1)$ ,  $(6, 1)$  and  $(6, 3)$ .

Transform triangle  $T$  by the matrix  $\begin{pmatrix} 1 & 0 \\ 1 & 1 \end{pmatrix}$ .

Draw this image on the grid and label it  $E$ .

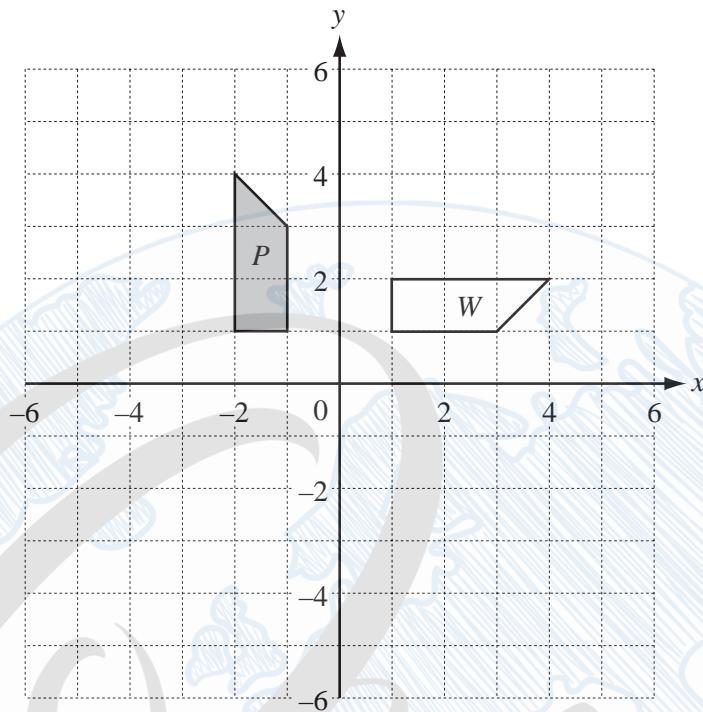
- (ii) Describe fully the **single** transformation represented by the matrix  $\begin{pmatrix} 1 & 0 \\ 1 & 1 \end{pmatrix}$ . [3]

Answer(c)(ii) ..... [3]

- (d) Write down the matrix that transforms triangle  $B$  onto triangle  $T$ .

$$\left( \quad \quad \right) \quad [2]$$

4



- (a) Draw the reflection of shape  $P$  in the line  $y = x$ . [2]
- (b) Draw the translation of shape  $P$  by the vector  $\begin{pmatrix} -2 \\ 1 \end{pmatrix}$ . [2]
- (c) (i) Describe fully the **single** transformation that maps shape  $P$  onto shape  $W$ .

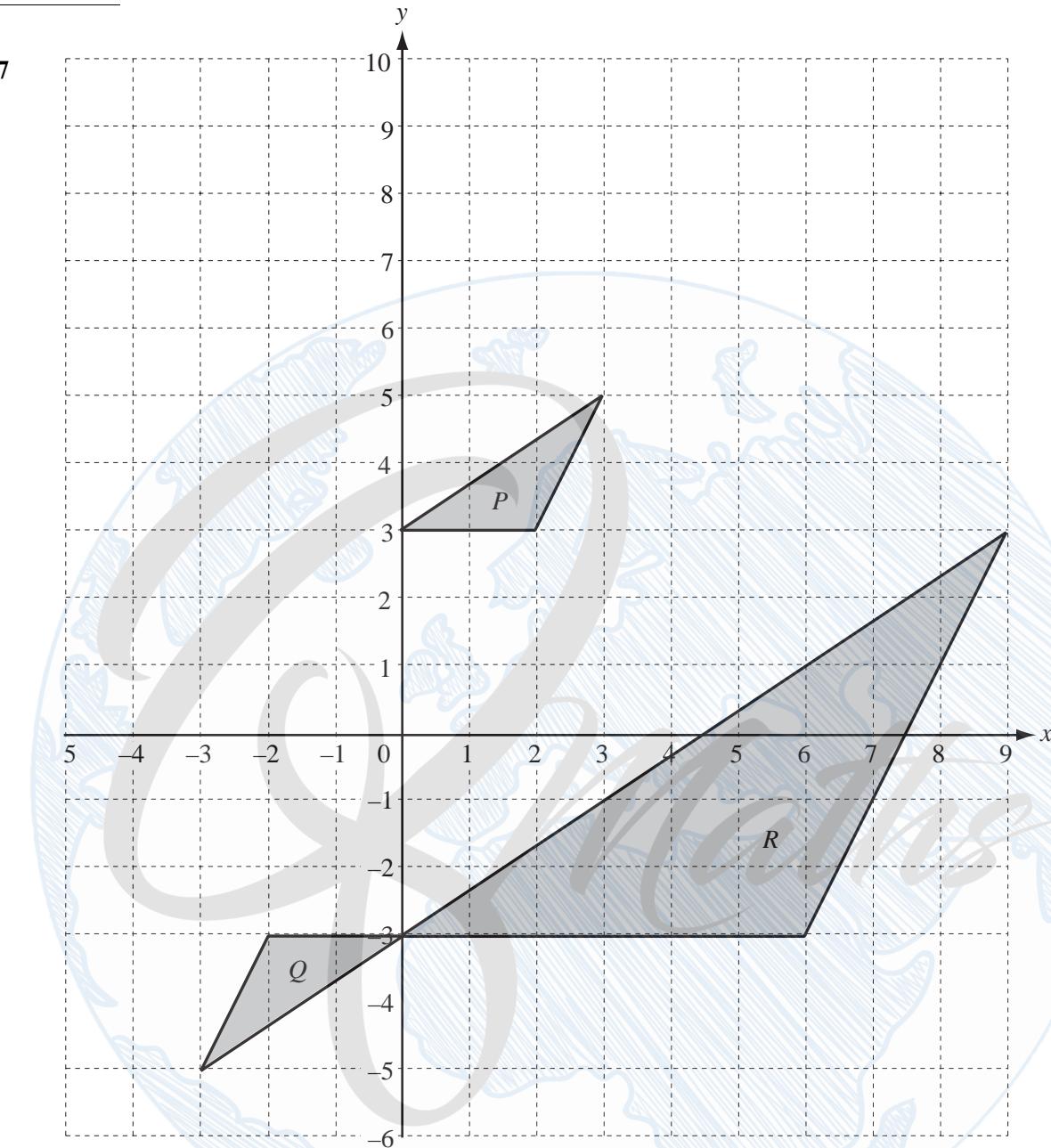
*Answer(c)(i)* ..... [3]

- (ii) Find the 2 by 2 matrix which represents this transformation.

*Answer(c)(ii)*  $\begin{pmatrix} & \\ & \end{pmatrix}$  [2]

- (d) Describe fully the **single** transformation represented by the matrix  $\begin{pmatrix} 1 & 0 \\ 0 & 2 \end{pmatrix}$ .

*Answer(d)* ..... [3]



(a) Describe fully

- (i) the **single** transformation which maps **triangle P** onto **triangle Q**,

*Answer(a)(i)* ..... [3]

- (ii) the **single** transformation which maps **triangle Q** onto **triangle R**,

*Answer(a)(ii)* ..... [3]

- (iii) the **single** transformation which maps **triangle R** onto **triangle P**.

*Answer(a)(iii)* ..... [3]

(b) On the grid, draw the image of

(i) triangle **P** after translation by  $\begin{pmatrix} -4 \\ -5 \end{pmatrix}$ , [2]

(ii) triangle **P** after reflection in the line  $x = -1$ . [2]

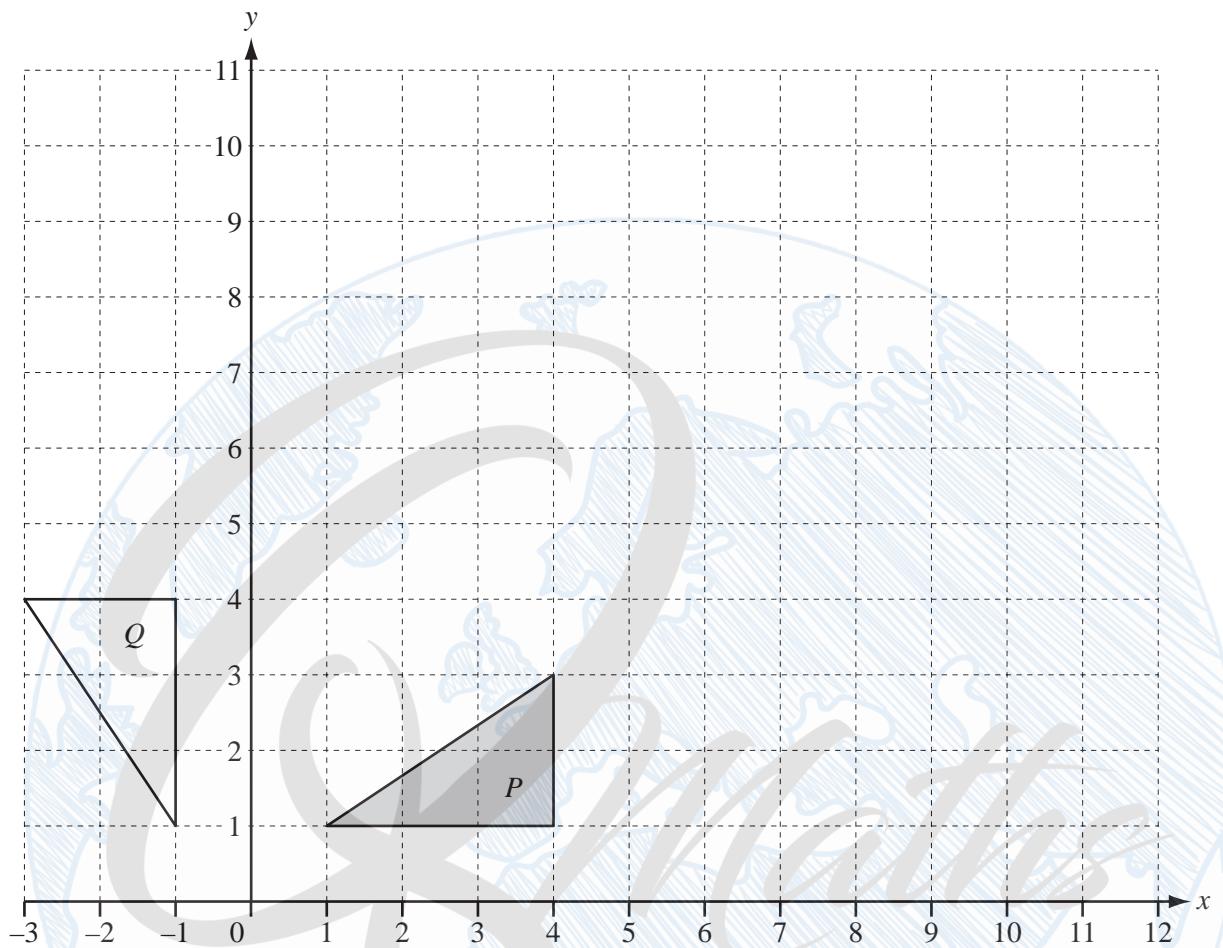
(c) (i) On the grid, draw the image of triangle **P** after a stretch, scale factor 2 and the  $y$ -axis as the invariant line. [2]

(ii) Find the matrix which represents this stretch.

Answer(c)(ii)

$$\left( \quad \quad \right) [2]$$

3



- (a) Draw the translation of triangle  $P$  by  $\begin{pmatrix} 5 \\ 3 \end{pmatrix}$ . [2]

- (b) Draw the reflection of triangle  $P$  in the line  $x = 6$ . [2]

- (c) (i) Describe fully the **single** transformation that maps triangle  $P$  onto triangle  $Q$ .

*Answer(c)(i)* ..... [3]

- (ii) Find the 2 by 2 matrix which represents the transformation in part(c)(i).

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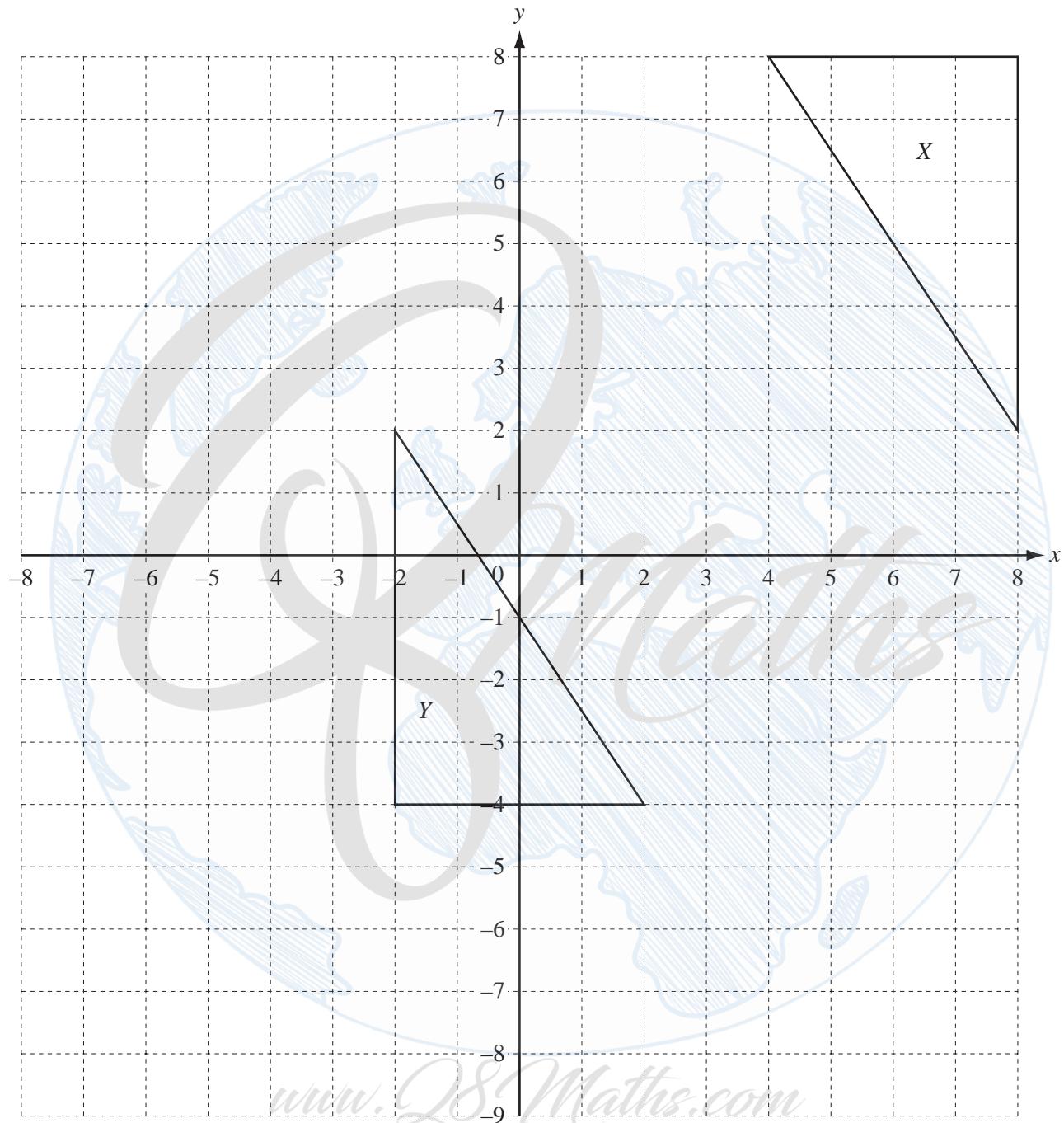
*Answer(c)(ii)*  $\begin{pmatrix} & \\ & \end{pmatrix}$  [2]

- (d) (i) Draw the stretch of triangle  $P$  with scale factor 3 and the  $x$ -axis as the invariant line. [2]

- (ii) Find the 2 by 2 matrix which represents a stretch, scale factor 3 and  $x$ -axis invariant.

*Answer(d)(ii)*  $\begin{pmatrix} & \\ & \end{pmatrix}$  [2]

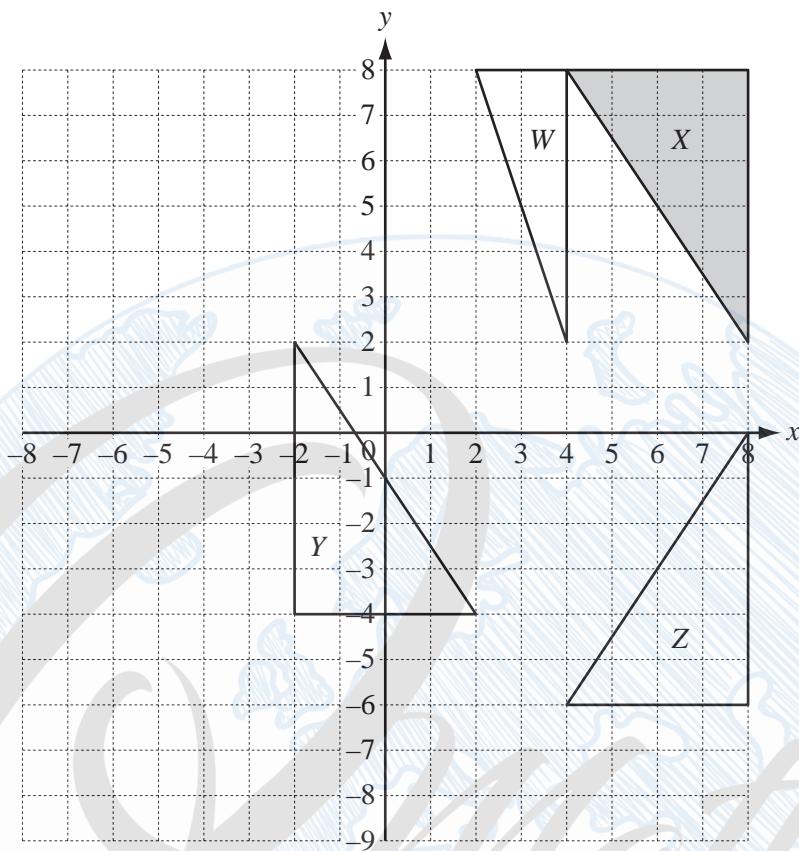
2 (a)



- (i) Draw the translation of triangle X by the vector  $\begin{pmatrix} -11 \\ -1 \end{pmatrix}$ . [2]

- (ii) Draw the enlargement of triangle Y with centre  $(-6, -4)$  and scale factor  $\frac{1}{2}$ . [2]

(b)



Describe fully the **single** transformation that maps

- (i) triangle X onto triangle Z,

*Answer(b)(i)* ..... [2]

- (ii) triangle X onto triangle Y,

*Answer(b)(ii)* ..... [3]

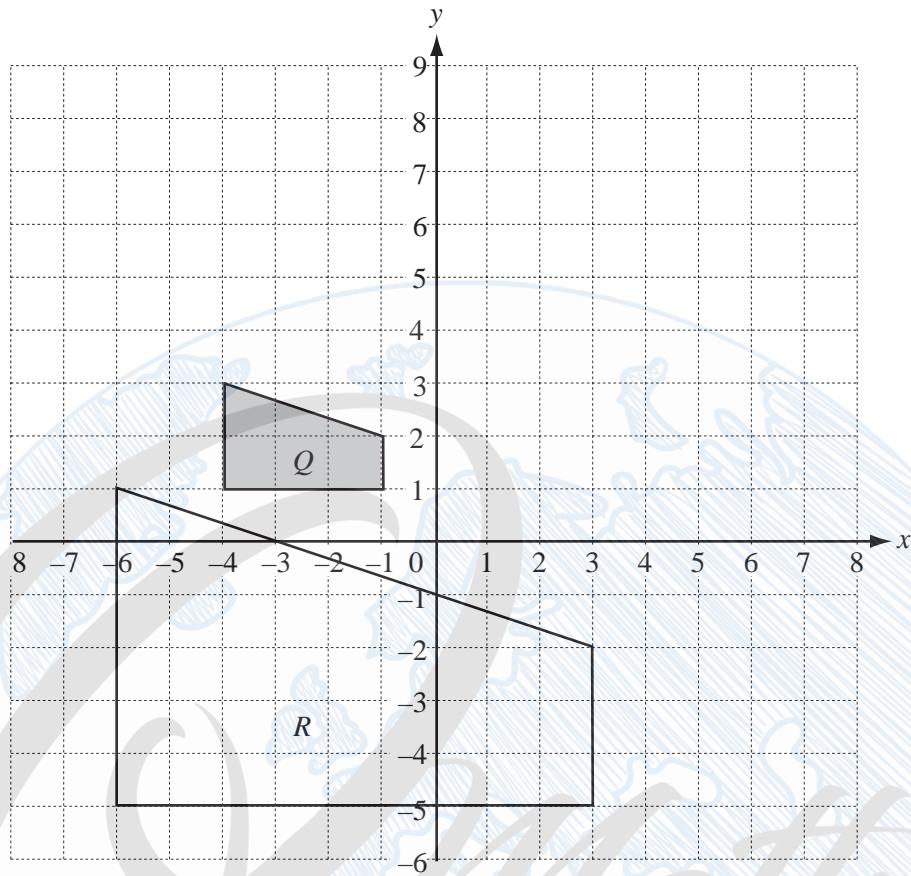
- (iii) triangle X onto triangle W.

*Answer(b)(iii)* ..... [3]

- (c) Find the matrix that represents the transformation in part (b)(iii).

*Answer(c)*  $\begin{pmatrix} & \\ & \end{pmatrix}$  [2]

4



- (a) Describe fully the **single** transformation that maps shape  $Q$  onto shape  $R$

*Answer(a)* ..... [3]

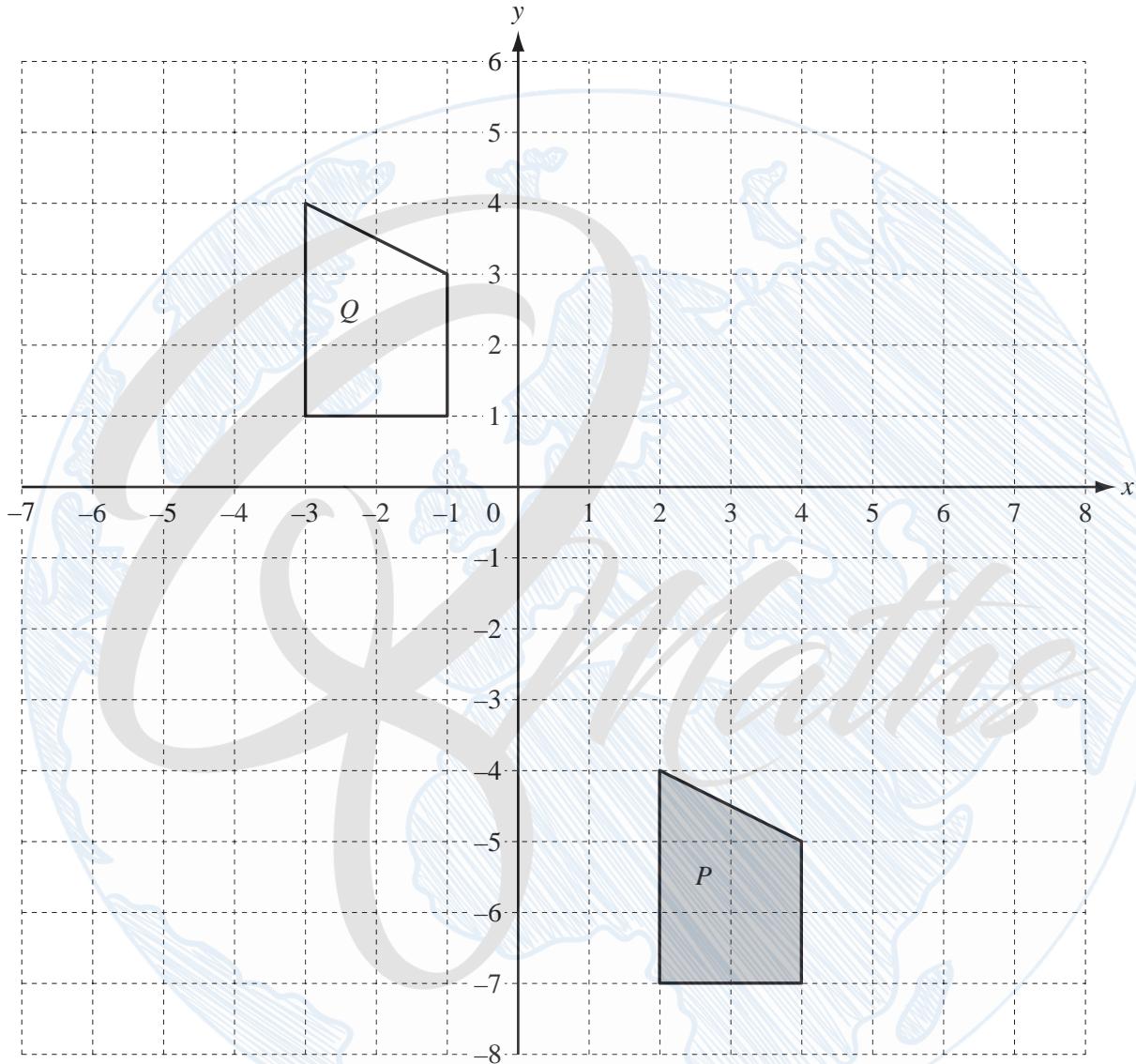
- (b) (i) Draw the image when shape  $Q$  is translated by the vector  $\begin{pmatrix} 5 \\ 4 \end{pmatrix}$ . [2]
- (ii) Draw the image when shape  $Q$  is reflected in the line  $x = 2$ . [2]
- (iii) Draw the image when shape  $Q$  is stretched, factor 3,  $x$ -axis invariant. [2]
- (iv) Find the  $2 \times 2$  matrix that represents a stretch of factor 3,  $x$ -axis invariant.

*Answer(b)(iv)*  $\begin{pmatrix} & \\ & \end{pmatrix}$  [2]

- (c) Describe fully the **single** transformation represented by the matrix  $\begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}$

*Answer(c)* ..... [2]

2 (a)

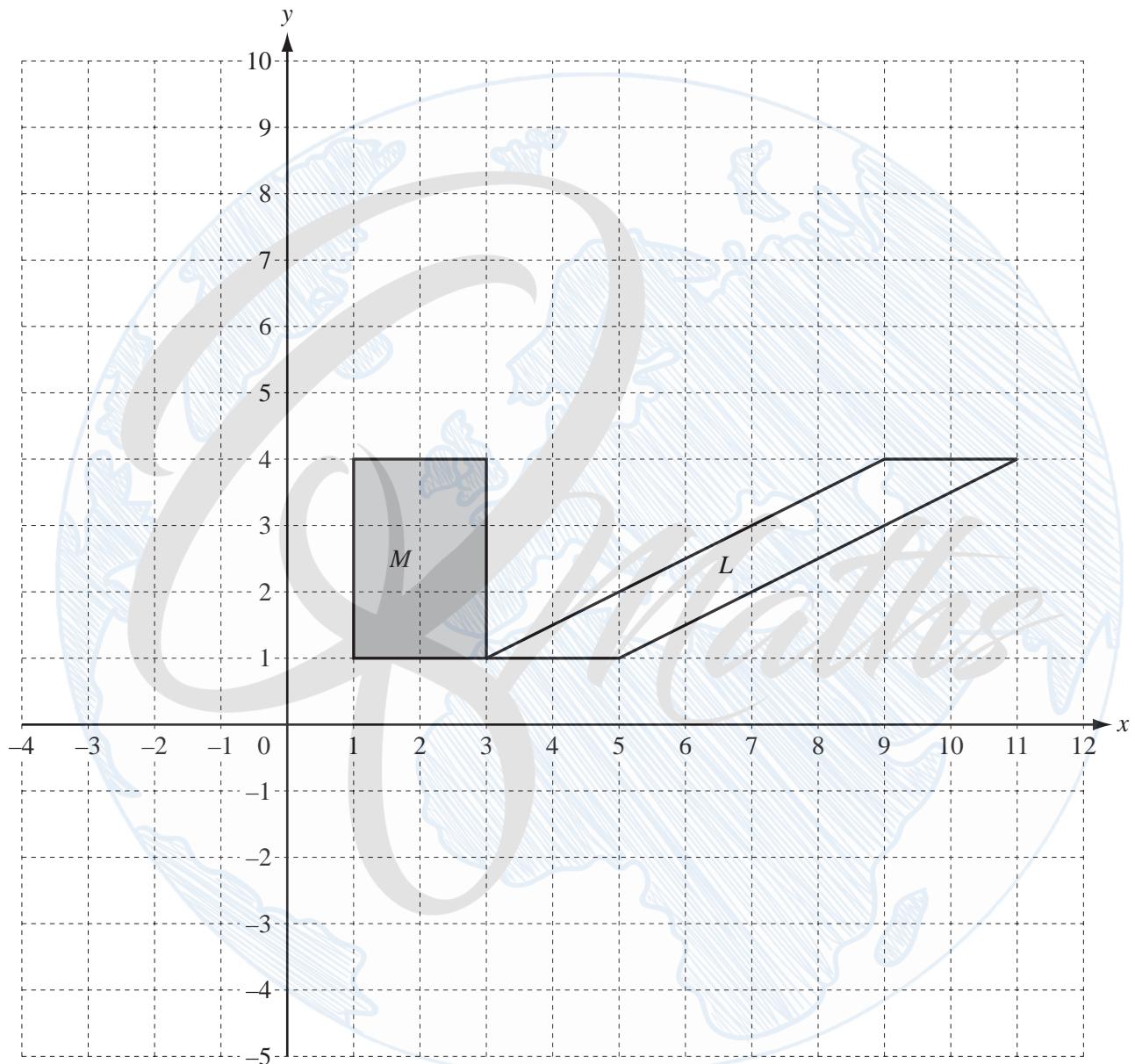


- (i) Describe fully the **single** transformation which maps shape  $P$  onto shape  $Q$ .

*Answer(a)(i) ..... [2]*

- (ii) On the grid above, draw the image of shape  $P$  after reflection in the line  $y = -1$ . [2]
- (iii) On the grid above, draw the image of shape  $P$  under the transformation represented by the matrix  $\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$ . [3]

(b)

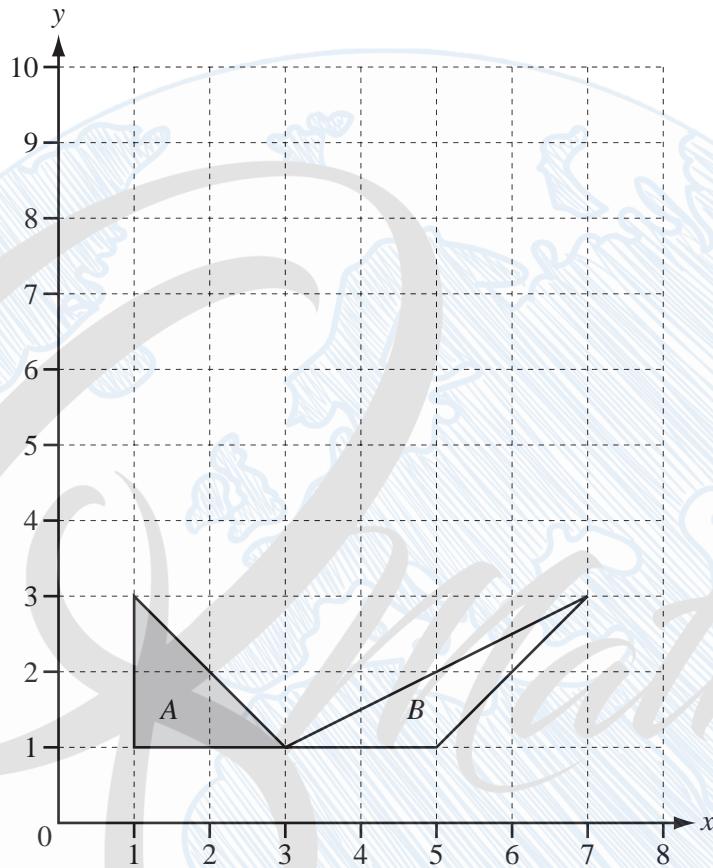


- (i) Describe fully the **single** transformation which maps shape  $M$  onto shape  $L$ .

Answer(b)(i) ..... [3]

- (ii) On the grid above, draw the image of shape  $M$  after enlargement by scale factor 2, centre  $(5, 0)$ . [2]

7



- (a) (i) Draw the image of shape A after a stretch, factor 3,  $x$ -axis invariant. [2]
- (ii) Write down the matrix representing a stretch, factor 3,  $x$ -axis invariant.

Answer(a)(ii)  $\begin{pmatrix} & \\ & \end{pmatrix}$  [2]

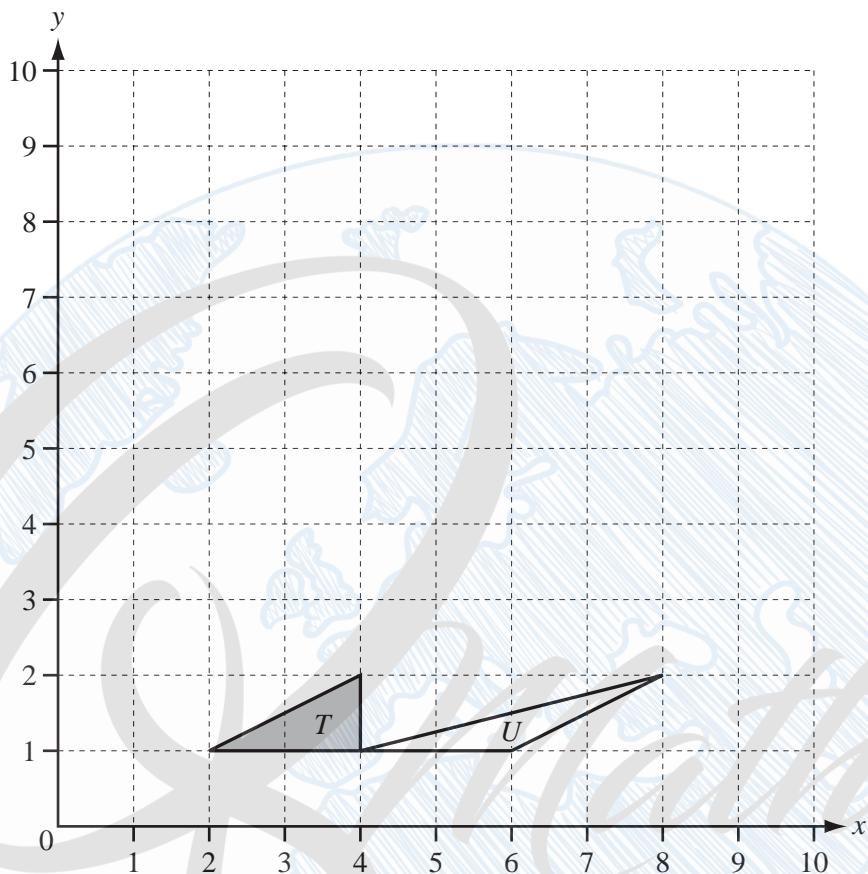
- (b) (i) Describe fully the **single** transformation which maps shape A onto shape B.

Answer(b)(i) ..... [3]

- (ii) Write down the matrix representing the transformation which maps shape A onto shape B.

Answer(b)(ii)  $\begin{pmatrix} & \\ & \end{pmatrix}$  [2]

5 (a)



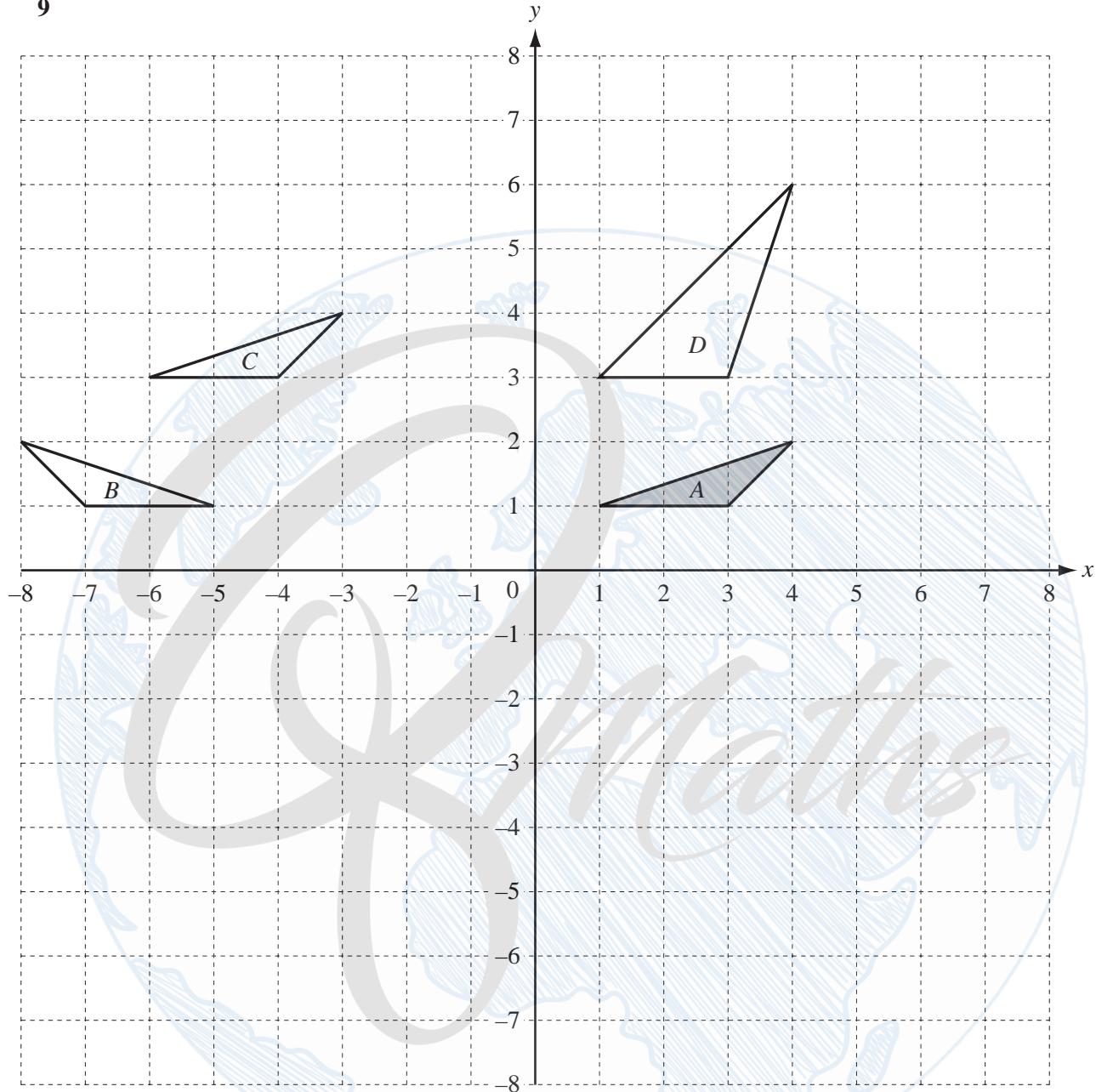
- (i) Draw the reflection of triangle  $T$  in the line  $y = 5$ . [2]
- (ii) Draw the rotation of triangle  $T$  about the point  $(4, 2)$  through  $180^\circ$ . [2]
- (iii) Describe fully the **single** transformation that maps triangle  $T$  onto triangle  $U$ .

*Answer(a)(iii) .....* [3]

- (iv) Find the  $2 \times 2$  matrix which represents the transformation in part (a)(iii).

*Answer(a)(iv)  $\begin{pmatrix} & \\ & \end{pmatrix}$*  [2]

9



- (a) Describe fully the **single** transformation that maps triangle A onto

- (i) triangle B,

*Answer(a)(i)* ..... [2]

- (ii) triangle C,

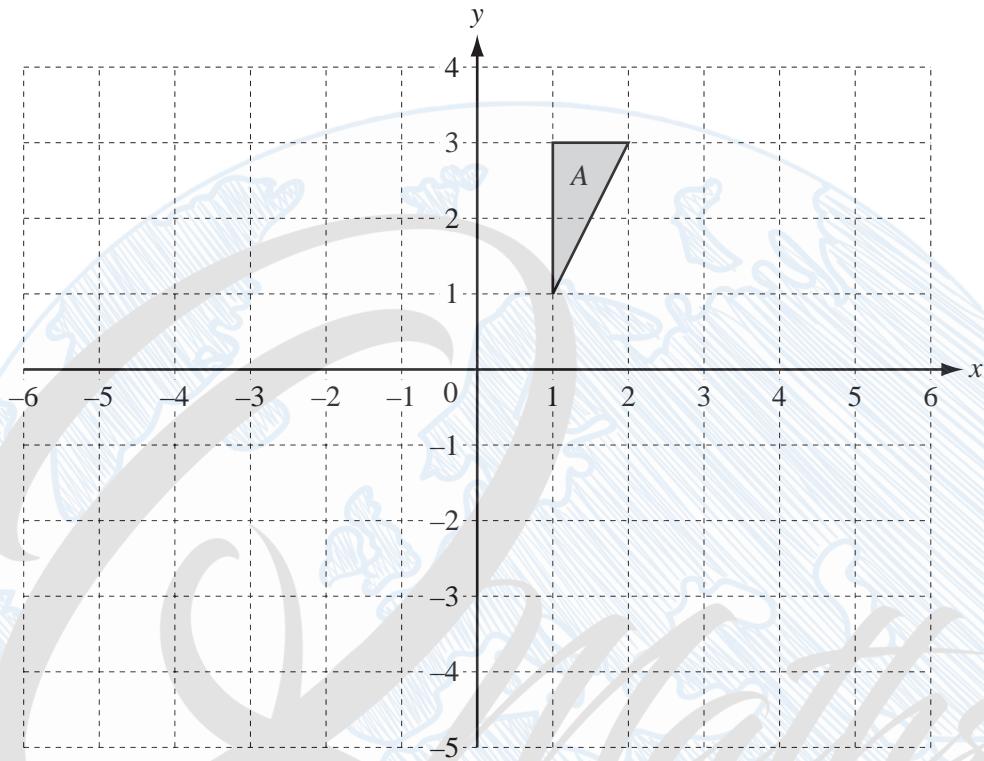
*Answer(a)(ii)* ..... [2]

- (iii) triangle D.

*Answer(a)(iii)* ..... [3]

- (b) On the grid, draw
- (i) the rotation of triangle A about (6, 0) through  $90^\circ$  clockwise, [2]
  - (ii) the enlargement of triangle A by scale factor  $-2$  with centre  $(0, -1)$ , [2]
  - (iii) the shear of triangle A by shear factor  $-2$  with the  $y$ -axis invariant. [2]
- (c) Find the matrix that represents the transformation in part (b)(iii).
- Answer(c)  $\left( \begin{array}{cc} & \\ & \end{array} \right)$  [2]

7



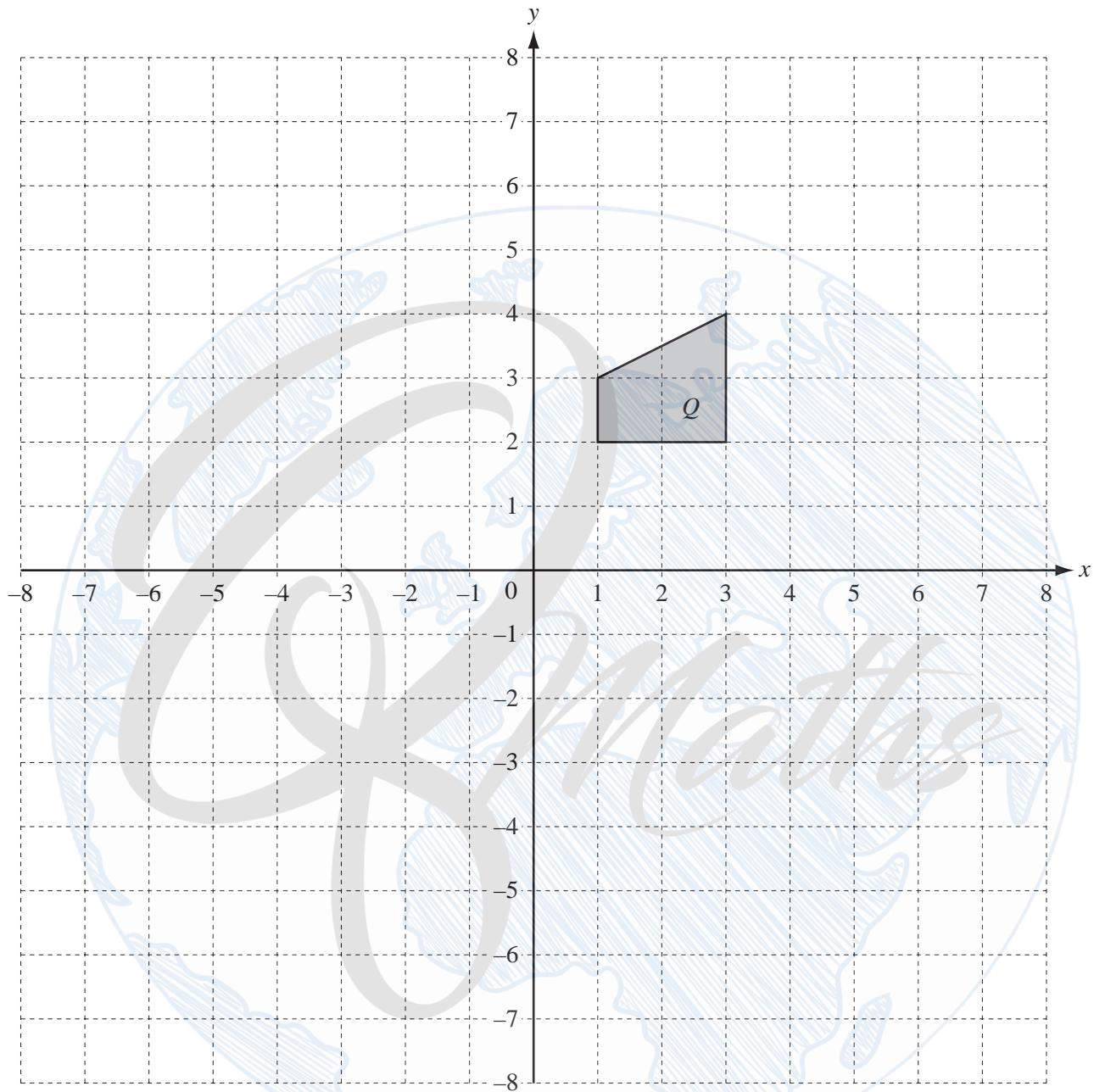
(a) On the grid,

(i) draw the image of shape A after a translation by the vector  $\begin{pmatrix} -5 \\ -4 \end{pmatrix}$ , [2](ii) draw the image of shape A after a rotation through  $90^\circ$  clockwise about the origin. [2](b) (i) On the grid, draw the image of shape A after the transformation represented by the matrix  $\begin{pmatrix} 2 & 0 \\ 0 & 1 \end{pmatrix}$ . [3](ii) Describe fully the **single** transformation represented by the matrix  $\begin{pmatrix} 2 & 0 \\ 0 & 1 \end{pmatrix}$ .

Answer(b)(ii) .....

..... [3]

4



- (a) Draw the reflection of shape  $Q$  in the line  $x = -1$ . [2]
- (b) (i) Draw the enlargement of shape  $Q$ , centre  $(0, 0)$ , scale factor  $-2$ . [2]
- (ii) Find the  $2 \times 2$  matrix that represents an enlargement, centre  $(0, 0)$ , scale factor  $-2$ .

Answer(b)(ii)  $\begin{pmatrix} & \\ & \end{pmatrix}$  [2]

(c) (i) Draw the stretch of shape  $Q$ , factor 2,  $x$ -axis invariant. [2]

(ii) Find the  $2 \times 2$  matrix that represents a stretch, factor 2,  $x$ -axis invariant.

Answer(c)(ii)  $\begin{pmatrix} & \\ & \end{pmatrix}$  [2]

(iii) Find the inverse of the matrix in **part (c)(ii)**.

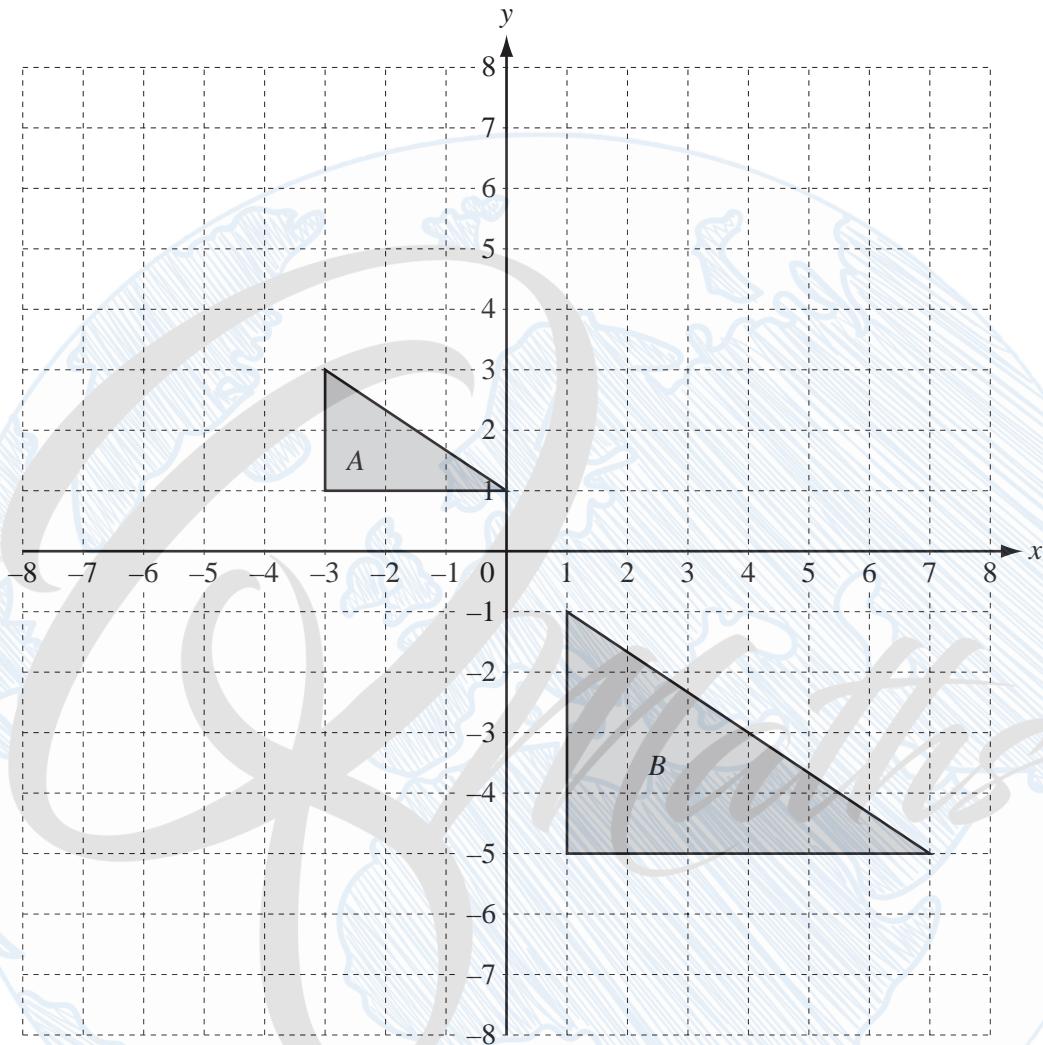
Answer(c)(iii)  $\begin{pmatrix} & \\ & \end{pmatrix}$  [2]

(iv) Describe fully the **single** transformation represented by the matrix in **part (c)(iii)**.

Answer(c)(iv) .....

[3]

3



- (a) Draw the image when triangle A is reflected in the line  $x = 0$ . [1]

- (b) Draw the image when triangle A is rotated through  $90^\circ$  anticlockwise about  $(-4, 0)$ . [2]

- (c) (i) Describe fully the **single** transformation that maps triangle A onto triangle B.

Answer(c)(i) .....

..... [3]

- (ii) Complete the following statement.

Area of triangle A : Area of triangle B = ..... : ..... [2]

- (d) Write down the matrix that represents a stretch, factor 4 with the  $y$ -axis invariant.

Answer(d)  $\begin{pmatrix} & \\ & \end{pmatrix}$  [2]

- (e) (i) On the grid, draw the image of triangle  $A$  after the transformation represented by the matrix  $\begin{pmatrix} 1 & 0 \\ 2 & 1 \end{pmatrix}$ .

[3]

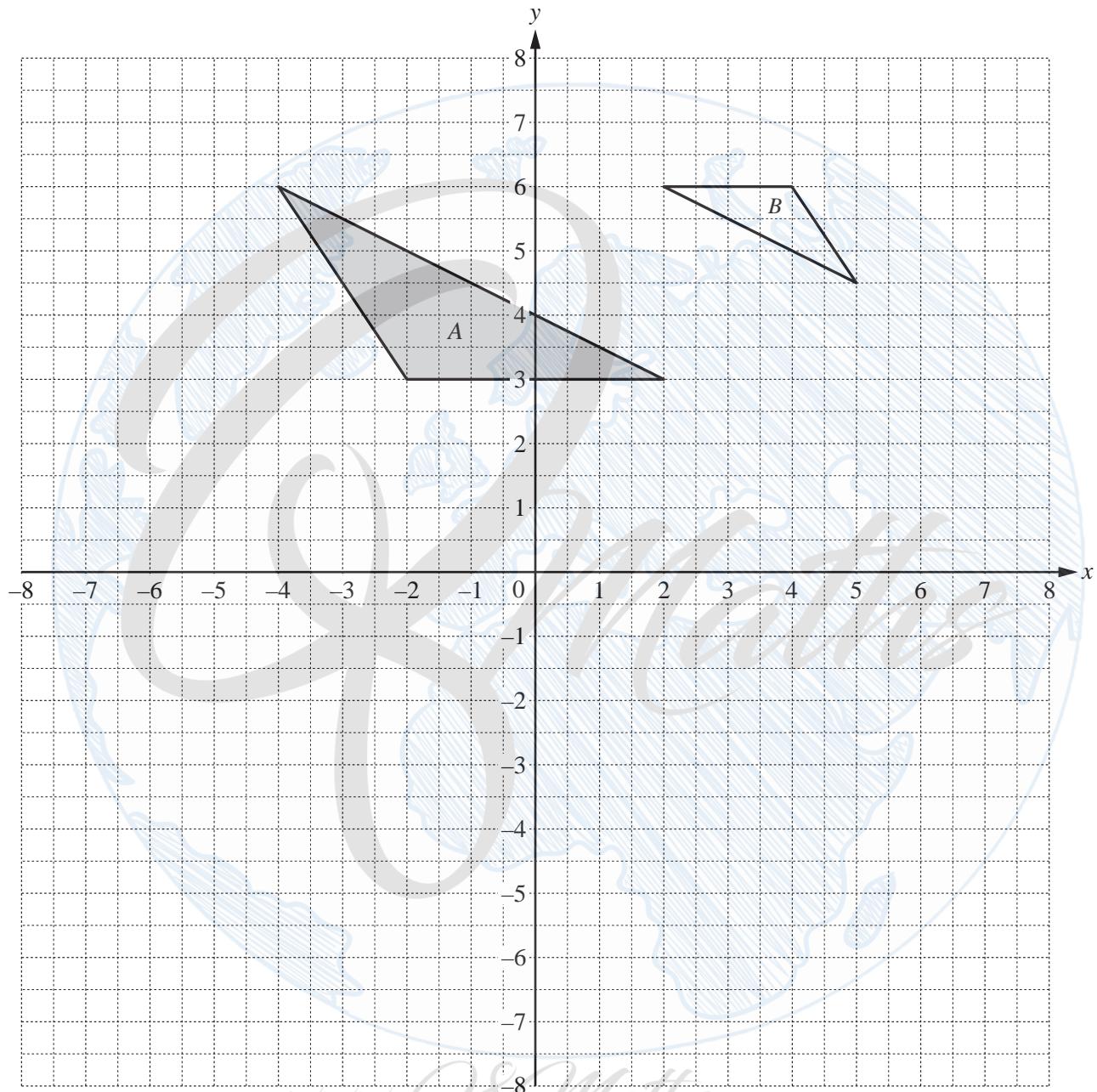
- (ii) Describe fully this **single** transformation.

Answer(e)(ii) .....  
..... [3]

- (iii) Find the inverse of the matrix  $\begin{pmatrix} 1 & 0 \\ 2 & 1 \end{pmatrix}$ .

Answer(e)(iii)  $\begin{pmatrix} & \\ & \end{pmatrix}$  [2]

4



- (a) Describe fully the **single** transformation that maps triangle A onto triangle B.

Answer(a) .....

..... [3]

(b) On the grid, draw the image of

(i) triangle A after a reflection in the line  $x = -3$ , [2]

(ii) triangle A after a rotation about the origin through  $270^\circ$  anticlockwise, [2]

(iii) triangle A after a translation by the vector  $\begin{pmatrix} -1 \\ -5 \end{pmatrix}$ . [2]

(c) M is the matrix that represents the transformation in part (b)(ii).

(i) Find M.

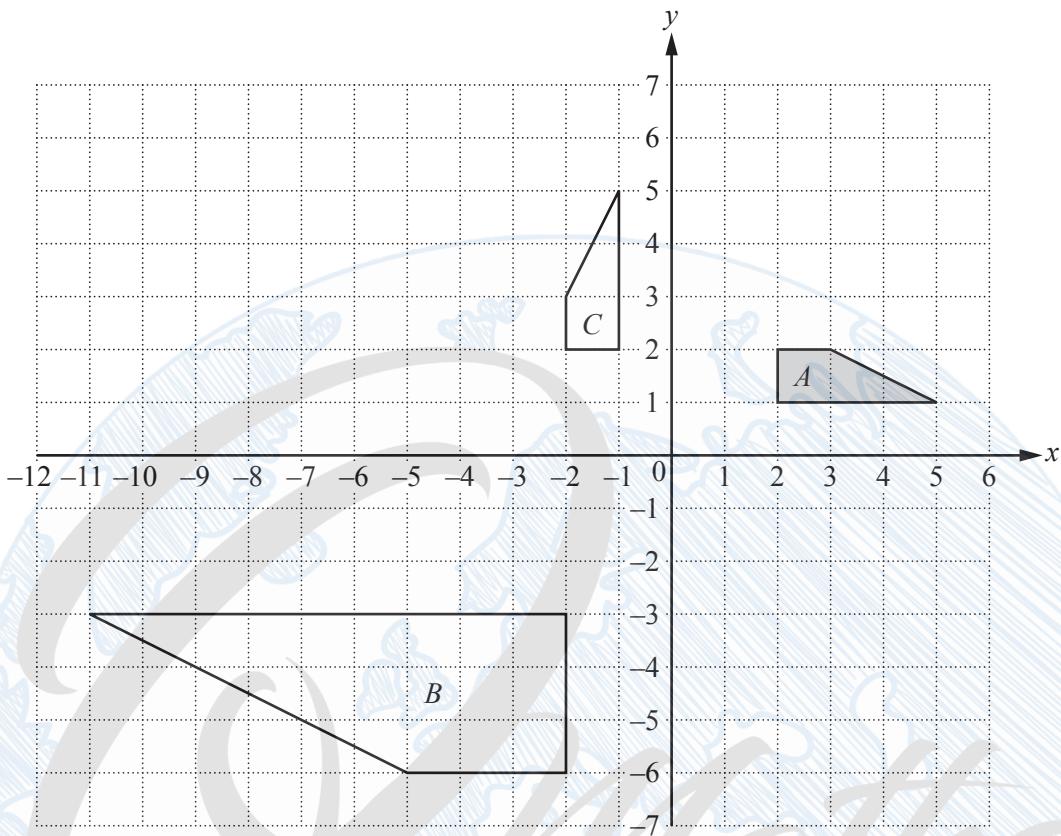
Answer(c)(i)  $M = \begin{pmatrix} \quad & \quad \\ \quad & \quad \end{pmatrix}$  [2]

(ii) Describe fully the **single** transformation represented by  $M^{-1}$ , the inverse of M.

Answer(c)(ii) .....

..... [2]

3



- (a) Draw the image of

(i) shape  $A$  after a translation by  $\begin{pmatrix} -1 \\ 3 \end{pmatrix}$ ,

[2]

(ii) shape  $A$  after a rotation through  $180^\circ$  about the point  $(0, 0)$ ,

[2]

(iii) shape  $A$  after the transformation represented by the matrix  $\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$ .

[3]

- (b) Describe fully the **single** transformation that maps shape  $A$  onto shape  $B$ .

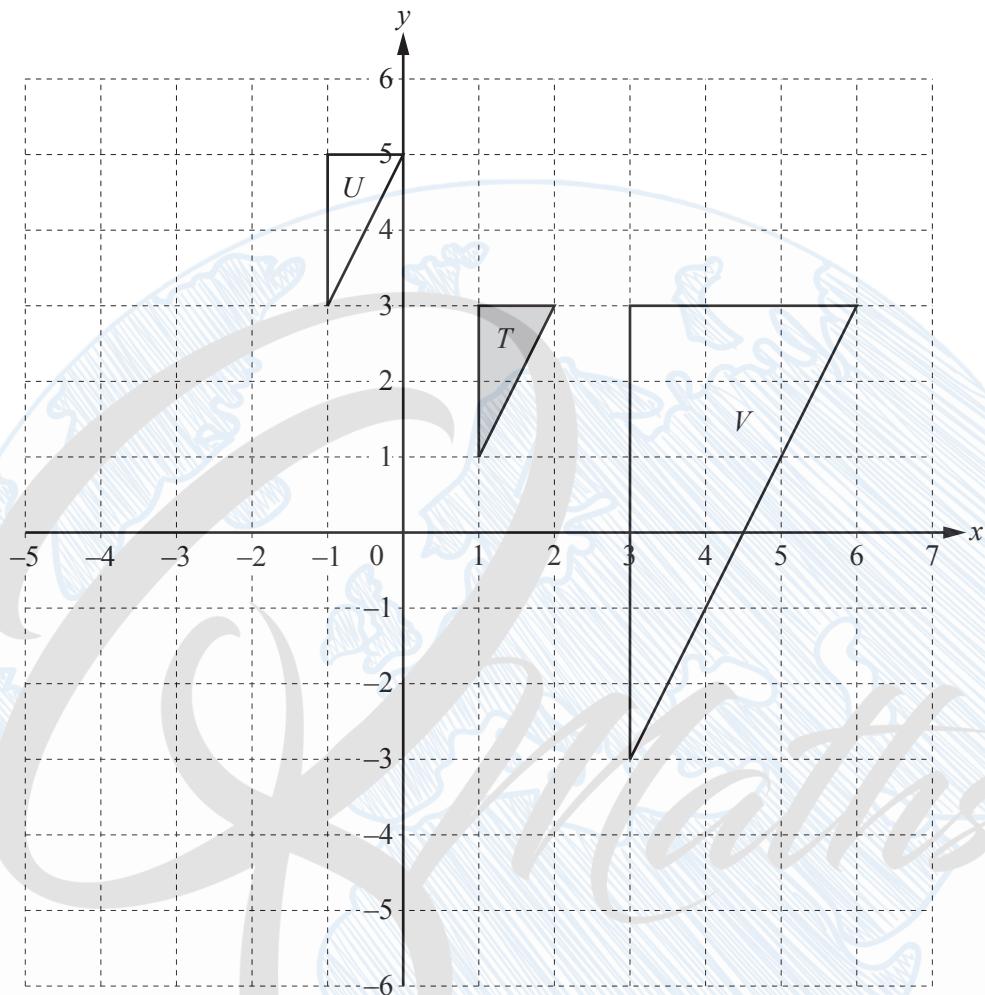
*Answer(b)* .....  
.....

[3]

- (c) Find the matrix which represents the transformation that maps shape  $A$  onto shape  $C$ .

*Answer(c)*  $\left( \quad \quad \right)$  [2]

1



- (a) On the grid, draw the image of

(i) triangle  $T$  after a reflection in the line  $x = -1$ ,

[2]

(ii) triangle  $T$  after a rotation through  $180^\circ$  about  $(0, 0)$ .

[2]

- (b) Describe fully the **single** transformation that maps

(i) triangle  $T$  onto triangle  $U$ ,

*Answer(b)(i) .....*

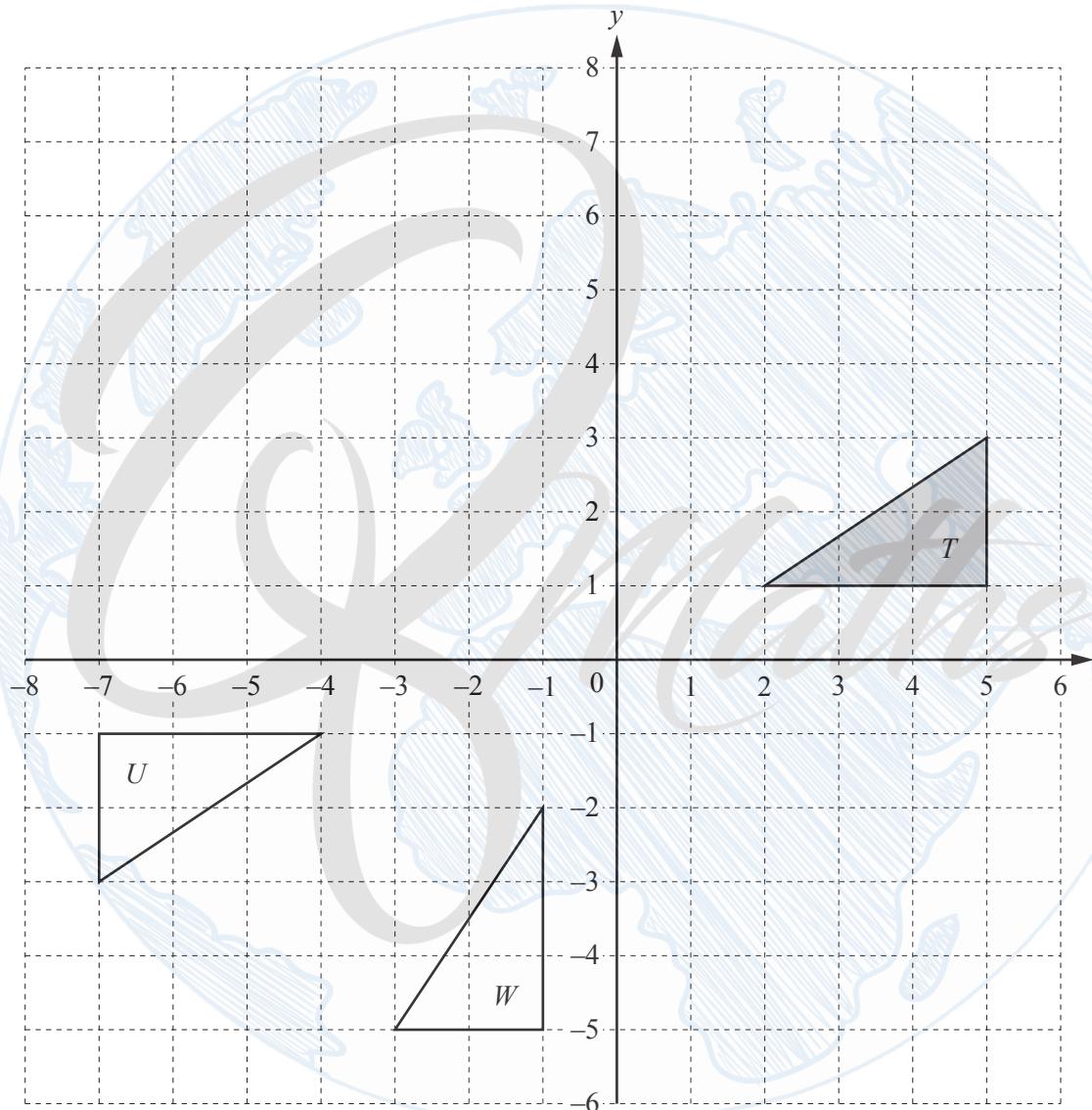
[2]

(ii) triangle  $T$  onto triangle  $V$ .

*Answer(b)(ii) .....*

[3]

2



(a) On the grid, draw the image of

(i) triangle T after a translation by the vector  $\begin{pmatrix} -4 \\ 4 \end{pmatrix}$ ,

[2]

(ii) triangle T after a reflection in the line  $y = -1$ .

[2]

- (b) Describe fully the **single** transformation that maps triangle  $T$  onto triangle  $U$ .

*Answer(b)* .....

[3]

- (c) (i) Describe fully the **single** transformation that maps triangle  $T$  onto triangle  $W$ .

*Answer(c)(i)* .....

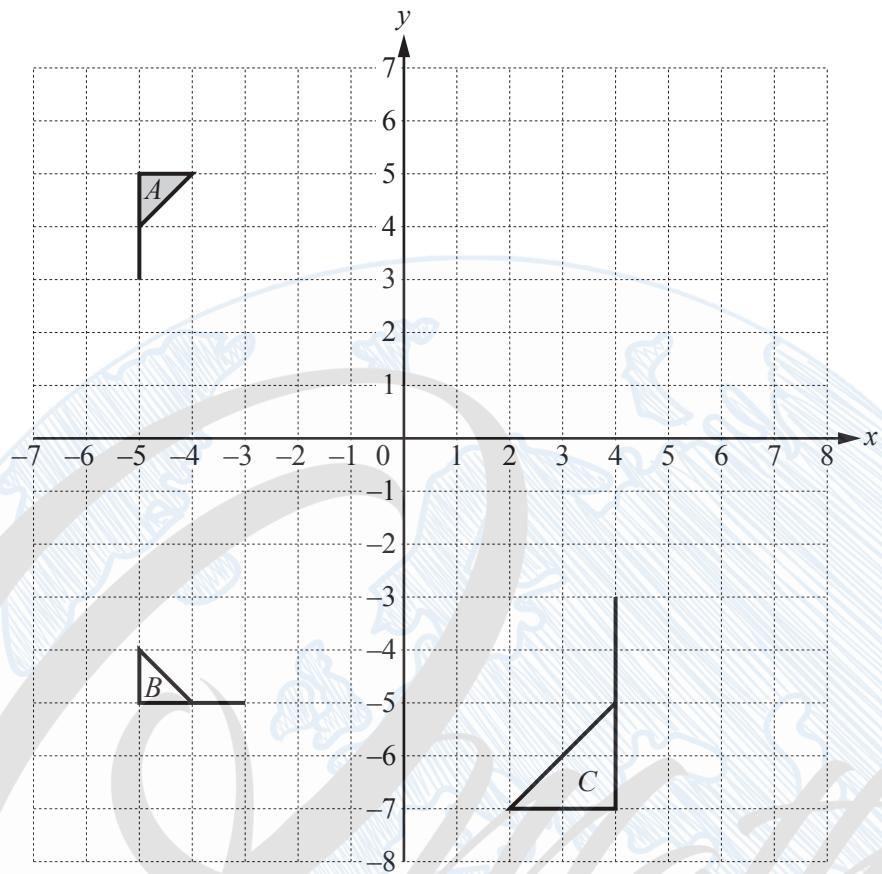
[2]

- (ii) Find the  $2 \times 2$  matrix that represents the transformation in part (c)(i).

*Answer(c)(ii)*  $\left( \begin{array}{cc} & \\ & \end{array} \right)$

[2]

7



- (a) Describe fully the **single** transformation that maps

- (i) flag A onto flag B,

*Answer(a)(i)* ..... [3]

- (ii) flag A onto flag C.

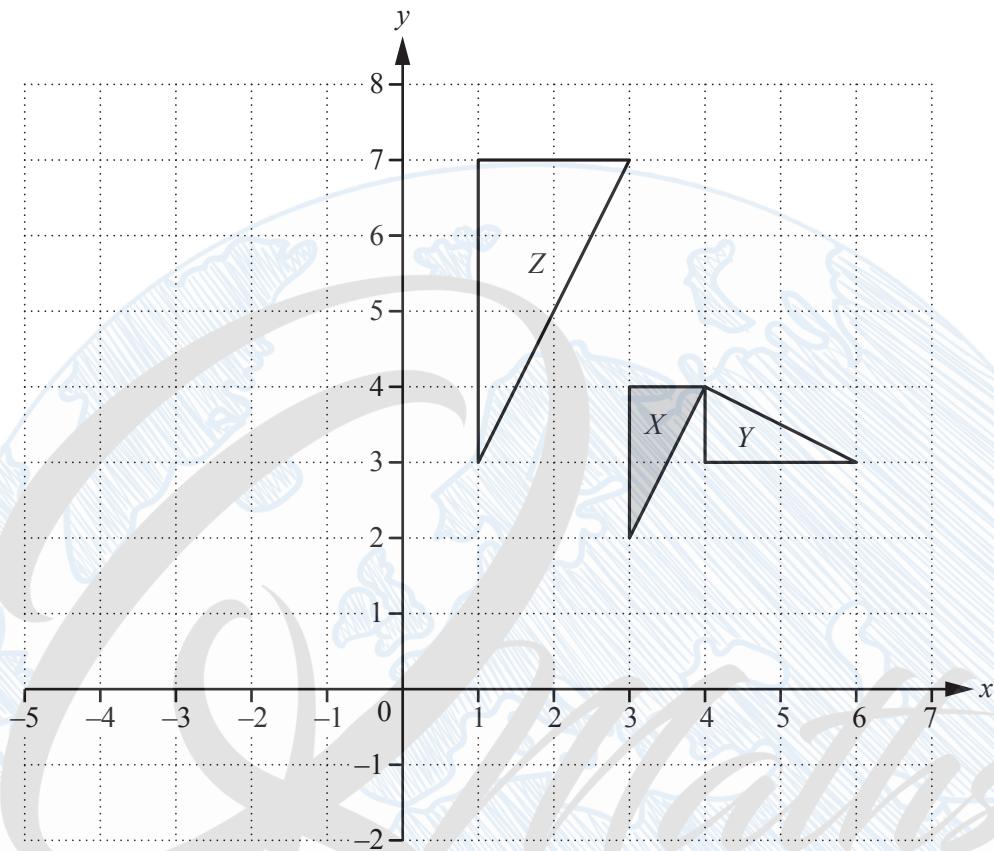
*Answer(a)(ii)* ..... [3]

- (b) Draw the image of flag A after a translation by the vector  $\begin{pmatrix} 2 \\ 1 \end{pmatrix}$ . [2]

- (c) Draw the image of flag A after a reflection in the line  $x = 1$ . [2]

- (d) Describe fully the **single** transformation represented by the matrix  $\begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix}$ .

*Answer(d)* ..... [2]



- (a) Describe fully the **single** transformation that maps

(i) triangle  $X$  onto triangle  $Y$ ,

[3]

(ii) triangle  $X$  onto triangle  $Z$ .

[3]

- (b) (i) Draw the image of triangle  $X$  after a translation by the vector  $\begin{pmatrix} -5 \\ 3 \end{pmatrix}$ .

Label this triangle  $P$ .

[2]

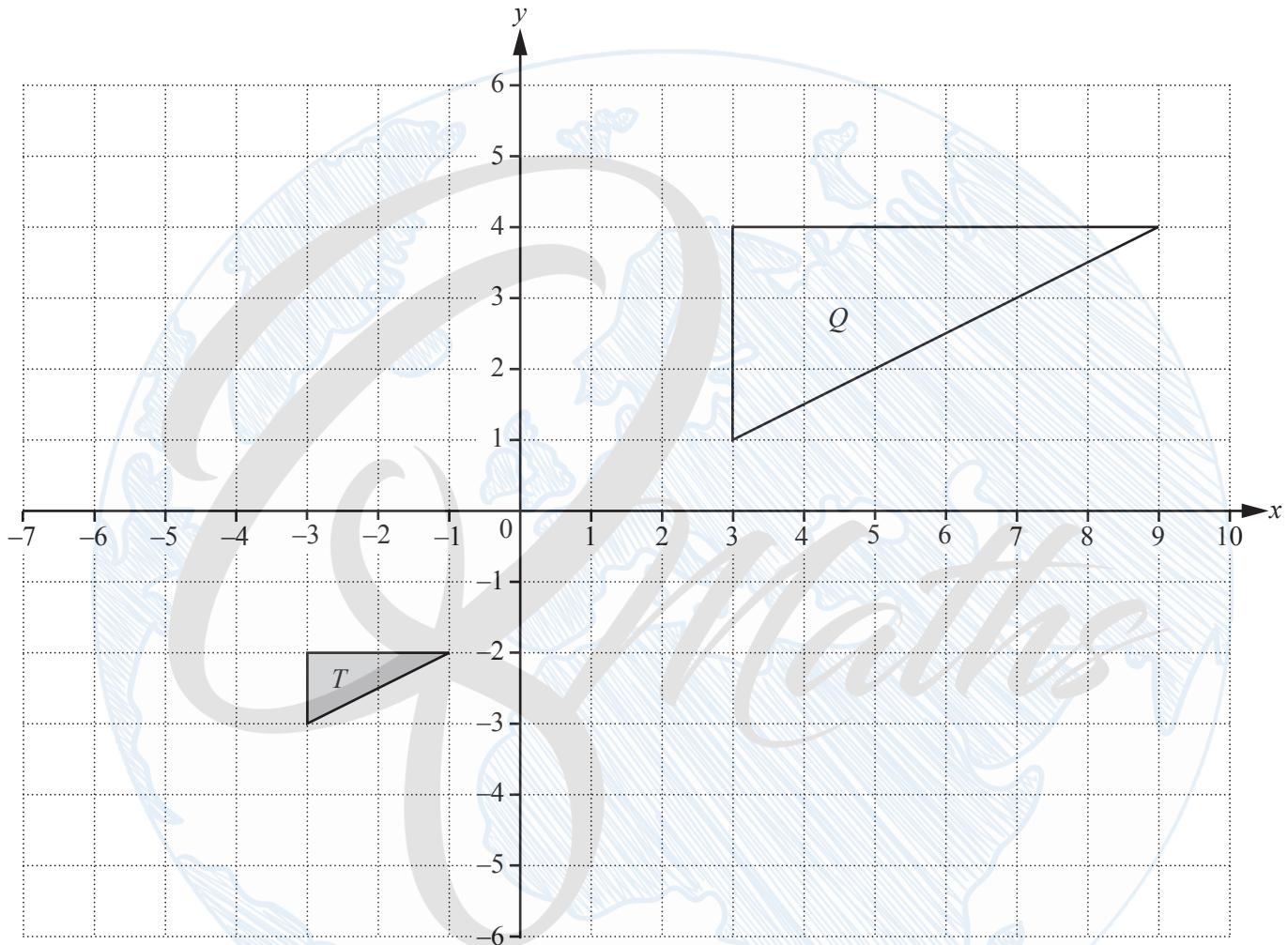
- (ii) Draw the reflection of triangle  $P$  in the line  $y = 3$ .

[2]

- (c) Draw the image of triangle  $X$  after the transformation represented by the matrix  $\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$ .

[3]

2 (a)



- (i) Draw the image of triangle  $T$  after a translation by the vector  $\begin{pmatrix} 5 \\ -2 \end{pmatrix}$ . [2]
- (ii) Draw the image of triangle  $T$  after a reflection in the line  $y = 1$ . [2]
- (iii) Describe fully the **single** transformation that maps triangle  $T$  onto triangle  $Q$ .

[3]

$$(b) \quad M = \begin{pmatrix} 1 & 2 \\ 3 & 4 \end{pmatrix} \quad N = \begin{pmatrix} 4 & 3 \\ 1 & k \end{pmatrix} \quad P = \begin{pmatrix} 1 & 3 \\ 0 & 6 \end{pmatrix}$$

(i) Work out  $M + P$ .

$$\left( \quad \quad \right) [1]$$

(ii) Work out  $PM$ .

$$\left( \quad \quad \right) [2]$$

(iii)  $|M| = |N|$

Find the value of  $k$ .

$$k = \dots \dots \dots [3]$$

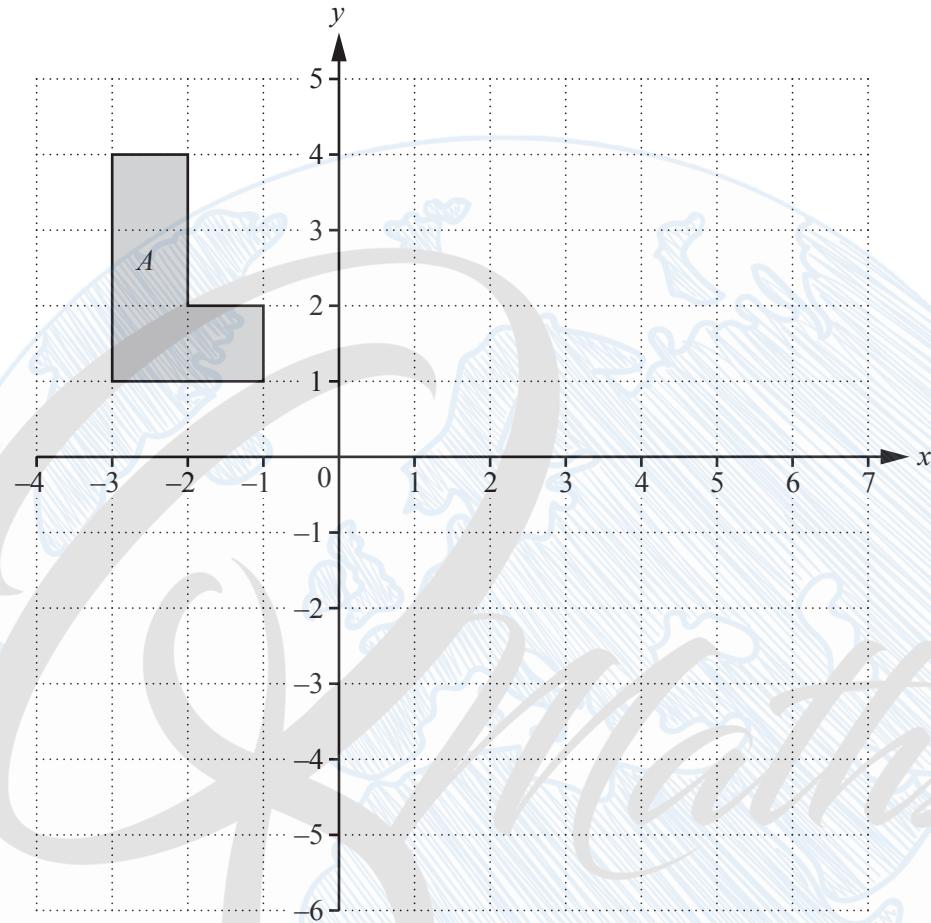
(c) (i) Describe fully the **single** transformation represented by the matrix  $\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$ .

$$\dots \dots \dots [3]$$

(ii) Find the matrix which represents a reflection in the line  $y = x$ .

$$\left( \quad \quad \right) [2]$$

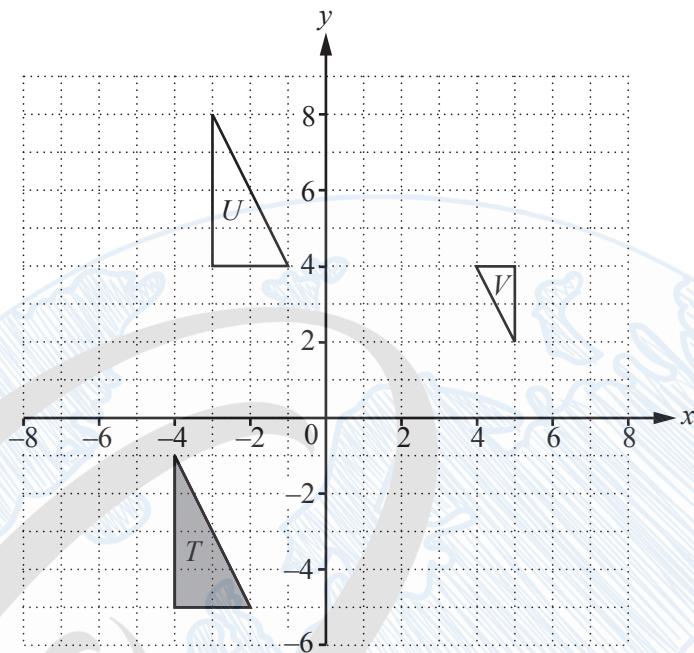
3 (a)



On the grid, draw the image of

- (i) shape  $A$  after a reflection in the line  $x = 1$ , [2]
  - (ii) shape  $A$  after an enlargement with scale factor  $-2$ , centre  $(0, 1)$ , [2]
  - (iii) shape  $A$  after the transformation represented by the matrix  $\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$ . [3]
- (b)** Describe fully the single transformation represented by the matrix  $\begin{pmatrix} 3 & 0 \\ 0 & 3 \end{pmatrix}$ .

[3]



- (a) (i) Draw the image of triangle  $T$  after a reflection in the line  $x = 0$ . [2]

.....  
..... [2]

- (ii) Draw the image of triangle  $T$  after a rotation through  $90^\circ$  clockwise about  $(-2, -1)$ .

.....  
..... [2]

- (iii) Describe fully the **single** transformation that maps triangle  $T$  onto triangle  $U$ .

- (iv) Describe fully the **single** transformation that maps triangle  $T$  onto triangle  $V$ .

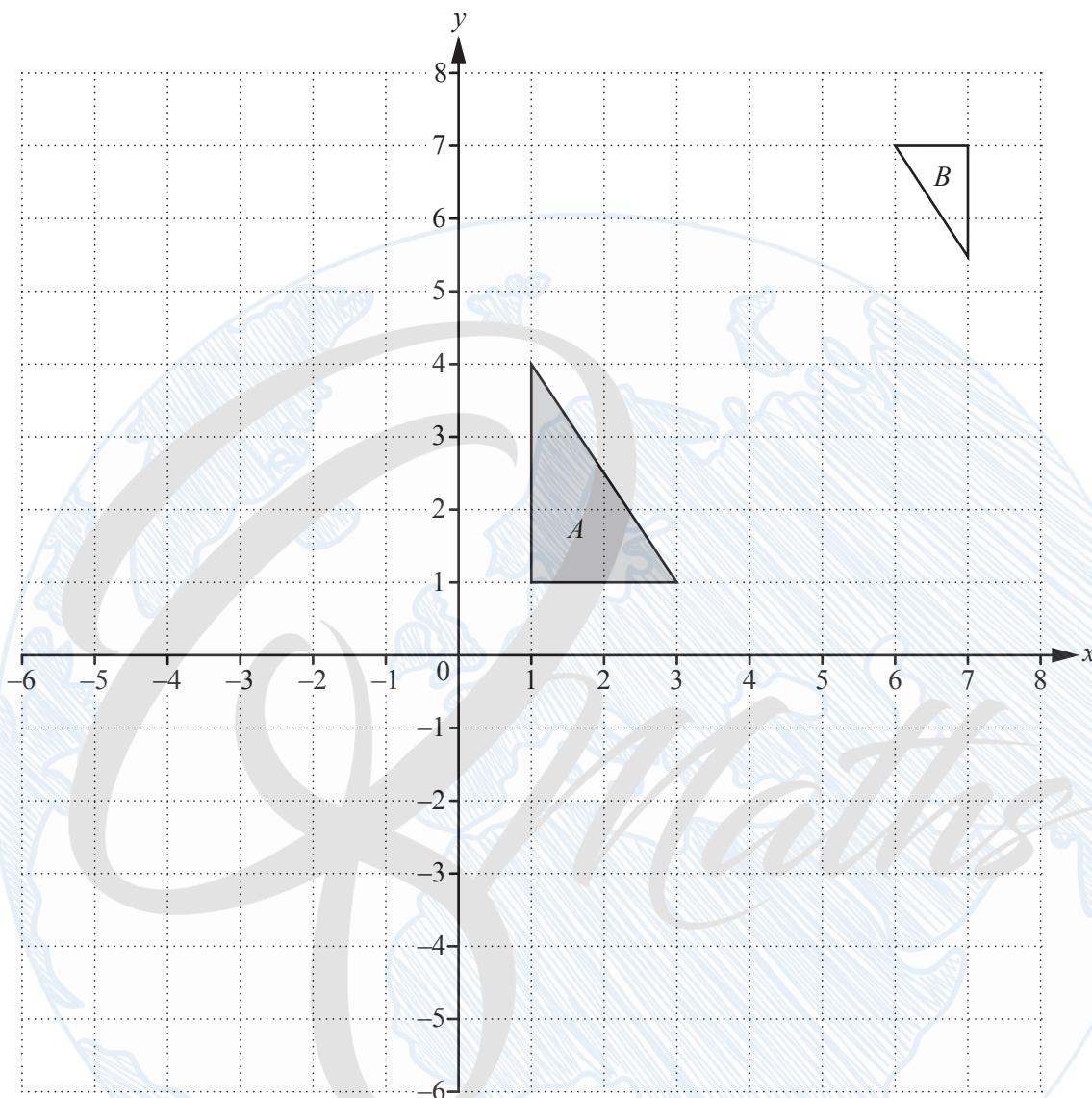
- (b) (i) Find the matrix that represents the transformation in part (a)(i).

*www.Q8Maths.com*  $\begin{pmatrix} & \\ & \end{pmatrix}$  [2]

- (ii) Describe fully the **single** transformation represented by the inverse of the matrix in part (b)(i).

.....  
..... [2]

3



- (a) (i) Draw the image of triangle A after reflection in the line  $x = 4$ . [2]

- (ii) Draw the image of triangle A after rotation of  $90^\circ$  anticlockwise about  $(0, 0)$ . [2]

- (iii) Draw the image of triangle A after translation by the vector  $\begin{pmatrix} 1 \\ -5 \end{pmatrix}$ . [2]

- (b) Describe fully the **single** transformation that maps triangle A onto triangle B.
- .....
- .....

[3]

- (c) Find the matrix that represents the transformation in part (a)(ii).

$$\left( \quad \quad \right) [2]$$

(d) Point  $P$  has co-ordinates  $(4, 1)$ .

$\mathbf{F} = \begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$  and  $\mathbf{G} = \begin{pmatrix} 1 & 0 \\ 0 & 2 \end{pmatrix}$  represent transformations.

(i) Find  $\mathbf{G}(P)$ , the image of  $P$  after the transformation represented by  $\mathbf{G}$ .

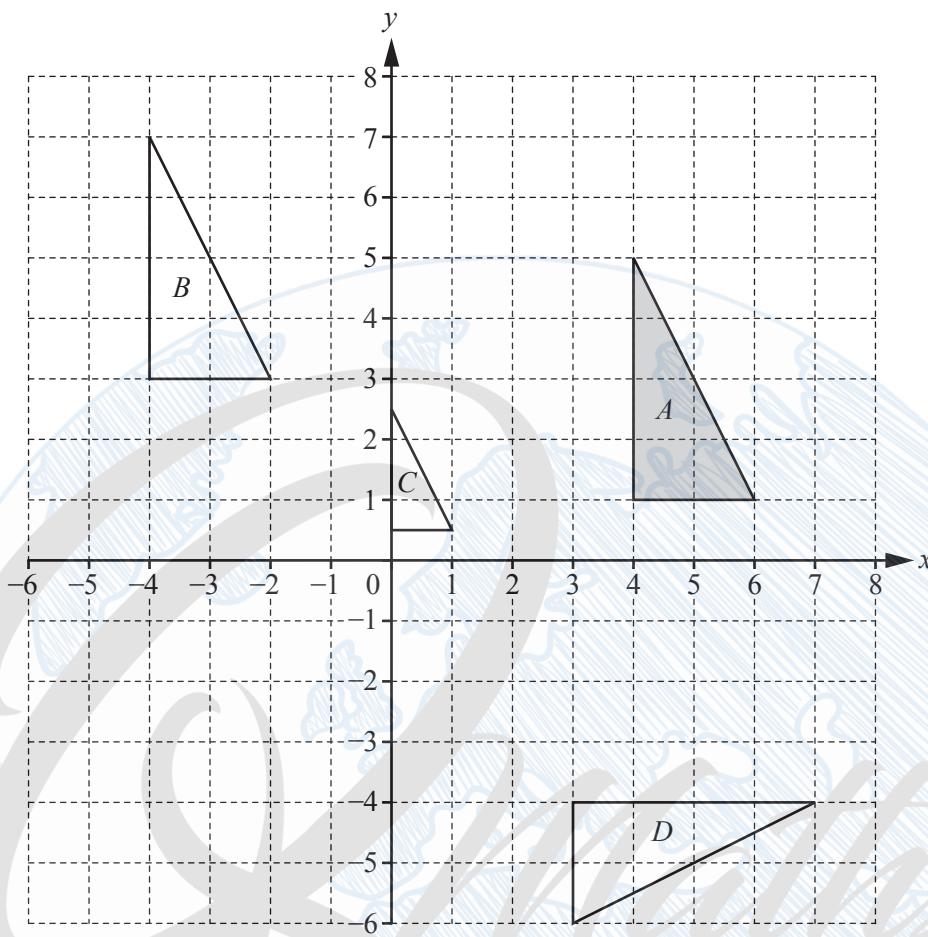
(....., ....) [2]

(ii) Find  $\mathbf{GF}(P)$ .

(....., ....) [3]

(iii) Find the matrix  $\mathbf{Q}$  such that  $\mathbf{GQ}(P) = P$ .

( ) [3]



(a) Describe fully the **single** transformation that maps

- (i) triangle A onto triangle B,

[2]

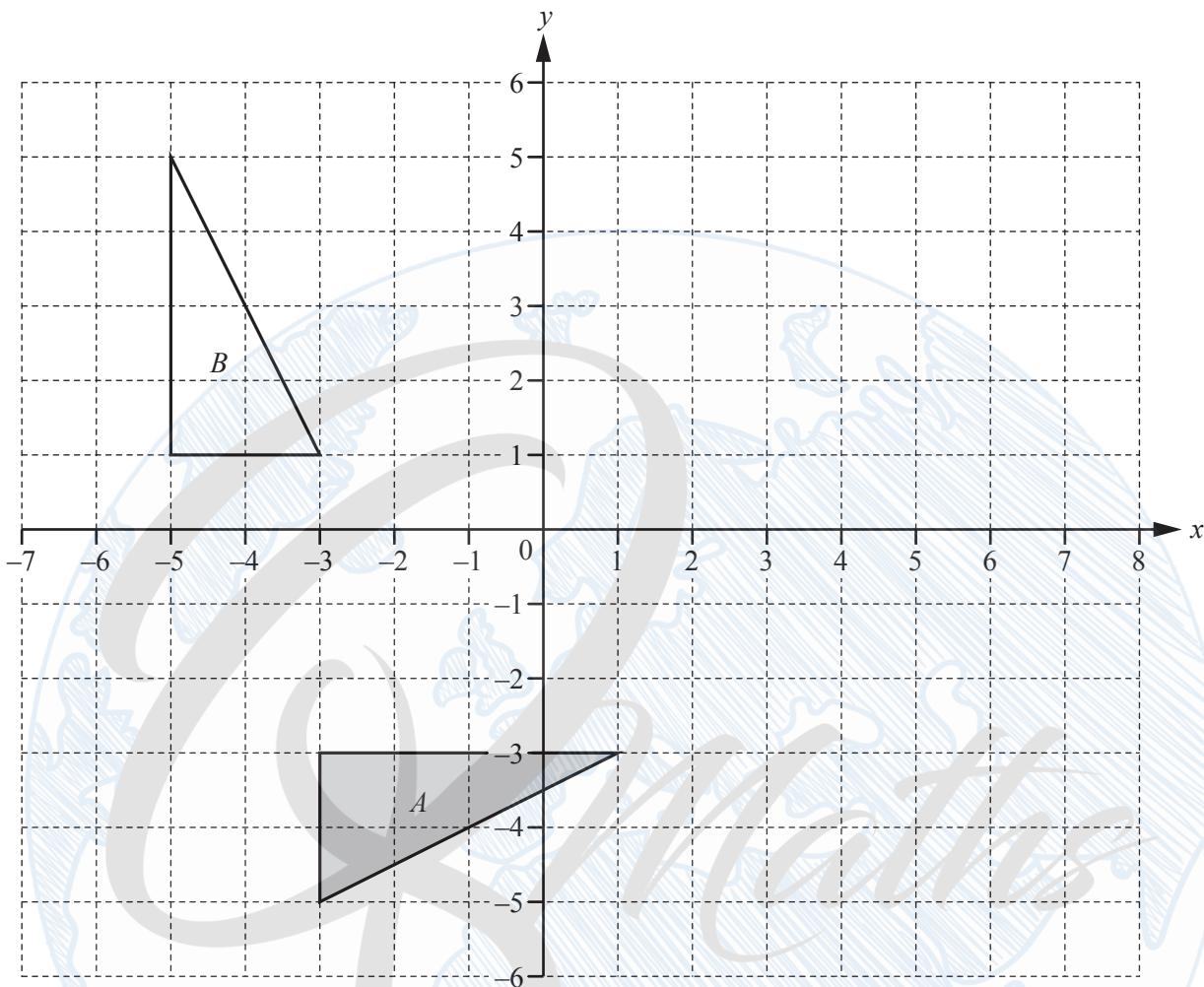
- (ii) triangle A onto triangle C,

[3]

- (iii) triangle A onto triangle D.

[3]

(b) On the grid, draw the image of triangle A after an enlargement by scale factor 2, centre (7, 3). [2]

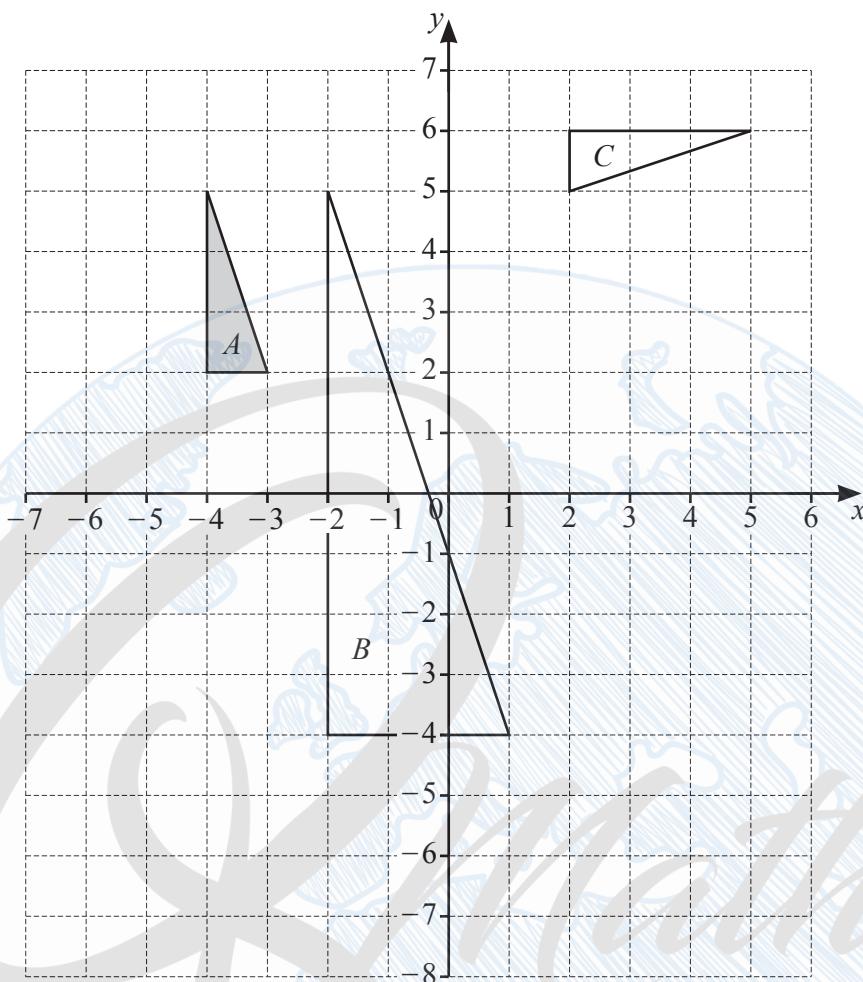


- (a) (i) Draw the image of triangle  $A$  after a reflection in the line  $x = 2$ . [2]
- (ii) Draw the image of triangle  $A$  after a translation by the vector  $\begin{pmatrix} -2 \\ 4 \end{pmatrix}$ . [2]
- (iii) Draw the image of triangle  $A$  after an enlargement by scale factor  $-\frac{1}{2}$ , centre  $(3, 1)$ . [3]

- (b) Describe fully the **single** transformation that maps triangle  $A$  onto triangle  $B$ .

..... *www.Q8Maths.com* .....

- (c) Describe fully the **single** transformation represented by the matrix  $\begin{pmatrix} 0 & -1 \\ -1 & 0 \end{pmatrix}$ .
- ..... [2]



(a) Draw the image of shape  $A$  after a translation by the vector  $\begin{pmatrix} 8 \\ -6 \end{pmatrix}$ . [2]

(b) Draw the image of shape  $A$  after a reflection in the line  $y = -1$ . [2]

(c) Describe fully the **single** transformation that maps shape  $A$  onto shape  $B$ .

.....

[3]

(d) Describe fully the **single** transformation that maps shape  $A$  onto shape  $C$ .

.....

[3]