

# Circles – Paper 2 – Mark Scheme

## Question 1

|    |        |   |  |
|----|--------|---|--|
| 17 | (a) 52 | 1 |  |
|    | (b) 64 | 1 |  |
|    | (c) 71 | 2 |  |

## Question 2

|   |        |   |  |
|---|--------|---|--|
| 4 | (a) 40 | 1 |  |
|   | (b) 65 | 1 |  |

## Question 3

|    |                              |   |                                                                                               |
|----|------------------------------|---|-----------------------------------------------------------------------------------------------|
| 23 | (a) (Angles in) same segment | 1 | Allow (angles on) the same arc<br><br><b>B1</b> $OBC$ or $OCB = \frac{1}{2}(180 - 86) (= 47)$ |
|    | (b) (i) 100                  | 1 |                                                                                               |
|    | (ii) 43                      | 1 |                                                                                               |
|    | (iii) 3                      | 2 |                                                                                               |

## Question 4

|    |                 |   |                                                                                                   |
|----|-----------------|---|---------------------------------------------------------------------------------------------------|
| 17 | (a) $66^\circ$  | 2 | <b>M1</b> for $90^\circ$ clearly identified as $A$<br><br><b>B1</b> for $OBA$ or $OAB = 57^\circ$ |
|    | (b) $33^\circ$  | 1 |                                                                                                   |
|    | (c) $123^\circ$ | 2 |                                                                                                   |

## Question 5

|    |        |     |  |
|----|--------|-----|--|
| 13 | (a) 72 | 1   |  |
|    | (b) 36 | 1   |  |
|    | (c) 54 | 2ft |  |

## Question 6

|    |         |     |  |                        |
|----|---------|-----|--|------------------------|
| 20 | (a) 35  | 1   |  |                        |
|    | (b) 55  | 1ft |  | $90 - (a)$ but $b > 0$ |
|    | (c) 55  | 1ft |  | $= (b)$                |
|    | (d) 125 | 1ft |  | $180 - (c)$            |

## Question 7

|   |                  |     |  |
|---|------------------|-----|--|
| 7 | (a) ( $y =$ ) 80 | 1   |  |
|   | (b) ( $z =$ ) 40 | 1   |  |
|   | (c) ( $t =$ ) 10 | 1ft |  |

### Question 8

|    |                            |   |                                                                            |
|----|----------------------------|---|----------------------------------------------------------------------------|
| 22 | (a) Angles in same segment | 1 |                                                                            |
|    | (b) (i) 8.2(0)             | 2 | M1 for $\frac{CX}{3.84} = \frac{9.4}{4.4}$ (= 2.136) oe                    |
|    | (ii) 24.7                  | 2 | M1 for $\frac{\Delta}{5.41} = \left(\frac{9.4}{4.4}\right)^2$ (= 4.564) oe |

### Question 9

|    |              |   |                                                                                                                                                                                                                                                                      |
|----|--------------|---|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 20 | 64.8 to 64.9 | 6 | M2 $5 \tan 78$ soi by 23.5 or M1 $\tan 78 = \frac{PT}{5}$ or<br>$\frac{5}{\tan 12}$ or $\frac{5 \sin 78}{\sin 12}$<br>M2 $\frac{360 - 2 \times 78}{360} \times 2 \times \pi \times 5$ soi by 17.8<br>or M1 for $2\pi 5$ seen used<br>M1 for their arc + 2 (their PT) |
|----|--------------|---|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|

### Question 10

|   |     |   |                                                                                                              |
|---|-----|---|--------------------------------------------------------------------------------------------------------------|
| 6 | 144 | 2 | M1 for $ABC = 72$ or $AOC$ reflex = 216<br>Angles must be fully stated or marked in correct place on diagram |
|---|-----|---|--------------------------------------------------------------------------------------------------------------|

### Question 11

|    |        |   |                                                                                                                      |
|----|--------|---|----------------------------------------------------------------------------------------------------------------------|
| 10 | (a) 95 | 1 |                                                                                                                      |
|    | (b) 77 | 2 | B1 for [angle] $ACD = 58^\circ$ or [angle] $BAC = 19^\circ$ or [angle] $ANB = 103^\circ$ or [angle] $CAE = 66^\circ$ |

### Question 12

|    |         |   |                                               |
|----|---------|---|-----------------------------------------------|
| 12 | (a) 110 | 1 |                                               |
|    | (b) 79  | 2 | B1 for $DAC = 42$ or $ACB = 79$ or $ACD = 28$ |

### Question 13

|    |    |   |                                                     |
|----|----|---|-----------------------------------------------------|
| 14 | 52 | 3 | B2 for $AOB = 104$<br>or B1 for $OAB$ or $OBA = 38$ |
|----|----|---|-----------------------------------------------------|

### Question 14

|    |        |   |                                                  |
|----|--------|---|--------------------------------------------------|
| 13 | (a) 24 | 2 | M1 for $MOC = 48$                                |
|    | (b) 24 | 2 | M1 for $ACM = 66$<br>or<br>B1 for 48 – their (a) |

### Question 15

|    |        |   |                    |
|----|--------|---|--------------------|
| 13 | (a) 32 | 2 | B1 for $AOC = 116$ |
|    | (b) 35 | 2 | B1 for $CDA = 122$ |

### Question 16

|         |                                    |            |                                                                                                                                               |
|---------|------------------------------------|------------|-----------------------------------------------------------------------------------------------------------------------------------------------|
| 19 (a)  | $CBA$ and $BDA$ are equilateral oe | 1          |                                                                                                                                               |
| (b)     | 67[.0] or 67.02 to 67.03           | 2          | <b>M1</b> for $\frac{120}{360} \times \pi \times 8^2$ oe                                                                                      |
| (c) (i) | 39.3 or 39.28 to 39.33             | 3          | <b>M2FT</b> for <i>their</i> (b) $-\frac{1}{2} \times 8^2 \times \sin 120$ oe<br>or <b>M1</b> for $\frac{1}{2} \times 8^2 \times \sin 120$ oe |
| (ii)    | 78.6 or 78.7 or 78.56 to 78.66     | <b>1FT</b> | <b>FT 2</b> $\times$ <i>their</i> (c)(i) correctly evaluated                                                                                  |

### Question 17

|         |                                                                         |   |  |
|---------|-------------------------------------------------------------------------|---|--|
| 16 (a)  | 108                                                                     | 1 |  |
|         | Angle at <b>centre</b> is <b>twice</b> angle at <b>circumference</b> oe | 1 |  |
| (b) (i) | $-\frac{4}{3}$ oe                                                       | 1 |  |
| (ii)    | -1                                                                      | 1 |  |

### Question 18

|       |                          |   |                                                  |
|-------|--------------------------|---|--------------------------------------------------|
| 8 (a) | 90                       | 1 |                                                  |
| (b)   | 8.29 or 8.289... to 8.29 | 2 | <b>M1</b> for $\frac{OP}{11} = \tan 37^\circ$ oe |

### Question 19

|   |    |   |                                                                                                                       |
|---|----|---|-----------------------------------------------------------------------------------------------------------------------|
| 7 | 37 | 2 | <b>M1</b> for $180 - 90 - 53$ oe<br>or <b>B1</b> for 53 or the right angle, either marked in correct place on diagram |
|---|----|---|-----------------------------------------------------------------------------------------------------------------------|

### Question 20

|        |     |   |                                                               |
|--------|-----|---|---------------------------------------------------------------|
| 18 (a) | 47  | 1 |                                                               |
| (b)    | 117 | 2 | <b>M1</b> for $360 - (115 + 85 + 97)$                         |
| (c)    | 244 | 2 | <b>B1</b> for 116 seen at centre or 122 seen at circumference |

### Question 21

|        |                     |   |                                          |
|--------|---------------------|---|------------------------------------------|
| 11 (a) | 112                 | 1 |                                          |
| (b)    | 56                  | 1 |                                          |
| 12     | $2p^4$ final answer | 2 | <b>B1</b> for $kp^4$ or $2p^k$ as answer |
| 13     | $n > 3.75$          | 2 | <b>M1</b> for $7 + 8 < 5n - n$ oe        |

### Question 22

|    |                                                                                                          |   |                                                                                                                                                                                                                                                                                                                                                                                                          |
|----|----------------------------------------------------------------------------------------------------------|---|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 21 | 62 on answer line or clearly identified as $\angle ACB$<br><br>and<br><br>two correct supporting reasons | 4 | <b>B1</b> for $\angle AOB = 124$ or for <i>their</i> $\angle AOB \div 2$ or<br>other appropriate correct angle one step from $\angle ACB$<br><b>B1</b> for any correct reason<br>e.g. isosceles triangle or angles in triangle = 180<br><b>B1</b> for a different correct reason leading directly to $\angle ACB$<br>e.g. angle at circumference is $\frac{1}{2}$ angle at centre or<br><b>B1</b> for 62 |
|----|----------------------------------------------------------------------------------------------------------|---|----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|

### Question 23

|   |    |   |                                                         |
|---|----|---|---------------------------------------------------------|
| 6 | 42 | 2 | <b>M1</b> for $Q = 90$ or $WPQ = 90 - 42$ or $WPQ = 48$ |
|---|----|---|---------------------------------------------------------|

### Question 24

|       |           |   |                                                             |
|-------|-----------|---|-------------------------------------------------------------|
| 21(a) | [u =] 35  | 1 |                                                             |
|       | [v =] 110 | 2 | <b>B1</b> for $ACB$ or $ADB = 35$                           |
| 21(b) | 75        | 2 | <b>B1</b> for 150<br>or <b>M1</b> for $\frac{360 - 210}{2}$ |

### Question 25

|    |          |   |                                                                                                                   |
|----|----------|---|-------------------------------------------------------------------------------------------------------------------|
| 26 | [w =] 40 | 1 |                                                                                                                   |
|    | [x =] 95 | 2 | <b>B1</b> for angle $ABC = 85$<br>or <i>their</i> $w + \text{their } CBD = 85$                                    |
|    | [y =] 45 | 2 | <b>B1</b> for angle $CBD = 45$ or angle $ACD = 40$<br>or angle $ACD = \text{their } w$ or $y = \text{their } CBD$ |

### Question 26

|    |                                   |   |                                                                                                                                                                                                                                                                  |
|----|-----------------------------------|---|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| 22 | [w =] 54<br>[x =] 126<br>[y =] 60 | 3 | <b>B1</b> for [w =] 54<br><b>B1</b> for [x =] 126<br><br>If <b>B0 B0</b> for first two B marks then <b>B1</b> for<br><i>their</i> $w + \text{their } x = 180$<br><br><b>B1</b> for [y =] 60 or for<br><i>their</i> $w + \text{their } x + \text{their } y = 240$ |
|----|-----------------------------------|---|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|

### Question 27

|    |         |   |                                                                                                                |
|----|---------|---|----------------------------------------------------------------------------------------------------------------|
| 16 | 7.5 nfw | 3 | <b>M2</b> for $[OB^2 =] \left(\frac{12}{2}\right)^2 + 4.5^2$ oe<br>or <b>B1</b> for recognition of right angle |
|----|---------|---|----------------------------------------------------------------------------------------------------------------|

### Question 28

|    |     |   |                                                                        |
|----|-----|---|------------------------------------------------------------------------|
| 12 | 110 | 3 | <b>B2</b> for $ADC = 25$<br>or <b>B1</b> for $AEC = 135$ or $CAE = 25$ |
|----|-----|---|------------------------------------------------------------------------|

### Question 29

|   |           |     |                                      |
|---|-----------|-----|--------------------------------------|
| 9 | [x =] 55  | 1   |                                      |
|   | [y =] 125 | 1FT | correct or <b>FT</b> (180 – their x) |

**Question 30**

|          |          |          |  |
|----------|----------|----------|--|
| <b>3</b> | <i>B</i> | <b>1</b> |  |
|----------|----------|----------|--|